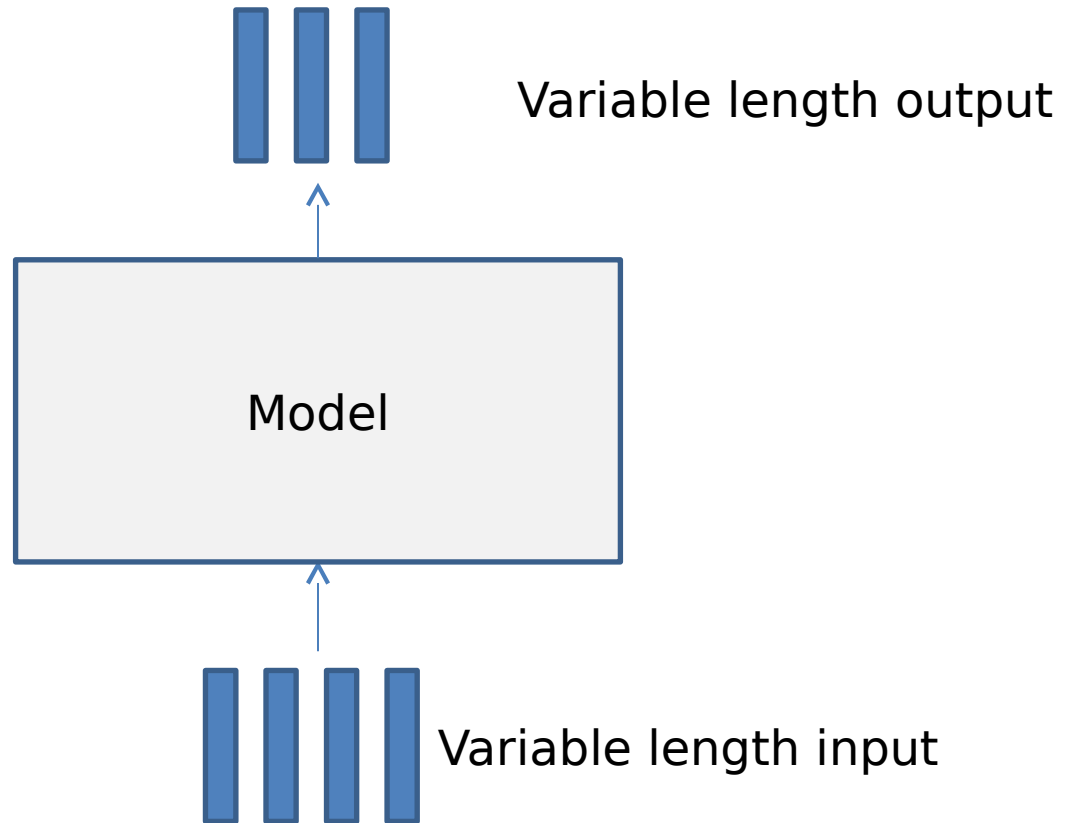


Sequence(s)-to-Sequence Transformations in Text Processing

Narada Warakagoda

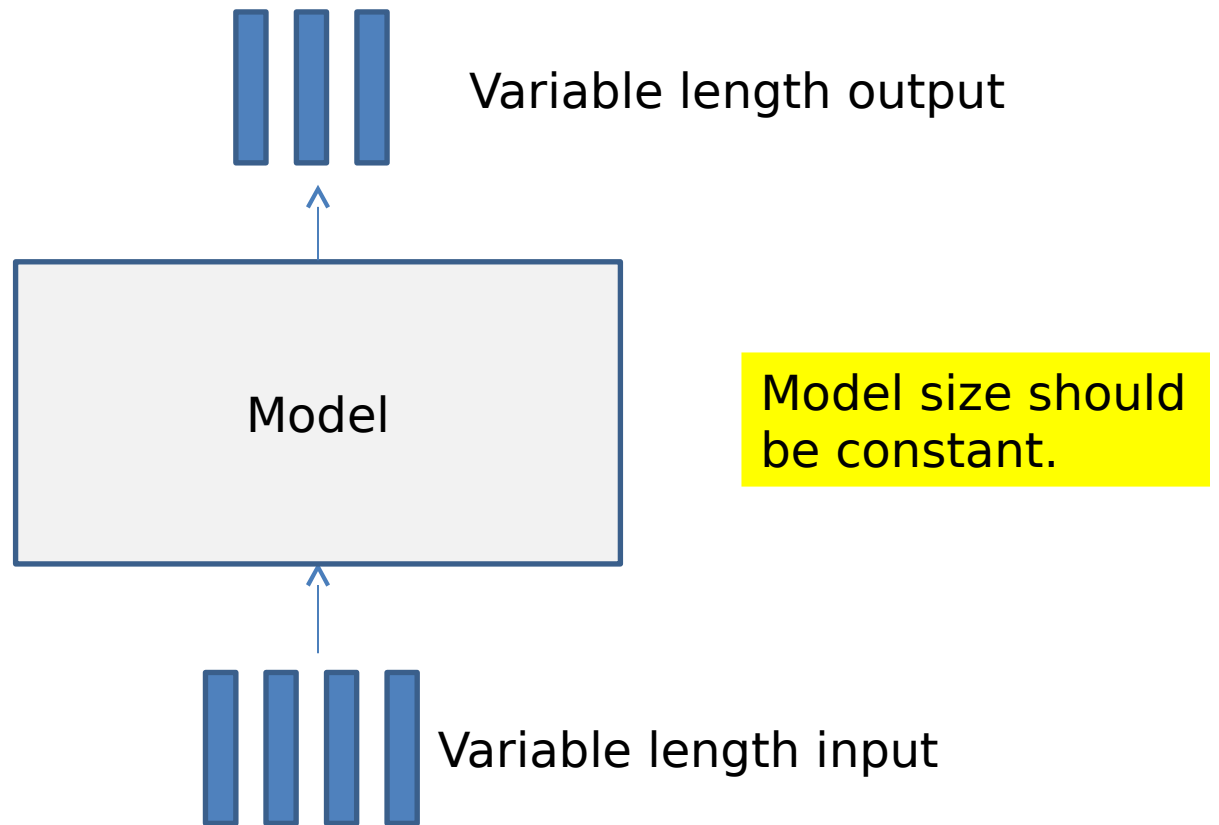
Seq2seq Transformation



Example Applications

- Summarization
(extractive/abstractive)
- Machine translation
- Dialog systems /chatbots
- Text generation
- Question answering ★
-
-

