Lecture 12 – Quantum computers, Shor's algorithm, post-quantum cryptography

TEK4500

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MIT Technology Review

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Computing

NSA Says It "Must Act Now" Against the Quantum Computing Threat

The National Security Agency is worried that quantum computers will neutralize our best encryption – but doesn't yet know what to do about that problem.

by Tom Simonite February 3, 2016

Quantum computing – the starting point

International Journal of Theoretical Physics, Vol. 21, Nos. 6/7, 1982

Simulating Physics with Computers

Richard P. Feynman

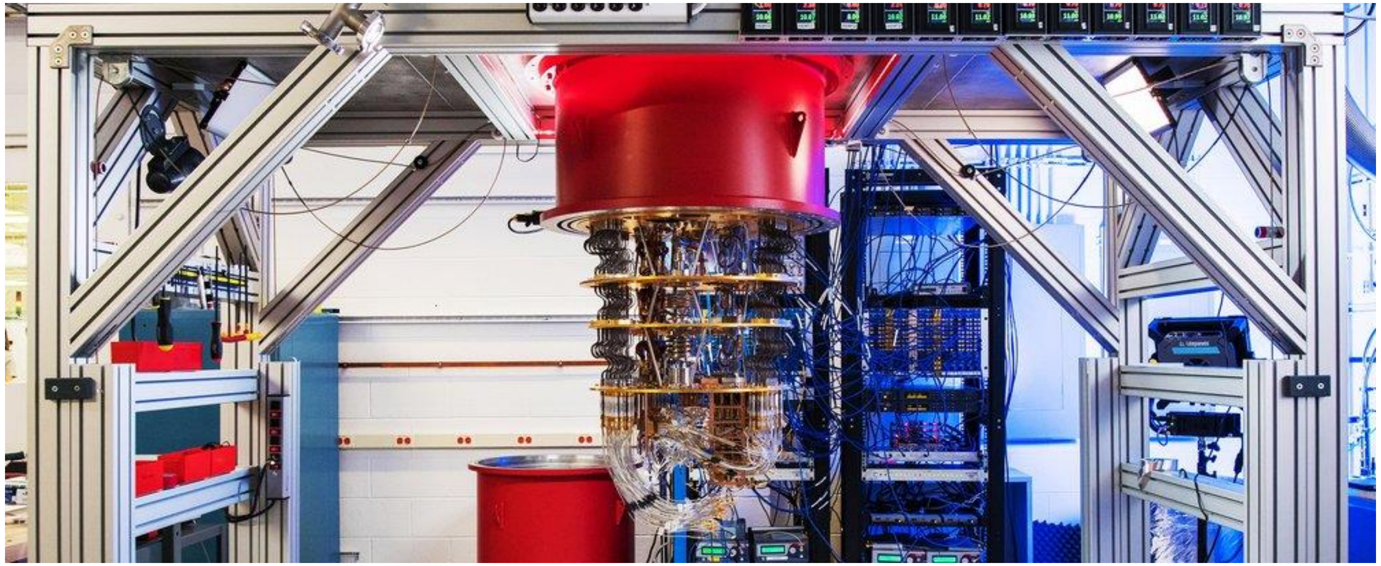
Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

Elements of (quantum) computing

- Three elements of all computations: data, operations, results

- Quantum computation
  - Data = **qubit**
  - Operation = **quantum gate**
  - Results = **measurements**



Qubits

- Classical bit: 0 1

- Qubit:

Can be in a **superposition** of two basic states $|0\rangle$ and $|1\rangle$

$$|\psi\rangle = \alpha\,|0\rangle + \beta\,|1\rangle \qquad \alpha, \beta \in \boldsymbol{C} \qquad |\alpha|^2 + |\beta|^2 = 1$$

But we can never observe α and β directly!

Must **measure** $|\psi\rangle$ to obtain its value $\Longrightarrow$ state *randomly* collapses to either $|0\rangle$ or $|1\rangle$

What's the probability of observing $|0\rangle$ or $|1\rangle$?

$$\Pr[\text{measure } |\psi\rangle \Rightarrow |0\rangle] = |\alpha|^2$$

$$\Pr[\text{measure } |\psi\rangle \Rightarrow |1\rangle] = |\beta|^2$$

Quantum states – multiple qubits

- A quantum computer consists of multiple qubits

$$|\psi_0\psi_1\rangle = \alpha\,|00\rangle + \beta\,|01\rangle + \gamma\,|10\rangle + \delta\,|11\rangle$$

$$\alpha, \beta, \gamma, \delta \in \boldsymbol{C}$$

$$|\alpha|^2 + |\beta|^2 + |\gamma|^2 + |\delta|^2 = 1$$

  - N-qubit system: 2^N basis states

$$|\boldsymbol{\psi}\rangle = |b_0 b_1 \cdots b_{N-1}\rangle = \sum_{i=0}^{2^N-1} \alpha_i |i\rangle$$

$$|\alpha_0|^2 + |\alpha_1|^2 + \cdots + |\alpha_{2^N-1}|^2 = 1$$

$$0.8|000\rangle - 0.6i|101\rangle = \begin{pmatrix} 0.8 \\ 0 \\ 0 \\ 0 \\ 0 \\ -0.6i \\ 0 \\ 0 \end{pmatrix}$$

