## UiO Department of Technology Systems University of Oslo

# Lecture 11.2 Image Feature Extraction

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### **Image Analysis**

#### **Typical steps:**

- Pre-processing
- Segmentation (object detection)
- Feature extraction
- Feature selection
- Classifier training
- Evaluation of classifier performance.



## Features for image analysis

#### **Applications:**

- Remote sensing
- Medical imaging
- Character recognition
- Robot Vision
- ...

#### Major goal of image feature extraction:

Given an image, or a region within an image, generate the features that will subsequently be fed to a classifier in order to classify the image in one of the possible classes.

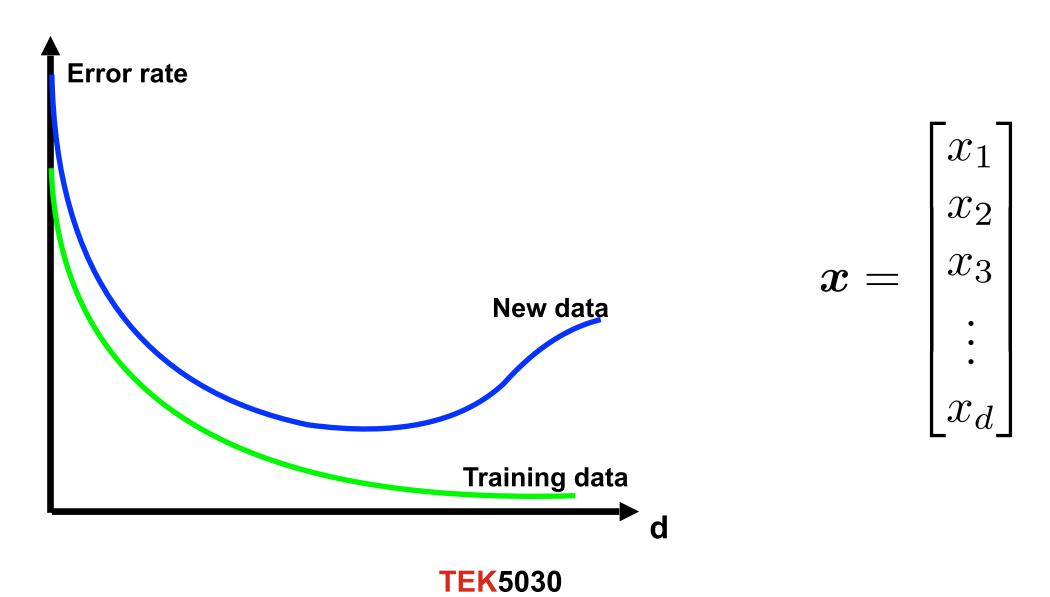
(Theodoridis & Koutroumbas: «Pattern Recognition», Elsevier 2006).

#### **Feature extraction**

The goal is to generate features that exhibit high information-packing properties:

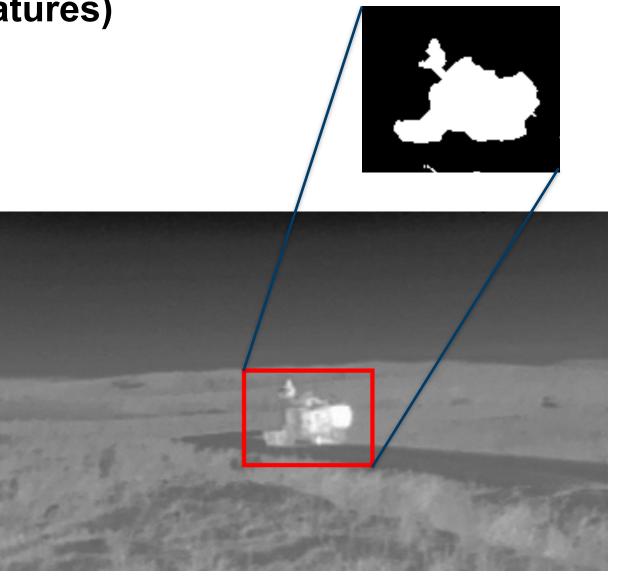
- Extract the information from the raw data that is most relevant for discrimination between the classes
- Extract features with low within-class variability and high between class variability
- Discard redundant information.
- The information in an image f[i,j] must be reduced to enable reliable classification (generalization)
- A 64x64 image → 4096-dimensional feature space!