Seq2seq Transformation

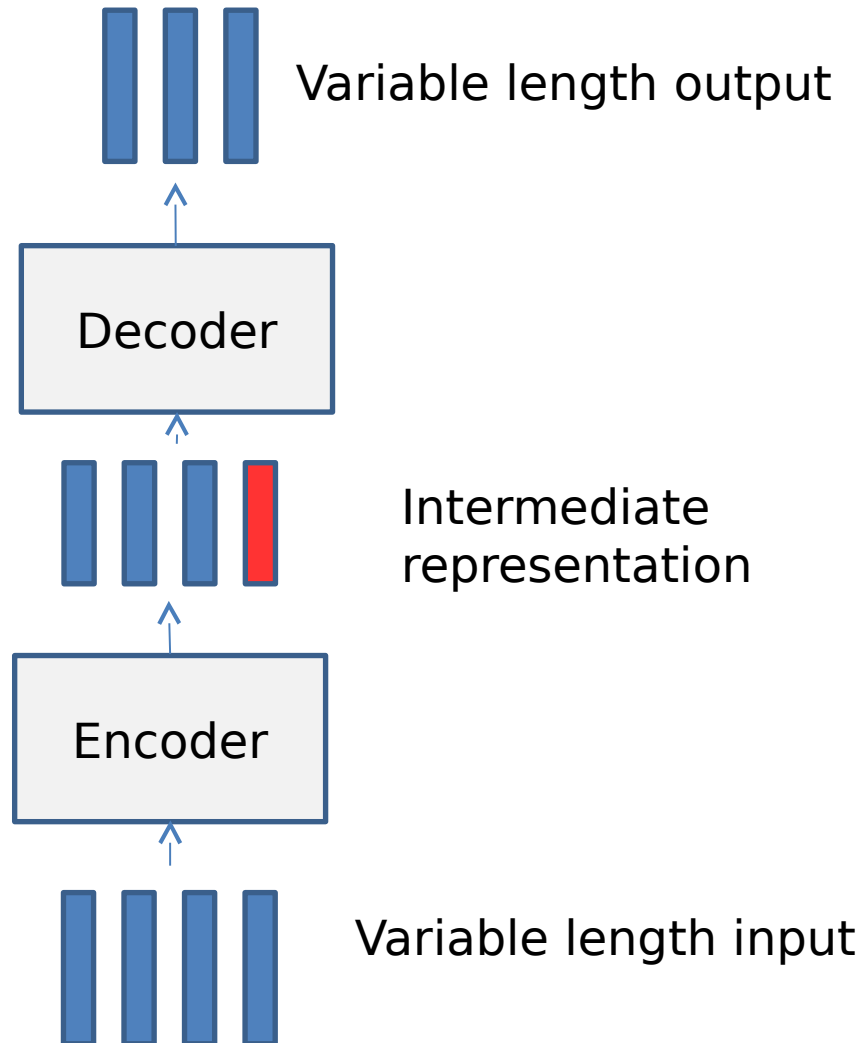


Solution: Apply a constant sized neural net module repeatedly on the data

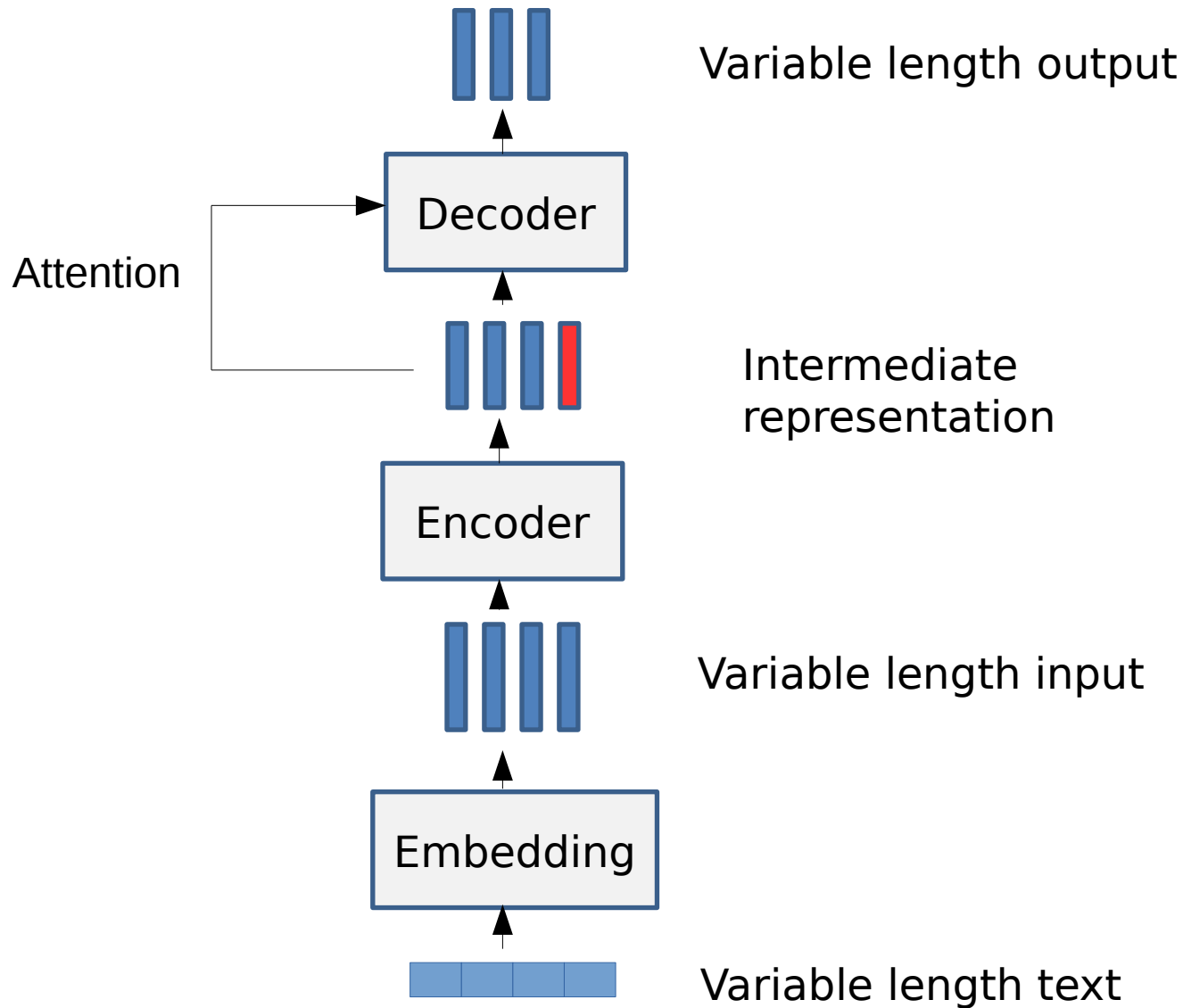
Possible Approaches

- Recurrent networks
 - Apply the NN module in a serial fashion
- Convolutions networks
 - Apply the NN modules in a hierarchical fashion
- Self-attention
 - Apply the NN module in a parallel fashion

Processing Pipeline




Processing Pipeline



Architecture Variants

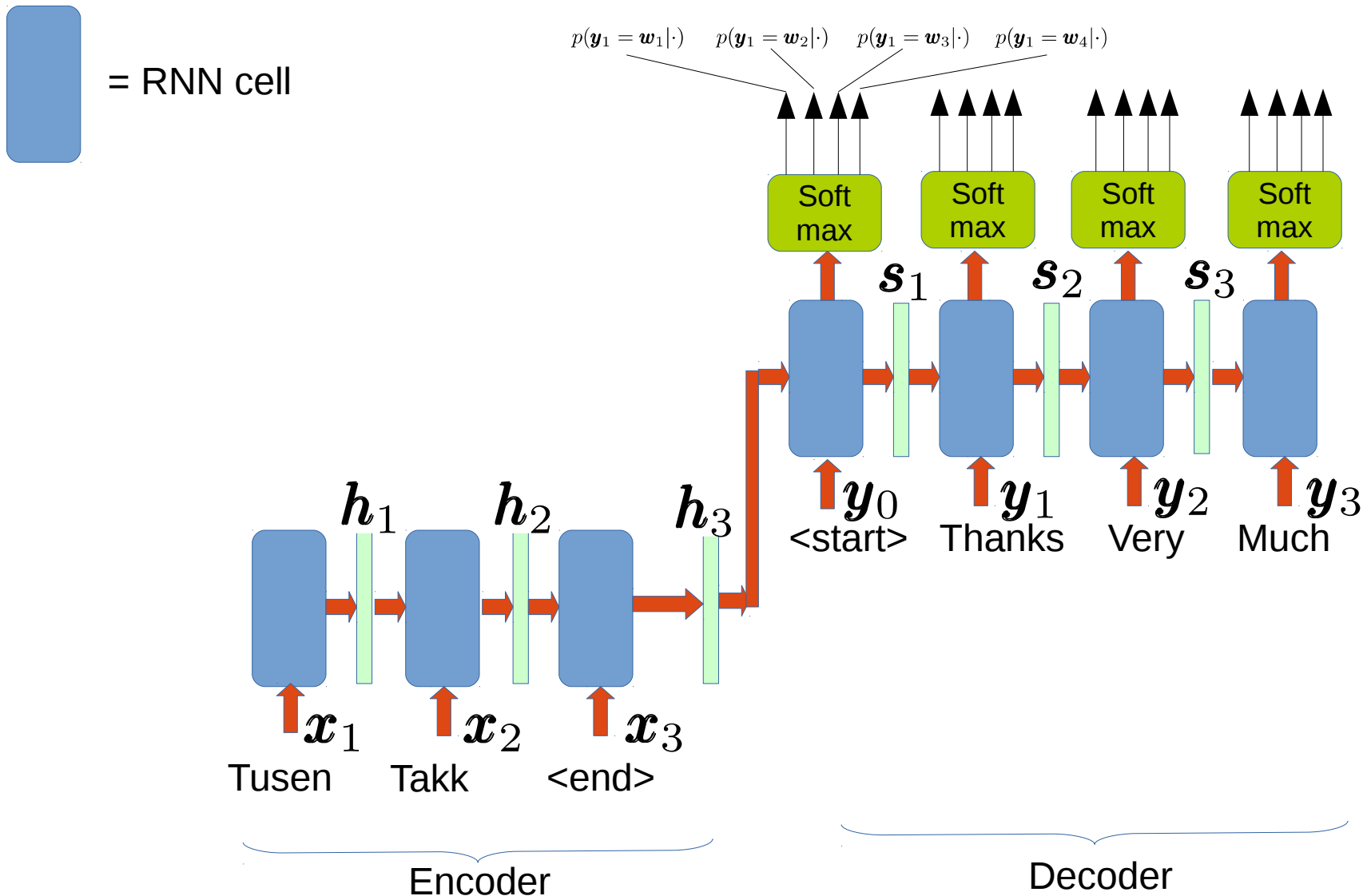
Encoder	Decoder	Attention
Recurrent net	Recurrent net	No
Recurrent net	Recurrent net	Yes
Convolutional net	Convolutional net	No
Convolutional net	Recurrent net	Yes
Convolutional net	Convolutional net	Yes
Fully connected net with self-attention	Fully connected net with self-attention	Yes