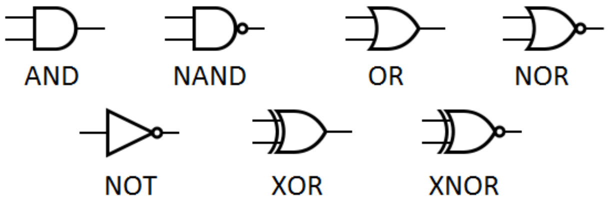
  - Representable by a 2^N element vector

$$|\boldsymbol{\psi}\rangle = \begin{pmatrix} \alpha_0 \\ \alpha_1 \\ \vdots \\ \alpha_{N-1} \end{pmatrix}$$

$$|000\rangle = \begin{pmatrix}1\\0\\0\\0\\0\\0\\0\\0\end{pmatrix} \quad |001\rangle = \begin{pmatrix}0\\1\\0\\0\\0\\0\\0\\0\end{pmatrix} \quad |010\rangle = \begin{pmatrix}0\\0\\1\\0\\0\\0\\0\\0\end{pmatrix} \quad |011\rangle = \begin{pmatrix}0\\0\\0\\1\\0\\0\\0\\0\end{pmatrix} \quad |100\rangle = \begin{pmatrix}0\\0\\0\\0\\1\\0\\0\\0\end{pmatrix} \quad |101\rangle = \begin{pmatrix}0\\0\\0\\0\\0\\1\\0\\0\end{pmatrix} \quad |110\rangle = \begin{pmatrix}0\\0\\0\\0\\0\\0\\1\\0\end{pmatrix} \quad |111\rangle = \begin{pmatrix}0\\0\\0\\0\\0\\0\\0\\1\end{pmatrix}$$

Quantum computation – quantum gates

- Classic bits are transformed using logical gates



- Qubits are transformed using **quantum gates**

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle \ \mapsto \ |\psi'\rangle = \alpha'|0\rangle + \beta'|1\rangle$$

Operator	Gate(s)		Matrix
Pauli-X (X)	X	$\oplus$	$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
Pauli-Z (Z)	Z		$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$
Hadamard (H)	H		$\frac{1}{\sqrt{2}}\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
Controlled Not (CNOT, CX)	$\bullet$ / $\oplus$		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$

(Quantum) NOT-gate (or X gate)

$$|0\rangle \overset{\boldsymbol{X}}{\mapsto} |1\rangle$$

$$|1\rangle \overset{\boldsymbol{X}}{\mapsto} |0\rangle$$

$$\alpha|0\rangle + \beta|1\rangle \overset{\boldsymbol{X}}{\mapsto} \beta|0\rangle + \alpha|1\rangle$$

X gate:

$$\boldsymbol{X} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

$$|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$|\psi\rangle = \begin{pmatrix} \alpha \\ \beta \end{pmatrix}$$

$$|1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$\boldsymbol{X}|0\rangle = \boldsymbol{X}\begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$\boldsymbol{X}|1\rangle = \boldsymbol{X}\begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$\boldsymbol{X}|\psi\rangle = \boldsymbol{X}\begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \ ?$$

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}\begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}\begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}\begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \begin{pmatrix} \beta \\ \alpha \end{pmatrix}$$

The Hadamard gate

$$|0\rangle \overset{H}{\mapsto} \frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

$$|1\rangle \overset{H}{\mapsto} \frac{|0\rangle - |1\rangle}{\sqrt{2}}$$

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

$$\Pr[\text{measure } |\psi\rangle = |0\rangle] = |\alpha|^2$$

$$\Pr[\text{measure } |\psi\rangle = |1\rangle] = |\beta|^2$$

H gate:

$$\boldsymbol{H} = \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} \end{bmatrix}$$

$$\Pr[\text{measure } \boldsymbol{H}|0\rangle \Rightarrow |0\rangle] = \left|\frac{1}{\sqrt{2}}\right|^2 = 0.5$$

$$\Pr[\text{measure } \boldsymbol{H}|1\rangle \Rightarrow |1\rangle] = \left|\frac{1}{\sqrt{2}}\right|^2 = 0.5$$

The Hadamard gate allows us to create random bits!

$$\begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} \end{bmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1/\sqrt{2} \\ 1/\sqrt{2} \end{pmatrix}$$

$$\begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} \end{bmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1/\sqrt{2} \\ -1/\sqrt{2} \end{pmatrix}$$

Controlled-NOT gate (CNOT)

CNOT

$|00\rangle \mapsto |00\rangle$

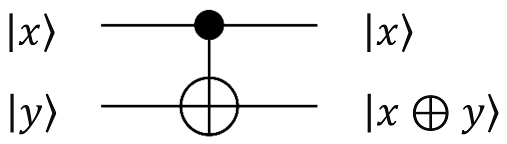
$|01\rangle \mapsto |01\rangle$

$|10\rangle \mapsto |11\rangle$

$|11\rangle \mapsto |10\rangle$

CNOT gate:

$$\mathbf{CNOT} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

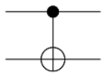
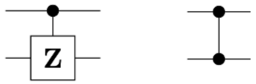
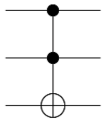


$|10\rangle$ $|11\rangle$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{pmatrix} \alpha \\ \beta \\ \gamma \\ \delta \end{pmatrix} = \begin{pmatrix} \alpha \\ \beta \\ \delta \\ \gamma \end{pmatrix}$$