## "Curse of dimensionality"



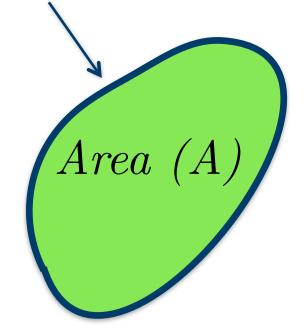
## Feature types (regional features)

- Colour features
- Gray level features
- Shape features
- Histogram (texture) features



## **Shape features - example**





Possible shape feature:

$$\frac{P^2}{A}$$

#### **Moments**

Geometric moments (order p, q):

$$m_{pq} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} x^p y^q f(x, y) dx dy \approx \sum_{i} \sum_{j} i^p j^q f[i, j]$$

Central moments:

$$\mu_{pq} = \sum_{i} \sum_{j} (i - \tilde{i})^{p} (j - \tilde{j})^{q} f[i, j] \text{ where } \begin{cases} \tilde{i} = \frac{m_{10}}{m_{00}} \\ \tilde{j} = \frac{m_{01}}{m_{00}} \end{cases}$$

$$\overline{m_{00}}$$

## **Binary images**

$$f[i,j] = \begin{cases} 1 \Rightarrow \text{Object pixel} \\ 0 \Rightarrow \text{Background pixel} \end{cases}$$



Area: 
$$m_{00} = \sum_{i} \sum_{j} f[i, j]$$

Center of mass: 
$$\begin{cases} m_{10} = \sum_{i} \sum_{j} i f[i, j] \Rightarrow & \tilde{i} = \frac{m_{10}}{m_{00}} \\ m_{01} = \sum_{i} \sum_{j} j f[i, j] \Rightarrow & \tilde{j} = \frac{m_{01}}{m_{00}} \end{cases}$$

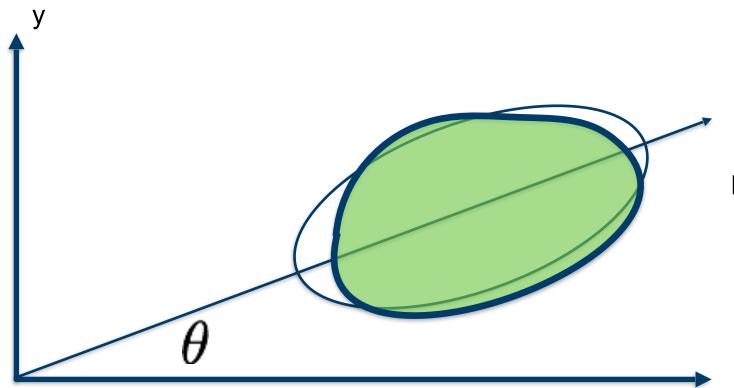
#### Moments of inertia

$$\mu_{20} = \sum_{i} \sum_{j} (i - \tilde{i})^2 f[i, j]$$

$$\mu_{02} = \sum_{i} \sum_{j} (j - \tilde{j})^2 f[i, j]$$

$$\mu_{11} = \sum_{i} \sum_{j} (i - \tilde{i})(j - \tilde{j})f[i, j]$$

## **Closest fitting ellipse**



Orientation:

$$\theta = \frac{1}{2} \tan^{-1} \left[ \frac{2\mu_{11}}{\mu_{20} - \mu_{02}} \right]$$

**Eccentricity:** 

$$\epsilon = \frac{(\mu_{20} - \mu_{02})^2 + 4\mu_{11}}{A}$$

X

## Major and minor axes

$$a^{2} = \frac{2(\mu_{20} + \mu_{02} + \sqrt{(\mu_{20} + \mu_{02})^{2} + 4\mu_{11}^{2}})}{\mu_{00}}$$

$$b^{2} = \frac{2(\mu_{20} + \mu_{02} - \sqrt{(\mu_{20} + \mu_{02})^{2} + 4\mu_{11}^{2}})}{\mu_{00}}$$

## Histogram (texture) features

- First order statistics (information related to the gray level distribution)
- Second order statistics (information related to spatial/relative distribution of gray level), i.e. second order histogram, co-occurrence matrix

#### Histogram:

$$P(I) = \frac{Number\ of\ pixels\ with\ gray\ level\ I}{Total\ number\ of\ pixels\ in\ the\ region}$$

#### Moments from gray level histogram:

$$m_p = E\{I^p\} = \sum_{I=0}^{L-1} I^p P(I), \quad p = 1, 2, \dots$$
  $H = -E\{\ln P(I)\} = -\sum_{I=0}^{L-1} P(I) \ln P(I)$ 

$$m_1 = E(I) = Mean \ value \ of \ I$$

#### Entropy:

$$H = -E\{\ln P(I)\} = -\sum_{I=0}^{L-1} P(I) \ln P(I)$$

## Histogram (texture) features

#### Central moments:

$$\mu_p = E\{(I - E(I))^p\} = \sum_{I=0}^{L-1} (I - m_1)^p P(I), \quad p = 1, 2, \dots$$