Possible Approaches

- Recurrent networks 
 - Apply the NN module in a serial fashion
- Convolutions networks
 - Apply the NN modules in a hierarchical fashion
- Self-attention
 - Apply the NN module in a parallel fashion

RNN-decoder with RNN-encoder

Decoder vocabulary = {Much (w_1), Thanks (w_2), Very (w_3), < end > (w_4)}

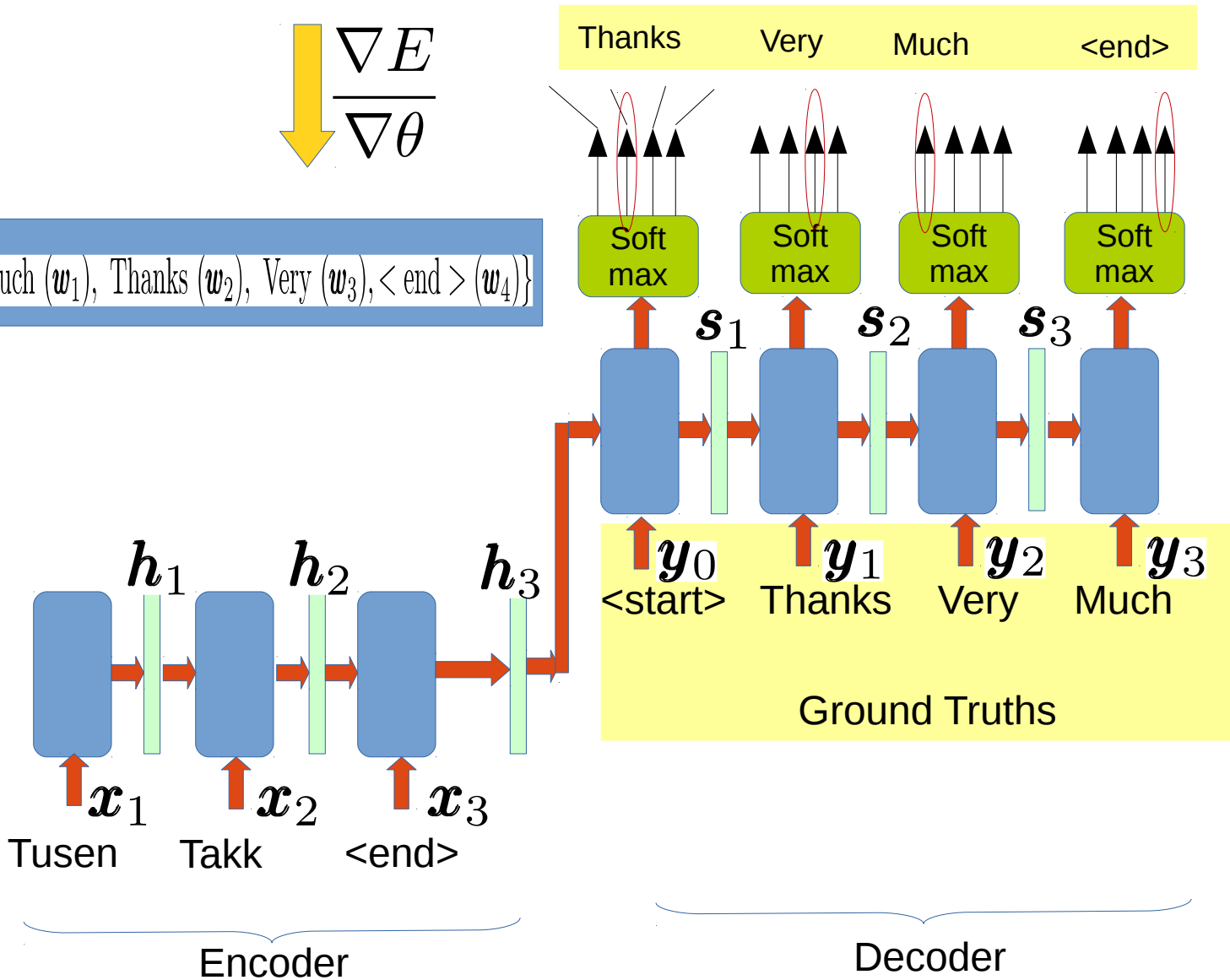


RNN-dec with RNN-enc, Training

$$E = \log L = \log [p(\mathbf{y}_1 = w_2 | \mathbf{X}) \cdot p(\mathbf{y}_2 = w_3 | w_2, \mathbf{X}) \cdot p(\mathbf{y}_3 = w_1 | w_2, w_3, \mathbf{X}) \cdot p(\mathbf{y}_4 = w_4 | w_2, w_3, w_1, \mathbf{X})]$$

$$\frac{\nabla E}{\nabla \theta}$$

Decoder vocabulary = {Much (w_1), Thanks (w_2), Very (w_3), <end> (w_4)}

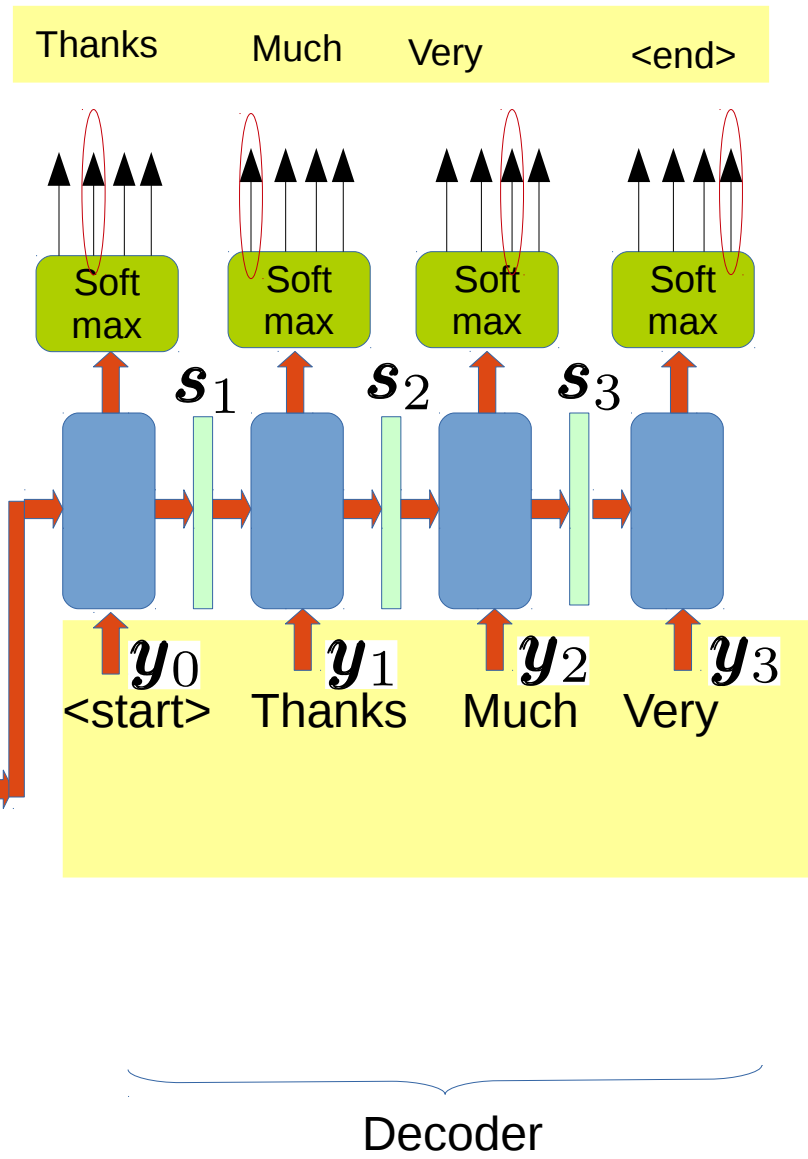
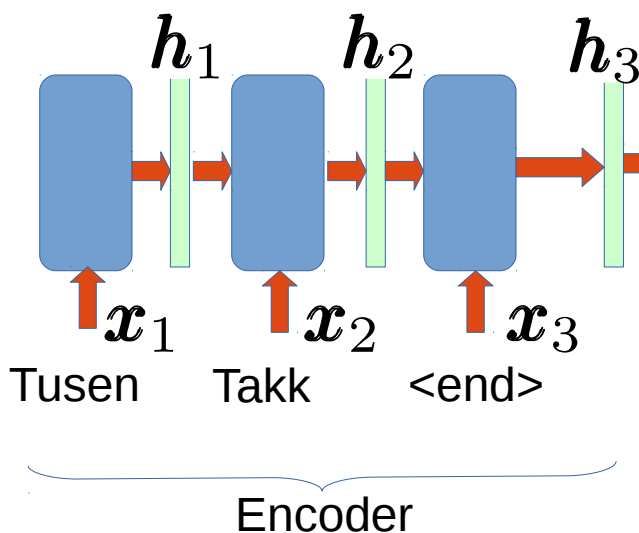