Many other gates…

Operator	Gate(s)		Matrix
Pauli-X (X)	X	$\oplus$	$\begin{bmatrix}0 & 1\\ 1 & 0\end{bmatrix}$
Pauli-Y (Y)	Y		$\begin{bmatrix}0 & -i\\ i & 0\end{bmatrix}$
Pauli-Z (Z)	Z		$\begin{bmatrix}1 & 0\\ 0 & -1\end{bmatrix}$
Hadamard (H)	H		$\frac{1}{\sqrt{2}}\begin{bmatrix}1 & 1\\ 1 & -1\end{bmatrix}$
Phase (S, P)	S		$\begin{bmatrix}1 & 0\\ 0 & i\end{bmatrix}$
$\pi/8$ (T)	T		$\begin{bmatrix}1 & 0\\ 0 & e^{i\pi/4}\end{bmatrix}$
Controlled Not (CNOT, CX)			$\begin{bmatrix}1&0&0&0\\0&1&0&0\\0&0&0&1\\0&0&1&0\end{bmatrix}$
Controlled Z (CZ)			$\begin{bmatrix}1&0&0&0\\0&1&0&0\\0&0&1&0\\0&0&0&-1\end{bmatrix}$
SWAP			$\begin{bmatrix}1&0&0&0\\0&0&1&0\\0&1&0&0\\0&0&0&1\end{bmatrix}$
Toffoli (CCNOT, CCX, TOFF)			$\begin{bmatrix}1&0&0&0&0&0&0&0\\0&1&0&0&0&0&0&0\\0&0&1&0&0&0&0&0\\0&0&0&1&0&0&0&0\\0&0&0&0&1&0&0&0\\0&0&0&0&0&1&0&0\\0&0&0&0&0&0&0&1\\0&0&0&0&0&0&1&0\end{bmatrix}$

Universal for classical logic!

Quantum gates

- Turns out that all quantum gates can be described by matrices
  - In fact, very special matrices: unitary matrices
  - … and *only* unitary matrices! (fact of nature)

$$|0\rangle \overset{X}{\mapsto} |1\rangle \qquad |1\rangle \overset{X}{\mapsto} |0\rangle \qquad \boldsymbol{X} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

- Quantum operations are *linear* and can be combined

$$|0\rangle \overset{Z}{\mapsto} |0\rangle \qquad |1\rangle \overset{Z}{\mapsto} -|1\rangle \qquad \boldsymbol{Z} = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

$$|\psi_0\rangle \overset{Z}{\mapsto} |\psi_1\rangle \overset{X}{\mapsto} |\psi_2\rangle \overset{H}{\mapsto} |\psi_3\rangle \overset{Z}{\mapsto} |\psi_4\rangle$$

$$\boldsymbol{ZHXZ}|\psi_0\rangle = |\psi_4\rangle$$

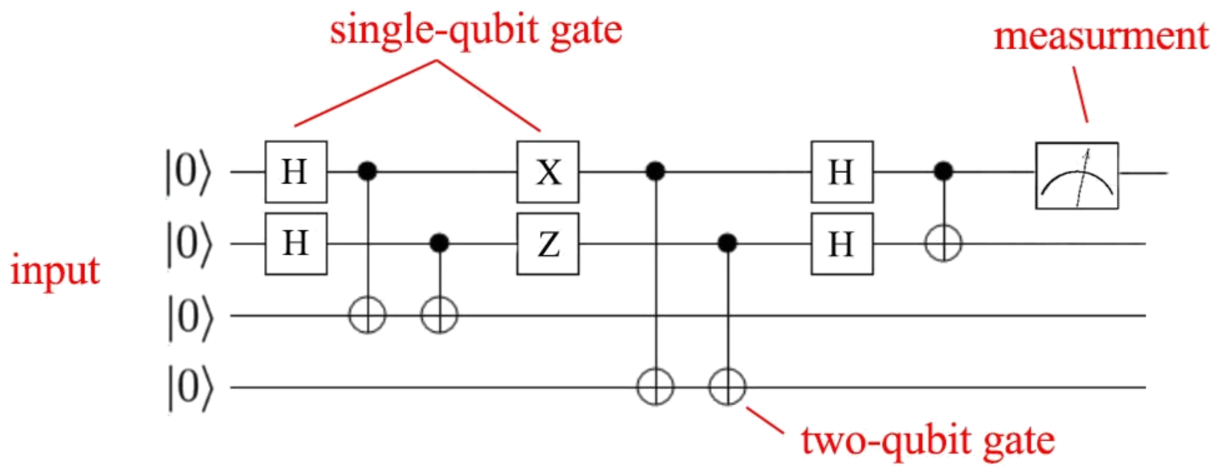
$$|0\rangle \overset{H}{\mapsto} \frac{|0\rangle + |1\rangle}{\sqrt{2}} \qquad |1\rangle \overset{H}{\mapsto} \frac{|0\rangle - |1\rangle}{\sqrt{2}} \qquad \boldsymbol{H} = \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} \end{bmatrix}$$

$$\boldsymbol{ZHXZ}|0\rangle = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$= \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ 1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1/\sqrt{2} \\ 1/\sqrt{2} \end{pmatrix}$$

Quantum computer

- A **quantum computer** consists of:
  - N input qubits
  - a sequence of quantum gates
  - N output qubits
  - result = measurement of final quantum state (output qubits)



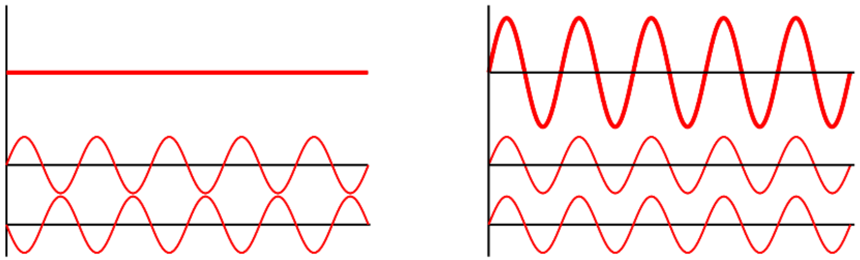
What makes quantum computation special?