#### Features:

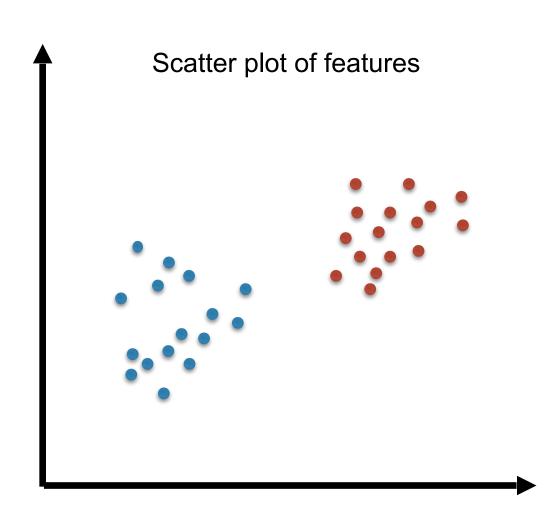
$$\mu_2 = \sigma^2 = variance$$

$$\mu_3 = skewness$$

$$\mu_4 = kurtosis$$

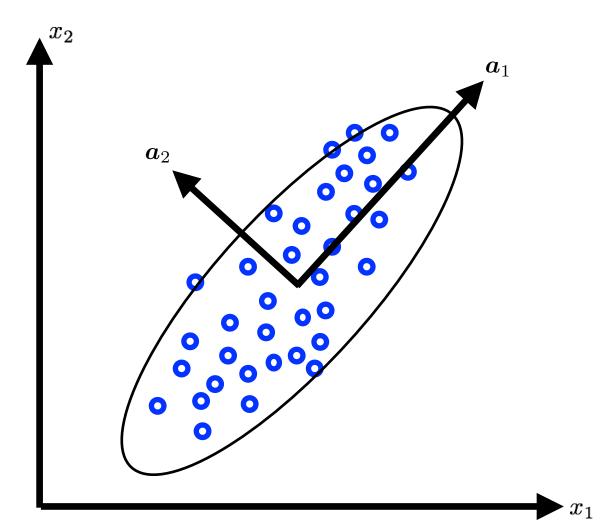
#### **Feature selection**

- A number of feature candidates may have been generated.
- Using all candidates will easily lead to over traing (unreliable classification of new data).
- Dimensionality reduction is required, i.e. feature selection!
- Exhaustive search impossible!
- Trial and error (select feature combination, train classifier, estimate error rate).
- Suboptimal search.
- «Branch and Bound» search.
- Linear or non-linear mappings to lower dimensional feature space.

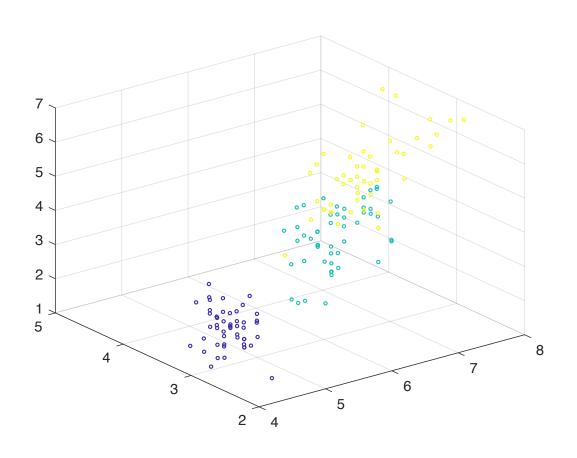


## **Dimensionality reduction - linear transformations**

- PCA, ICA, LLE, Isomap
- PCA (Principal Components Analysis) is one of the most important techniques for dimensionality reduction
- It takes advantage of correlations between the features to produce the best possible lower dimensional representation of the data with respect to reconstruction error
- The eigenvectors of the lumped covariance matrix defines the new features in the transformed feature space.



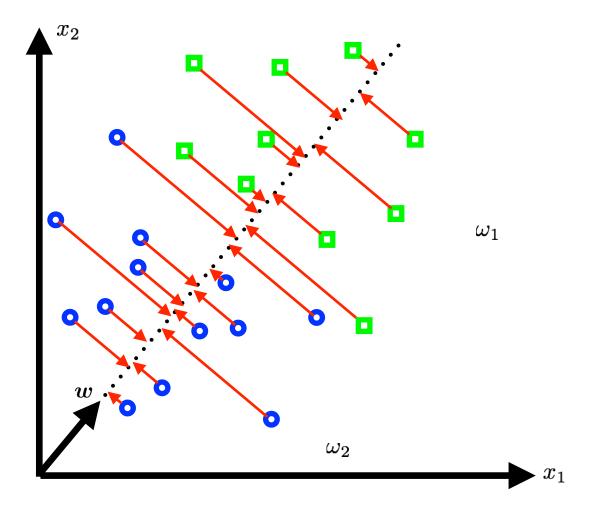
## **Principle Components Analysis - example**



6.5 Second principal component 5.5 4.5 3.5 2 3 9 10 First principal component

Fisher's Iris dataset (features 1, 2 and 3)

### **Dimensionality reduction – linear transformations**



- Projection of multidimensional feature vectors to a lower-dimensional feature space.
- Example: Fishers linear discriminant provides a projection from a d-dimensional space (d>1) to a one-dimensional space in such a way that the separation between classes are maximized.

## **Summary**

#### Image feature extraction:

- Feature extraction
- Feature selection

More information: Szeliski 14.4