RNN-dec with RNN-enc, Decoding

Decoder vocabulary = {Much (w_1), Thanks (w_2), Very (w_3), <end> (w_4)}

Greedy Decoding

$$y_1 = \operatorname{argmax}_{w \in \{w_1, w_2, w_3, w_4\}} p(y_1 = w | \mathbf{X})$$



Decoding Approaches

- Optimal decoding

Find $\mathbf{w} = \{w_1, w_2, w_3, w_4\}$ such that $p(w_1, w_2, w_3, w_4 | \mathbf{X})$ is maximum

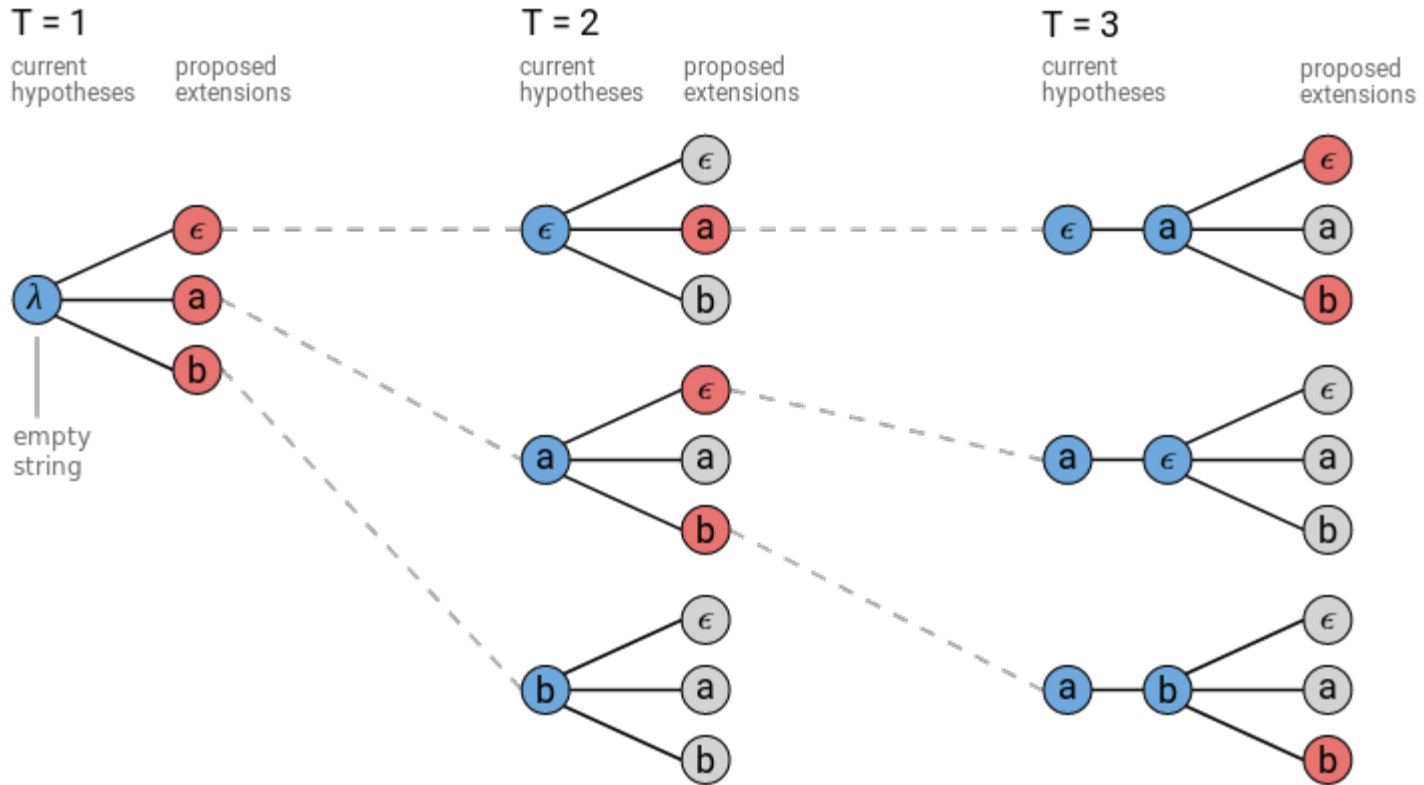
- Greedy decoding

- Easy
- Not optimal

- Beam search

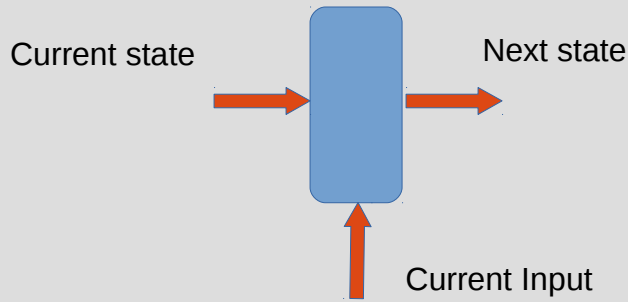
- Closer to optimal decoder
- Choose top N candidates instead of the best one at each step.