- **Warning:** a quantum computer does *not* simply "try out all solutions in parallel"

- The magic comes from allowing *complex* amplitudes (or even just negative reals)

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle \qquad \alpha, \beta \in \boldsymbol{C}$$

- **Quantum interference:** can *carefully* choreograph computations so wrong answers "cancel out" their amplitudes, while correct answers "combine"



  - increases probability of measuring correct result
  - only a few special problems allow this choreography

https://www.smbc-comics.com/comic/the-talk-3

Example (interference)

$$G = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ 0 & 0 & \frac{1}{\sqrt{2}} & \frac{-1}{\sqrt{2}} \end{bmatrix}$$

$G|10\rangle$ $\quad \frac{1}{\sqrt{2}}|10\rangle + \frac{1}{\sqrt{2}}|11\rangle$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ 0 & 0 & \frac{1}{\sqrt{2}} & \frac{-1}{\sqrt{2}} \end{bmatrix} \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix}$$

$G|11\rangle$ $\quad \frac{1}{\sqrt{2}}|10\rangle - \frac{1}{\sqrt{2}}|11\rangle$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ 0 & 0 & \frac{1}{\sqrt{2}} & \frac{-1}{\sqrt{2}} \end{bmatrix} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ \frac{1}{\sqrt{2}} \\ \frac{-1}{\sqrt{2}} \end{pmatrix}$$

$$G\left(\frac{1}{\sqrt{2}}|10\rangle - \frac{1}{\sqrt{2}}|11\rangle\right) = \frac{1}{\sqrt{2}}(G|10\rangle - G|11\rangle)$$

$$= \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}|10\rangle + \frac{1}{\sqrt{2}}|11\rangle - \frac{1}{\sqrt{2}}|10\rangle + \frac{1}{\sqrt{2}}|11\rangle\right)$$

$$= |11\rangle$$

Shor's algorithm

Polynomial-Time Algorithms for Prime Factorization and Discrete Logarithms on a Quantum Computer*

Peter W. Shor†

1994

Abstract

A digital computer is generally believed to be an efficient universal computing device; that is, it is believed able to simulate any physical computing device with an increase in computation time by at most a polynomial factor. This may not be true when quantum mechanics is taken into consideration. This paper considers factoring integers and finding discrete logarithms, two problems which are generally thought to be hard on a classical computer and which have been used as the basis of several proposed cryptosystems. Efficient randomized algorithms are given for these two problems on a hypothetical quantum computer. These algorithms take a number of steps polynomial in the input size, e.g., the number of digits of the integer to be factored.

Keywords: algorithmic number theory, prime factorization, discrete logarithms, Church's thesis, quantum computers, foundations of quantum mechanics, spin systems, Fourier transforms

First: something completely different

$2, 4, 8, 16, 32, 64, 128, 256, 512, 1024, \ldots$

$2, 4, 8, 1, 2, 4, 8, 1, 2, 4, 8, 1, 2 \ldots$ $\mod 15$

$2, 4, 8, 16, 11, 1, 2, 4, 8, 16, 11, 1, 2 \ldots$ $\mod 21$

sequences are periodic

Factoring to order-finding

$N = pq$

$|\langle a \rangle| = r$

$$a^1, a^2, a^3, \ldots, a^r, a^1, a^2 \ldots \pmod N$$

($a^r = 1$)

order of a = the smallest positive r such that $a^r = 1 \pmod N$

Euler's theorem: for all $a \in \mathbf{Z}_N^*$

$$a^{\phi(N)} = a^{(p-1)(q-1)} = 1 \pmod N$$

Fact: r must divide $(p-1)(q-1)$

Proof:

- $(p-1)(q-1) = sr + t \qquad 0 \le t < r$
- $a^{(p-1)(q-1)} = a^{sr+t} = a^{sr}a^t = (a^r)^s a^t = 1 \cdot a^t = 1 \bmod N \implies t = 0$ (since r is the *smallest*)
- $(p-1)(q-1) = sr$

QED

Conclusion: learn $r \implies$ we learn a factor of $(p-1)(q-1)$

repeat with a different $a \implies$ learn another factor of $(p-1)(q-1)$ (with high prob.)

eventually we can learn full $(p-1)(q-1) \implies$ can find p and q (Problem set 10)

Shor's algorithm

Where the quantum magic happens!

Shor's algorithm

Input: $N = pq$
Output: p and q

1. $a \overset{\$}{\leftarrow} \mathbf{Z}_N$
2. $r \leftarrow \text{Order}_N(a)$ // but how to find r?
3. use r to find $\phi(N)$
4. compute p and q from N and $\phi(N)$

Shor’s algorithm

- To factor N: find order of a in $\boldsymbol{Z}_N^*$

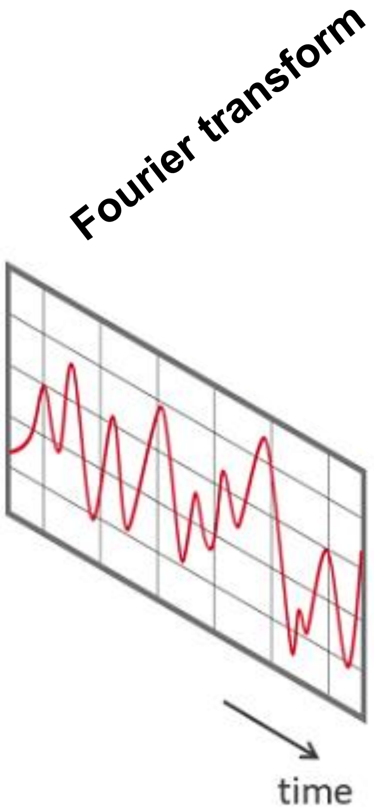
- Problem: r can be very large
  - Classical solutions take exponential time

- **Note:** the function $f(i) = a^i \bmod N$ is *periodic*:

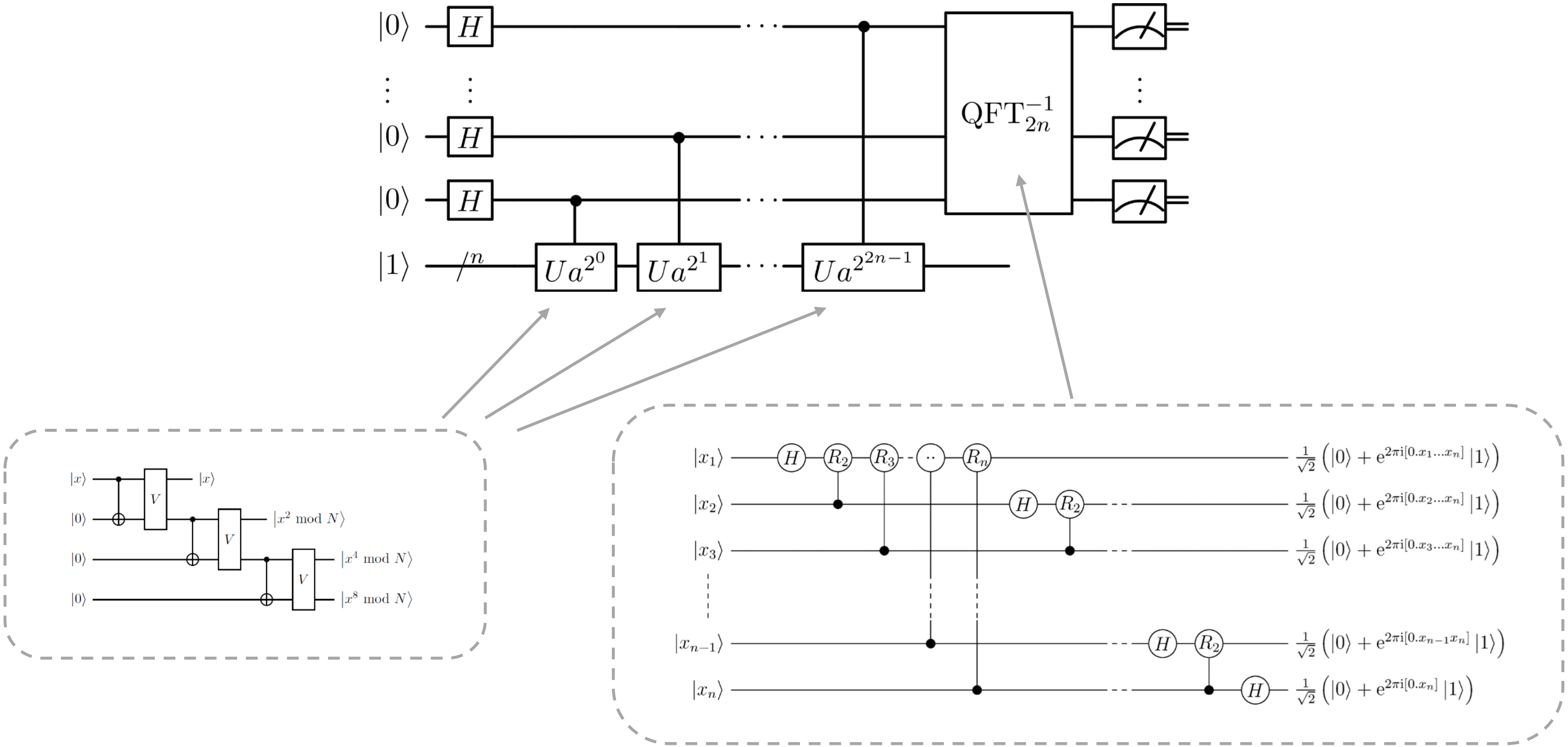
$$f(i + kr) = a^{i+kr} = a^i \bmod N = f(i)$$

  - finding signal frequencies ⟺ finding signal period

- Key ingredient of Shor's algorithm:
  quantum Fourier transform (QFT)