Beam Search Decoding

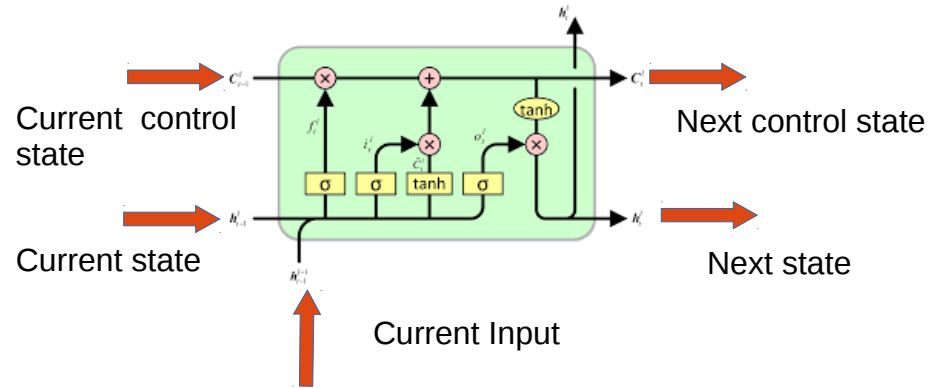


Beam Width = 3

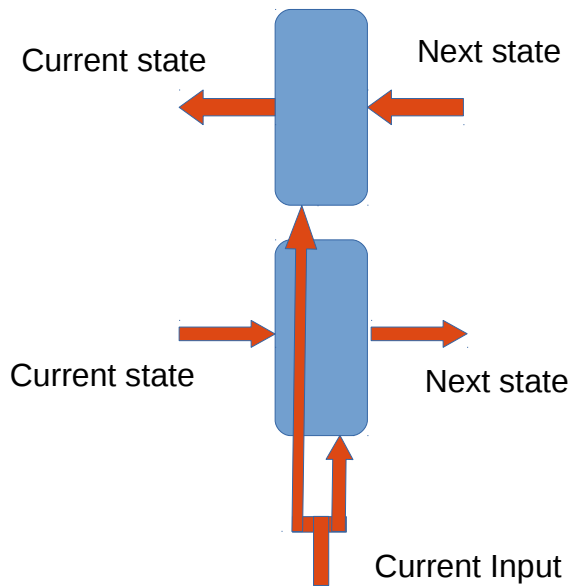
Straight-forward Extensions



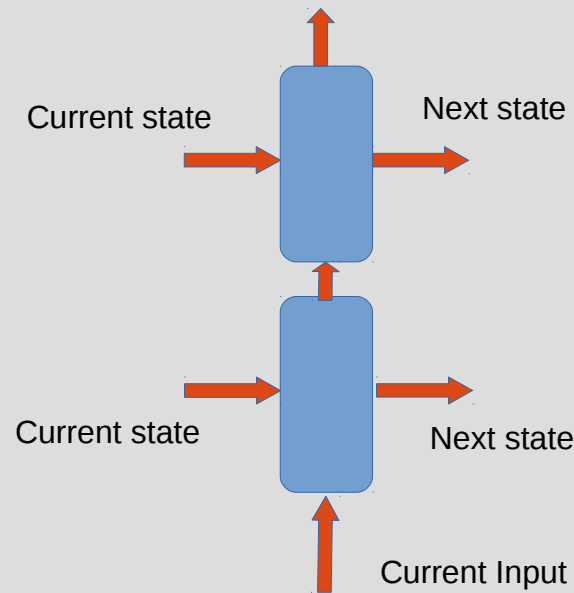
RNN Cell



LSTM Cell



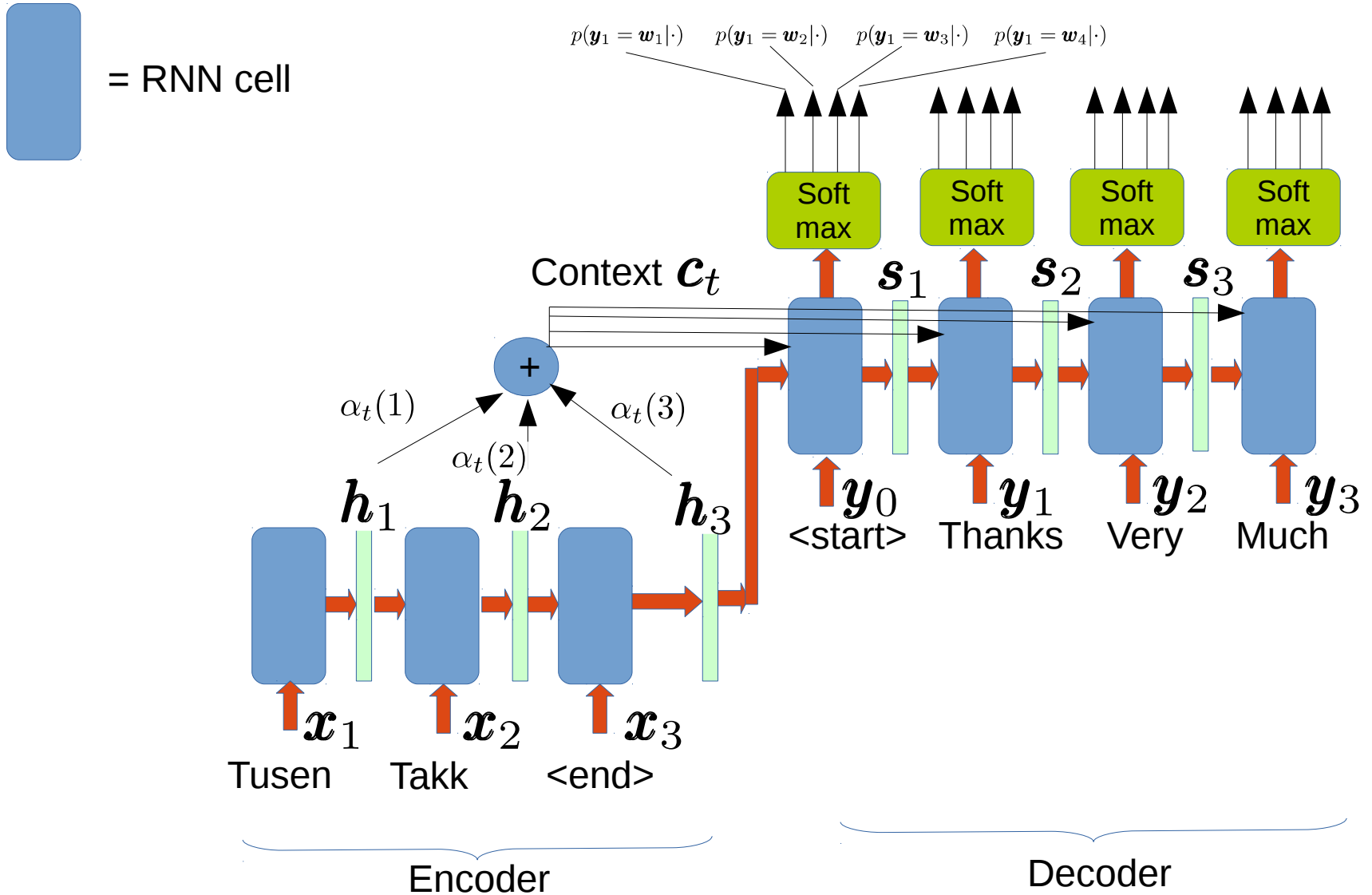
Bidirectional Cell



Stacked Cell

RNN-decoder with RNN-encoder with Attention

Decoder vocabulary = {Much (w_1), Thanks (w_2), Very (w_3), < end > (w_4)}



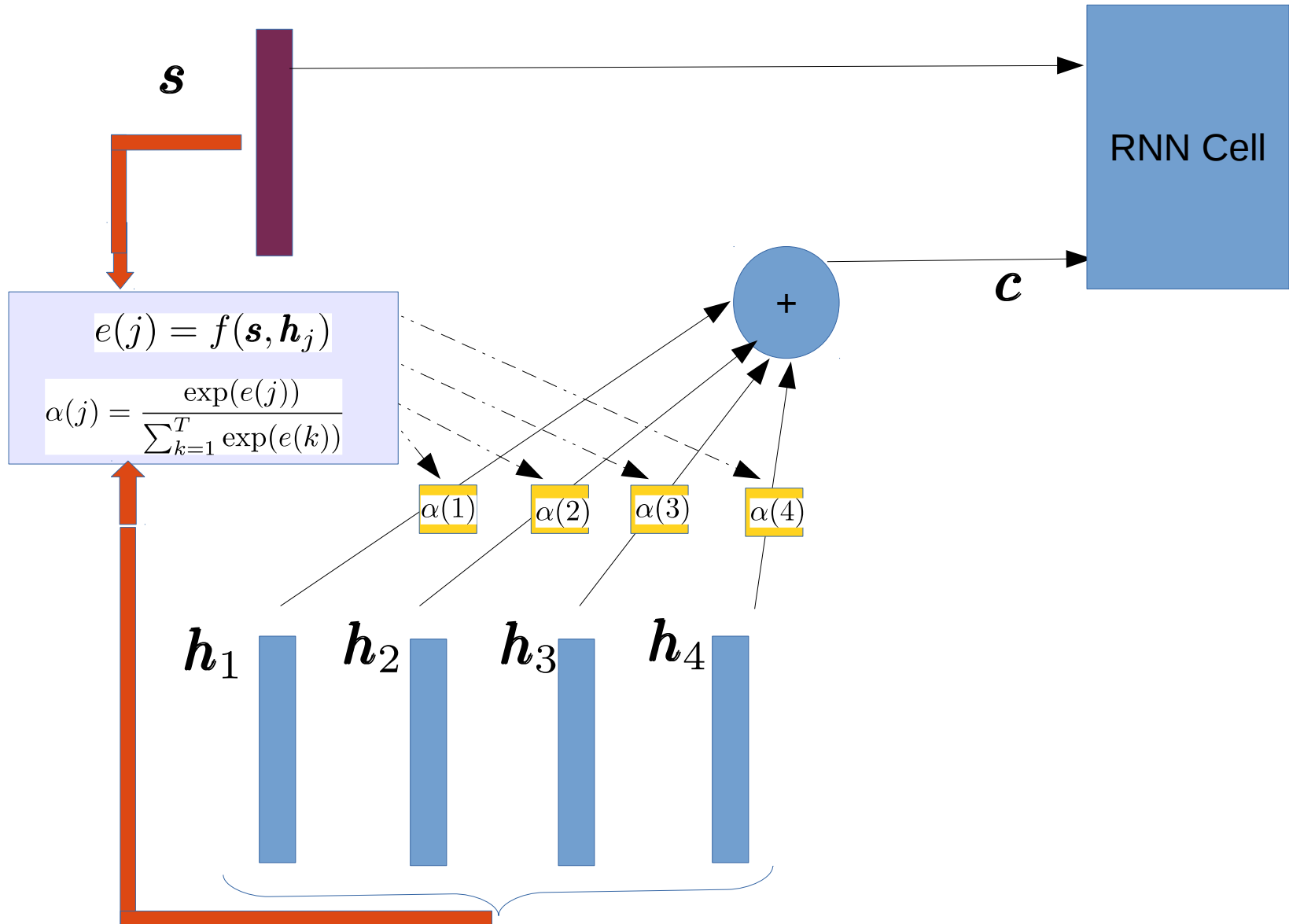
Attention

- Context is given by $c_t = \sum_{j=1}^{T_x} \alpha_t(j) \mathbf{h}_j$
- Attention weights $\alpha_t(j)$ are dynamic
- Generally defined by $\alpha_t(j) = \frac{\exp(e_t(j))}{\sum_{k=1}^{T_x} \exp(e_t(k))}$ with $e_t(j) = f(\mathbf{s}_{t-1}, \mathbf{h}_j)$

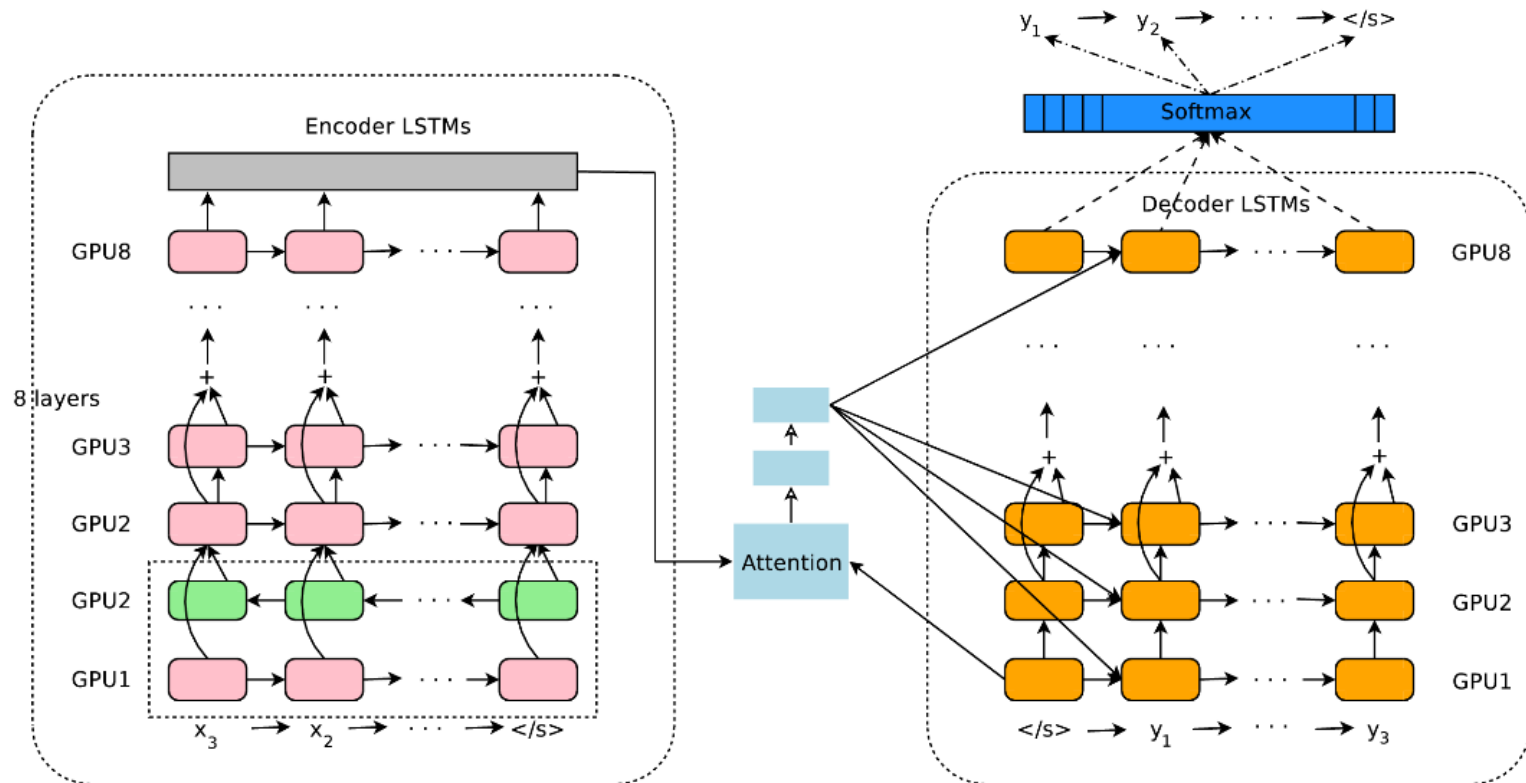
where function f can be defined in several ways.

- Dot product $e_t(j) = \mathbf{s}_{t-1}^T \cdot \mathbf{h}_j$
- Weighted dot product $e_t(j) = \mathbf{s}_{t-1}^T \cdot \mathbf{W} \cdot \mathbf{h}_j$
- Use another MLP (eg: 2 layer) $e_t(j) = \mathbf{v}^T \cdot \tanh(\mathbf{W} \cdot [\mathbf{h}_j; \mathbf{s}_{t-1}])$


Attention



Example: Google Neural Machine Translation



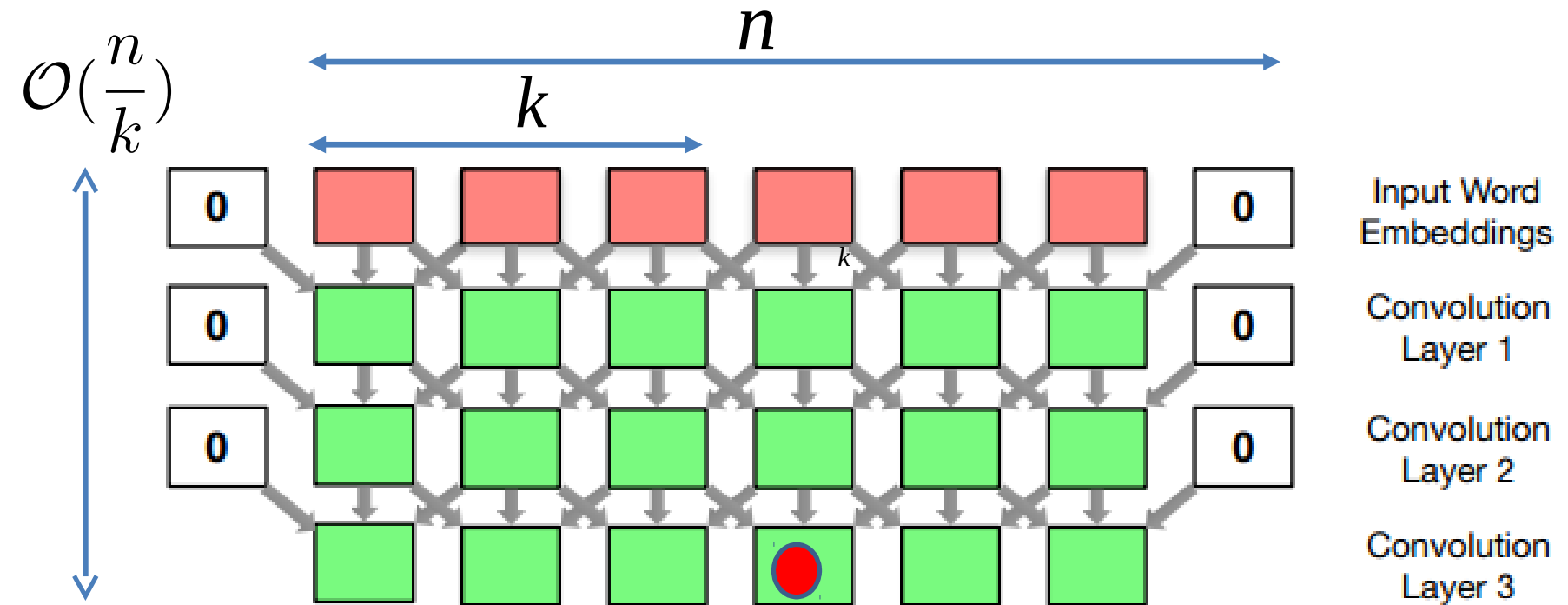
Possible Approaches

- Recurrent networks
 - Apply the NN module in a serial fashion
- Convolutions networks 
 - Apply the NN modules in a hierarchical fashion
- Self-attention
 - Apply the NN module in a parallel fashion