Shor's algorithm



Consequences of Shor's algorithm

- Cryptosystems broken by Shors' algorithm:
  - RSA
  - Diffie-Hellman
  - Schnorr
  - ElGamal
  - ECDSA

both $\boldsymbol{Z}_p^*$ and $E(\boldsymbol{F}_p)$

- …public-key crypto is dead

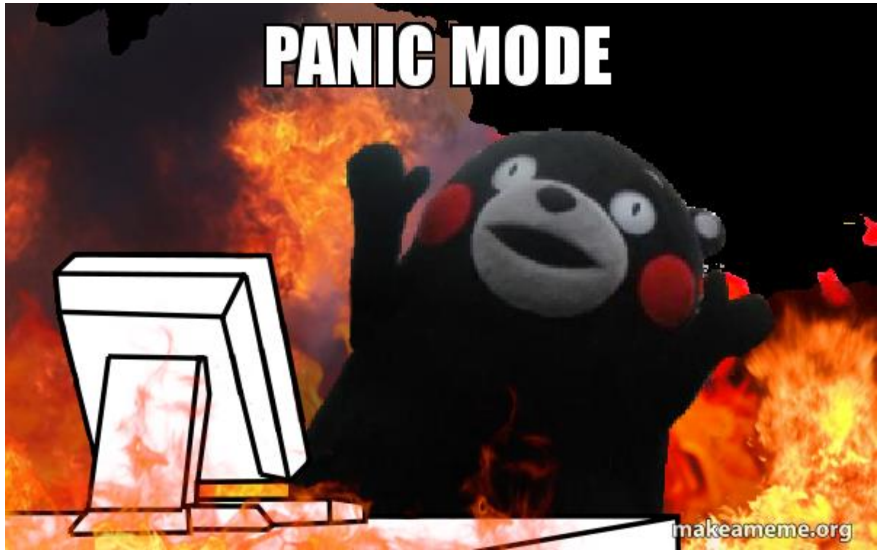
Shor's algorithm

Input: $N = pq$
Output: p and q

1. $a \overset{\$}{\leftarrow} \boldsymbol{Z}_N$
2. $r \leftarrow \mathrm{Order}_N(a)$ // QFT++
3. use r to find $\phi(N)$
4. compute p and q from N and $\phi(N)$