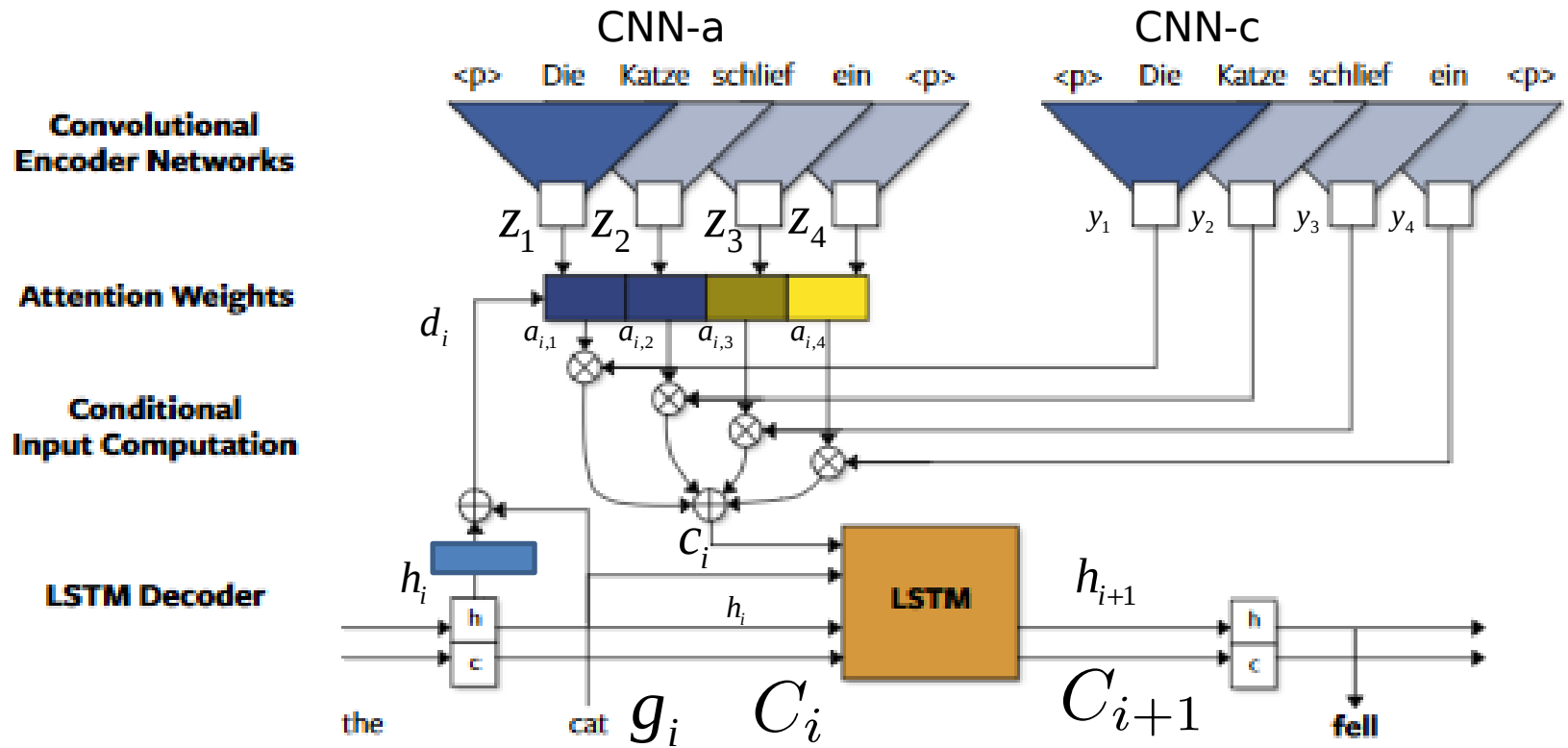
Why Convolution

- Recurrent networks are serial
 - Unable to be parallelized
 - “Distance” between feature vector and different inputs are not constant
- Convolutions networks
 - Can be parallelized (faster)
 - “Distance” between feature vector and different inputs are constant