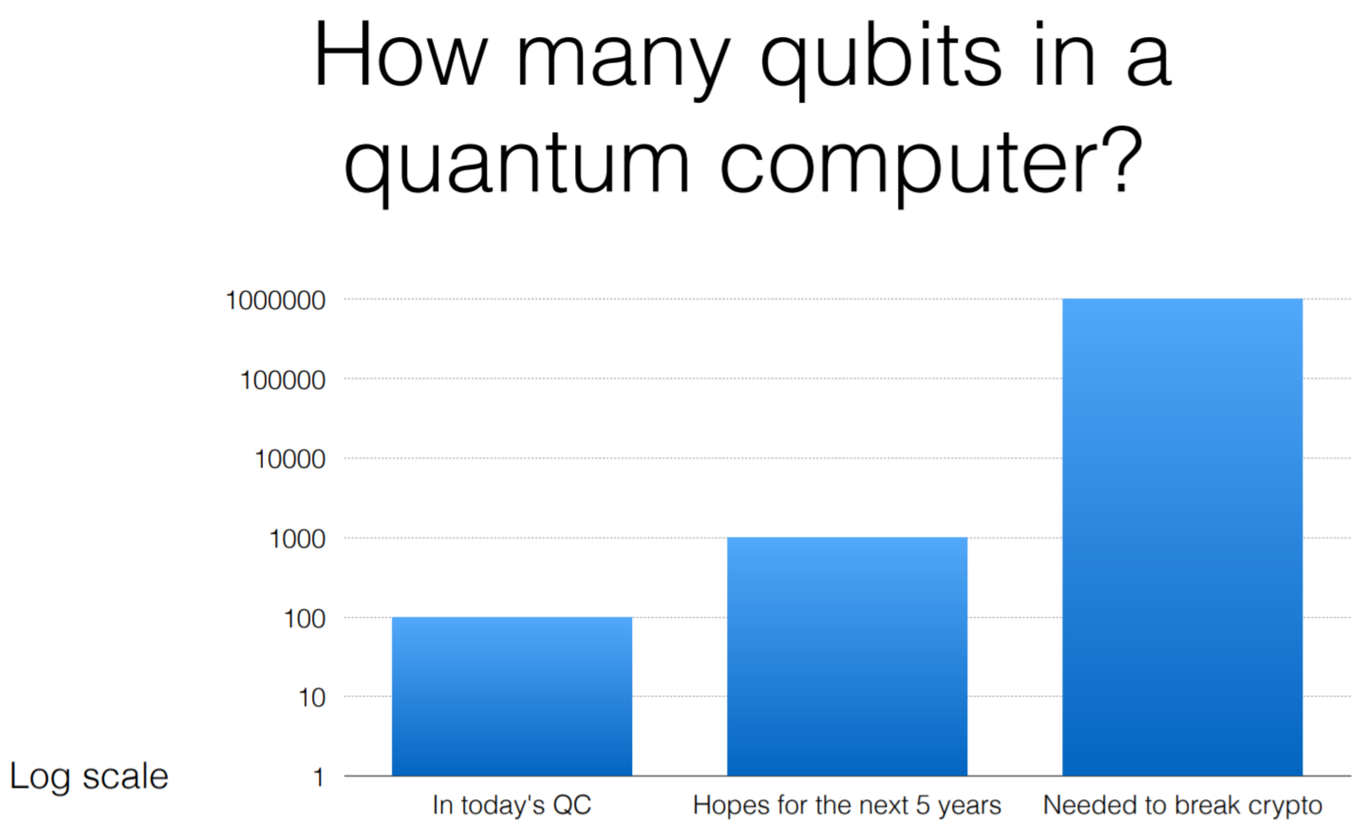
The quantum menace

- How far away is a quantum computer?
  - Nobody knows



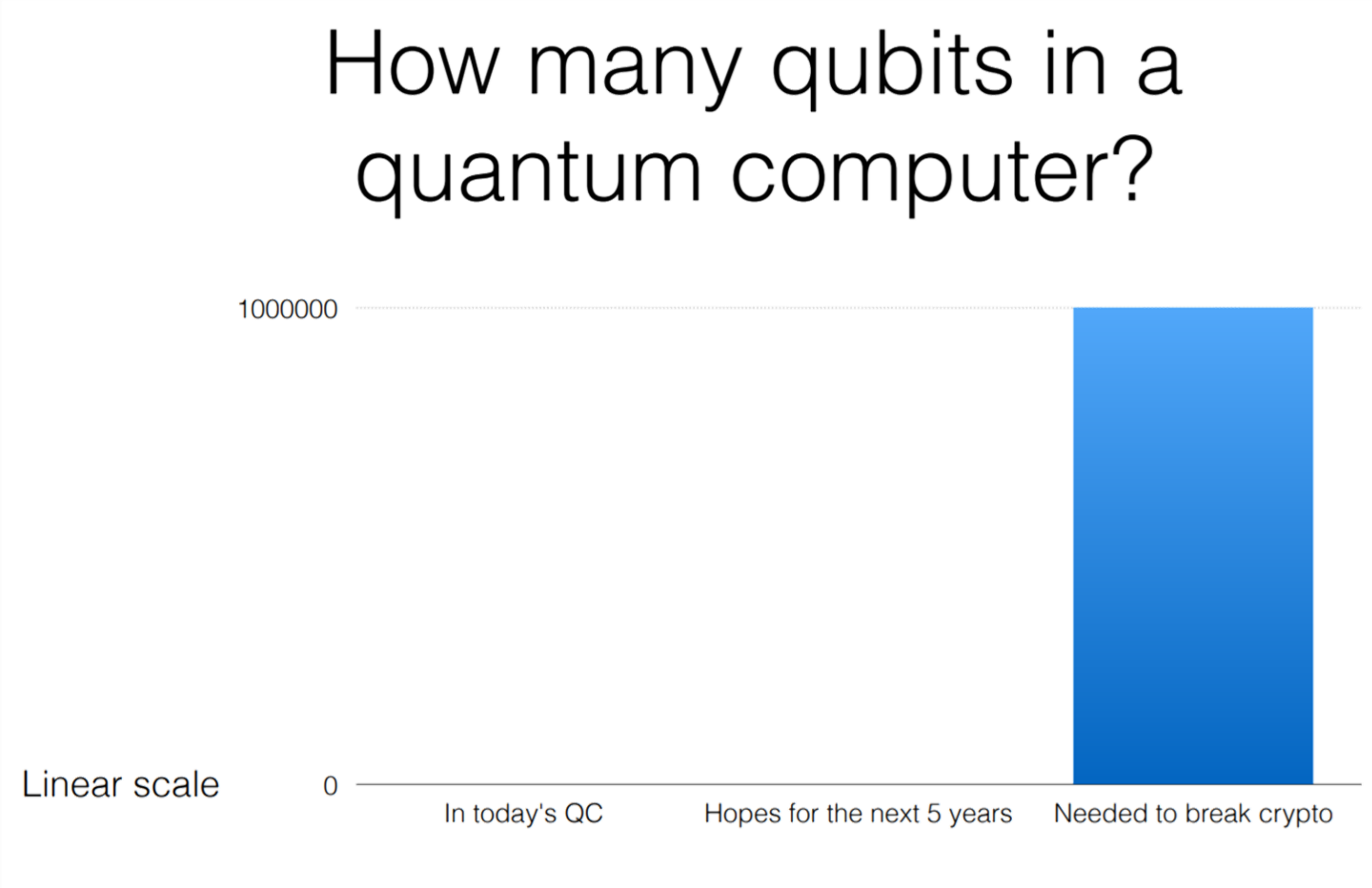
- Building large-scale quantum computers a huge engineering challenge
  - *very* susceptible to noise (decoherence)
  - requires quantum error correction (is it even possible?)
  - many *physical* qubits needed to simulate a single *logical* qubit
    - ≈ 1000 physical qubits needed for 1 logical qubit
    - ≈ 1000 logical qubits needed for Shor's algorithm
    - largest (known) quantum computers:
      ≈ 65 physical qubits (IBM; 2020) (no error correction)
      ≈ 53 physical qubits (Google; 2019) (no error correction; demonstrated *quantum supremacy*)

The quantum menace



Source: JP Aumasson; https://www.aumasson.jp/data/talks/quantum-cyberpeace-2021.pdf

The quantum menace



Source: JP Aumasson; https://www.aumasson.jp/data/talks/quantum-cyberpeace-2021.pdf

Dealing with quantum computers

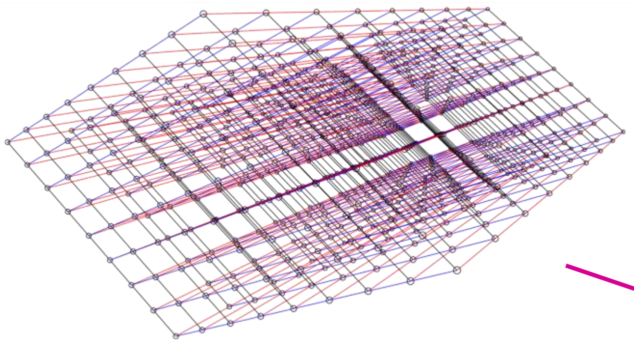
- **Symmetric cryptography**
  - Grover's algorithm: solves $\mathcal{O}(2^n)$ problems in $\mathcal{O}\left(2^{n/2}\right)$ quantum steps
  - Solution: double key-lengths $(128 \rightarrow 256)$

- **Quantum cryptography**
  - Use quantum mechanics to build cryptography

- **Post-quantum cryptography**
  - Classical algorithms believed to withstand quantum attacks

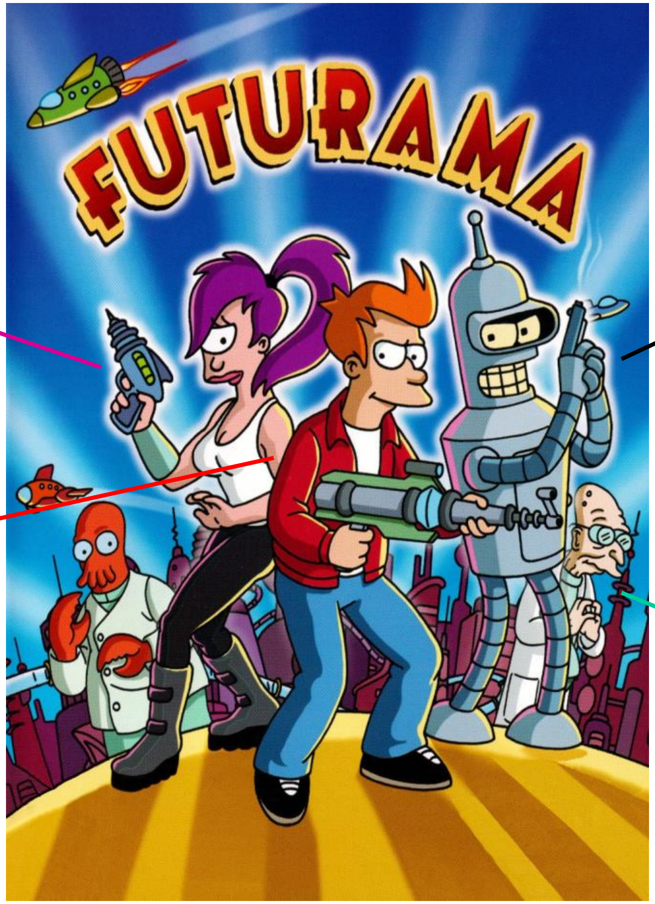
Post-quantum cryptography

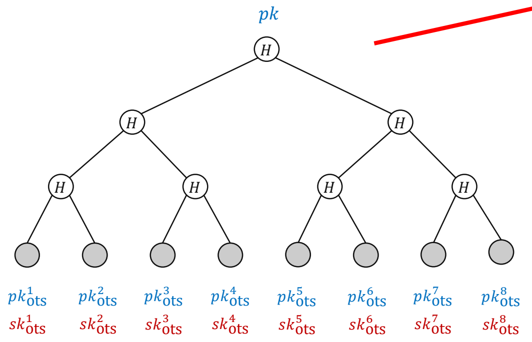
Lattice-based cryptography



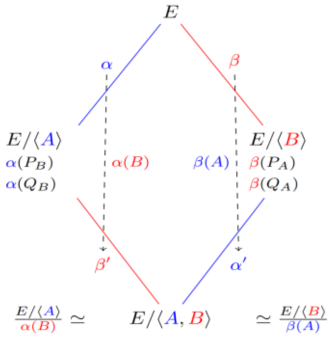
Code-based encryption

$$c = Gx + e \in F_2^n$$





Hash-based signatures



Supersingular isogeny key exchange

The NIST post-quantum competition

- Public competition to standardize post-quantum schemes
  - Public-key encryption
  - Digital signatures
- Started in 2017
  - Round 1: 69 submissions
  - Round 2: 26 candidates selected
  - Round 3: 15 candidates selected (current)
- Winner(s) expected in about a year

Algorithm (public-key encryption)	Problem
Classic McEliece	Code-based
CRYSTALS-KYBER	Lattice-based
NTRU	Lattice-based
SABER	Lattice-based
BIKE	Code-based
FrodoKEM	Lattice-based
HQC	Code-based
NTRU Prime	Lattice-based
SIKE	Isogeny-based

Algorithm (digital signatures)	Problem
CRYSTALS-DILITHIUM	Lattice-based
FALCON	Lattice-based
Rainbow	Multivariate-based
GeMSS	Multivariate-based
Picnic	ZKP
SPHINCS+	Hash-based

Learn more about post-quantum cryptography?

- Want to learn more about post-quantum cryptography?

- Sign up for TEK5550 - Advanced Topics in Cryptology next spring!

Next week

- Guest lecture
- Martin Strand, PhD, Norwegian Defence Research Establishment (FFI)
- Topic: blind signatures and anonymous authentication