Long range dependency capture with conv nets



Conv net, Recurrent net with Attention



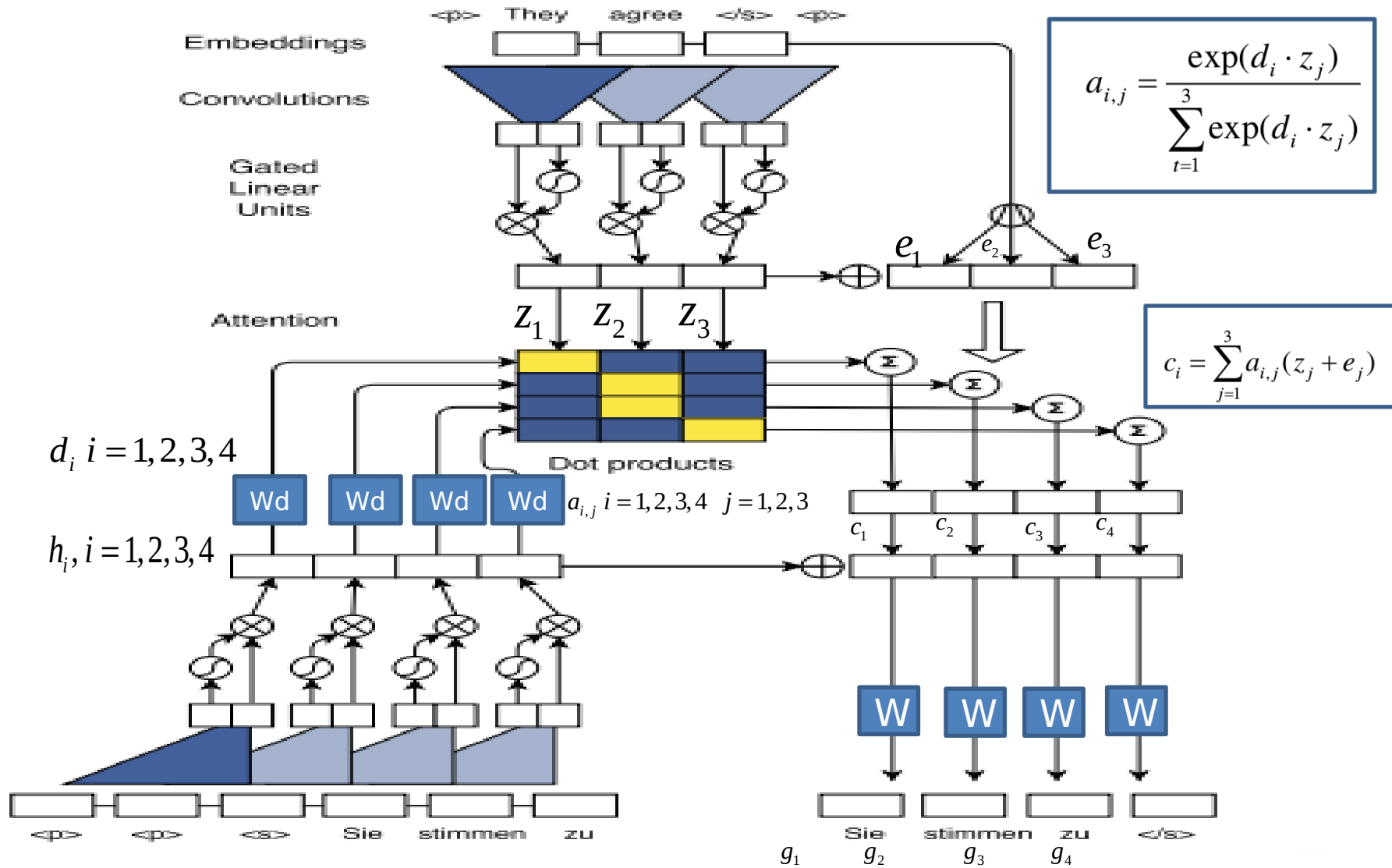
$$d_i = W_d h_i + g_i$$

$$a_{i,j} = \frac{\exp(d_i \cdot z_j)}{\sum_{t=1}^4 \exp(d_i \cdot z_t)}$$

$$c_i = \sum_{j=1}^4 a_{i,j} y_j$$


$$h_{i+1}, C_{i+1} = \text{LSTM}(c_i, h_i, g_i, C_i)$$

Two conv nets with attention

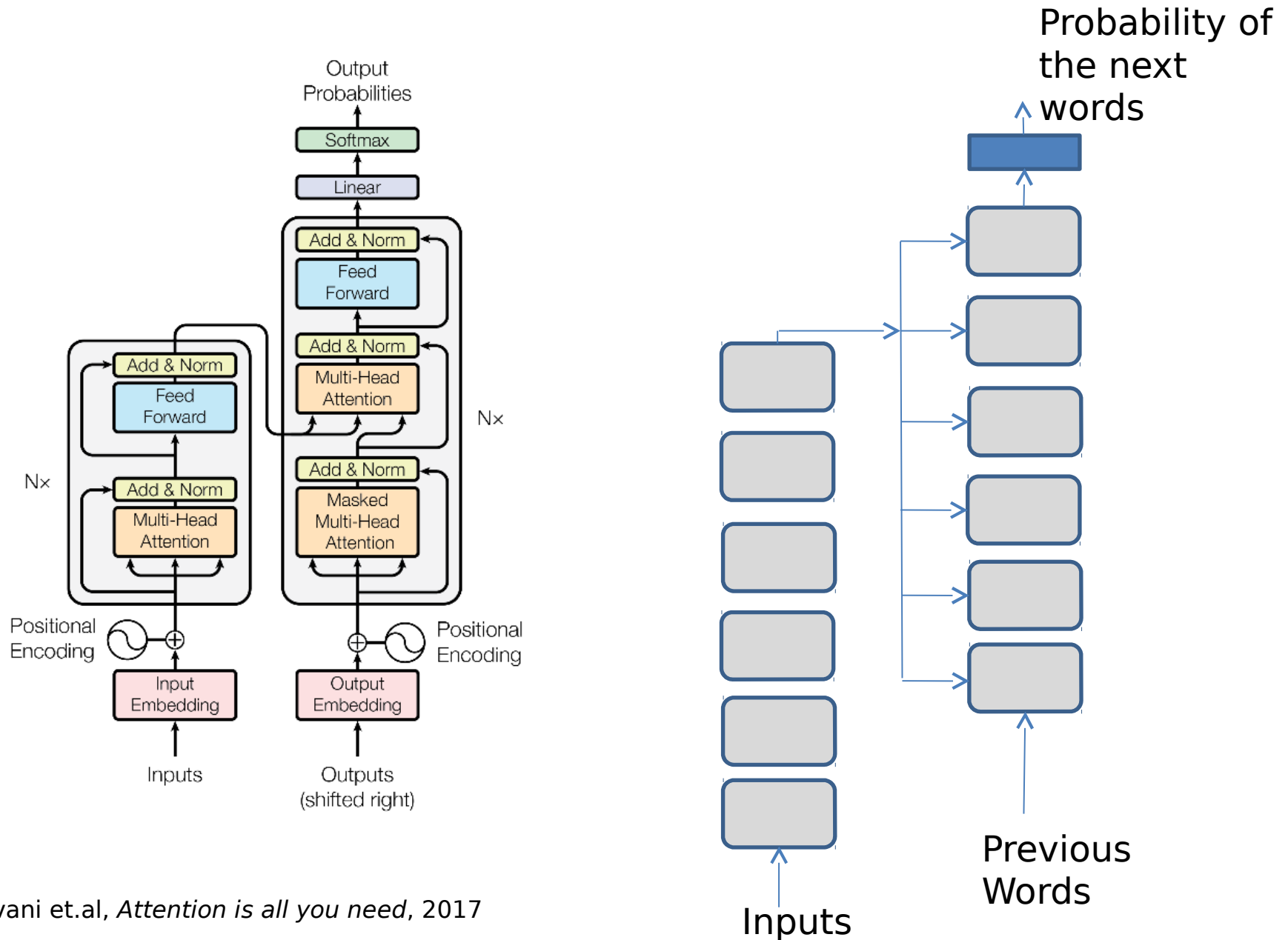


$$P(g_i | g_{i-1}, g_{i-2}, \dots) = \text{softmax}(W(c_{i-1} + h_{i-1}))$$

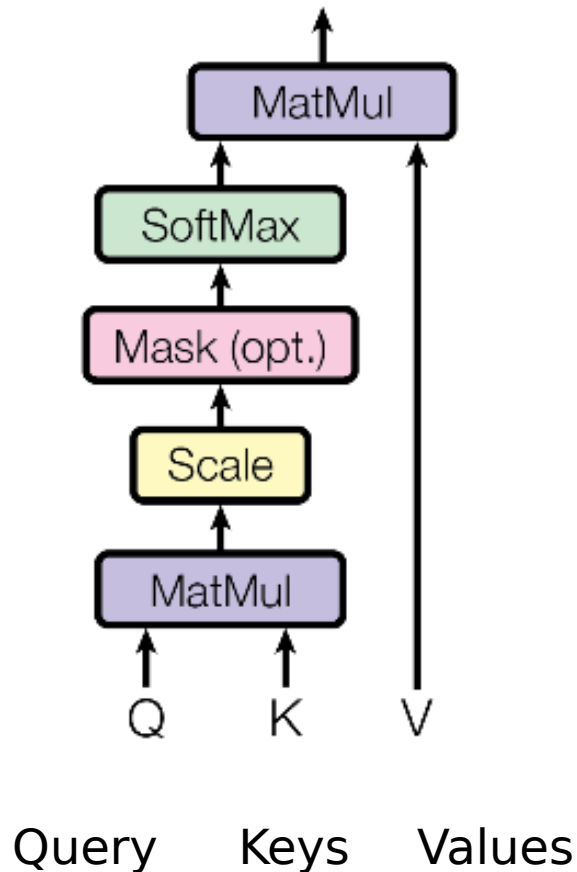
Possible Approaches

- Recurrent networks
 - Apply the NN module in a serial fashion
- Convolutions networks
 - Apply the NN modules in a hierarchical fashion
- Self-attention 
 - Apply the NN module in a parallel fashion

FCN with self-attention

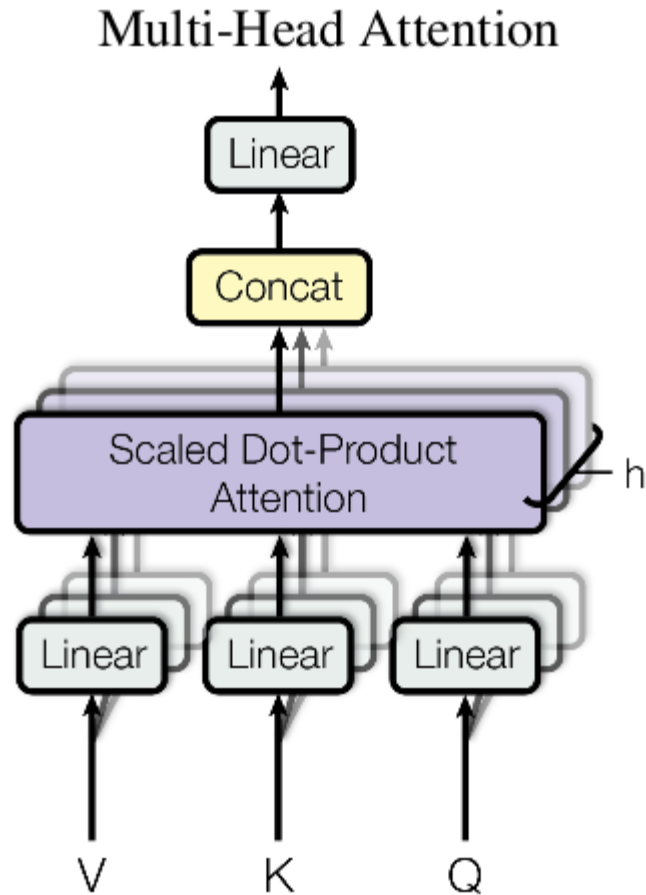


Scaled dot product attention

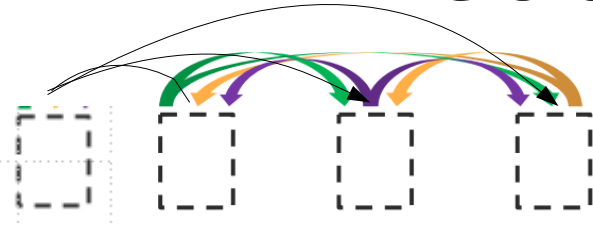


$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)V$$

Multi-Head Attention



Encoder Self-attention



Encoder Self-Attention

$$[h_1 \quad h_2 \quad h_3 \quad h_4]$$

N=4, d-dimensional vectors

$$\begin{bmatrix} \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_1) & \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_2) & \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_3) & \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_4) \\ \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_1) & \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_2) & \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_3) & \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_4) \\ \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_1) & \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_2) & \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_3) & \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_4) \\ \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_1) & \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_2) & \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_3) & \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_4) \end{bmatrix}$$

$$\begin{aligned} S_1 &= \sum_j \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_j) \\ S_2 &= \sum_j \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_j) \\ S_3 &= \sum_j \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_j) \\ S_4 &= \sum_j \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_j) \end{aligned}$$

$$\begin{aligned} a_{1,1} &= \frac{1}{S_1} \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_1) & a_{1,2} &= \frac{1}{S_1} \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_2) & a_{1,3} &= \frac{1}{S_1} \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_3) & a_{1,4} &= \frac{1}{S_1} \exp(\frac{1}{\sqrt{d}} h_1 \cdot h_4) \\ a_{2,1} &= \frac{1}{S_2} \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_1) & a_{2,2} &= \frac{1}{S_2} \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_2) & a_{2,3} &= \frac{1}{S_2} \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_3) & a_{2,4} &= \frac{1}{S_2} \exp(\frac{1}{\sqrt{d}} h_2 \cdot h_4) \\ a_{3,1} &= \frac{1}{S_3} \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_1) & a_{3,2} &= \frac{1}{S_3} \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_2) & a_{3,3} &= \frac{1}{S_3} \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_3) & a_{3,4} &= \frac{1}{S_3} \exp(\frac{1}{\sqrt{d}} h_3 \cdot h_4) \\ a_{4,1} &= \frac{1}{S_4} \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_1) & a_{4,2} &= \frac{1}{S_4} \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_2) & a_{4,3} &= \frac{1}{S_4} \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_3) & a_{4,4} &= \frac{1}{S_4} \exp(\frac{1}{\sqrt{d}} h_4 \cdot h_4) \end{aligned}$$

$$\begin{bmatrix} \sum_{j=1}^4 a_{1,j} h_j \\ \sum_{j=1}^4 a_{2,j} h_j \\ \sum_{j=1}^4 a_{3,j} h_j \\ \sum_{j=1}^4 a_{4,j} h_j \end{bmatrix}$$

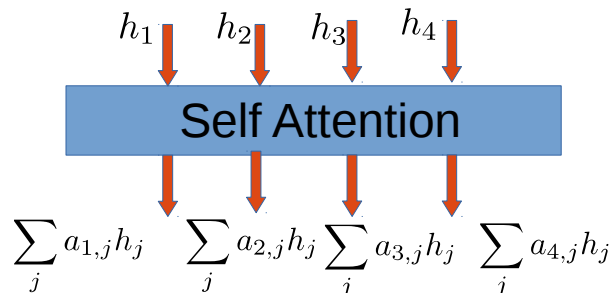
h_1

h_2

h_3

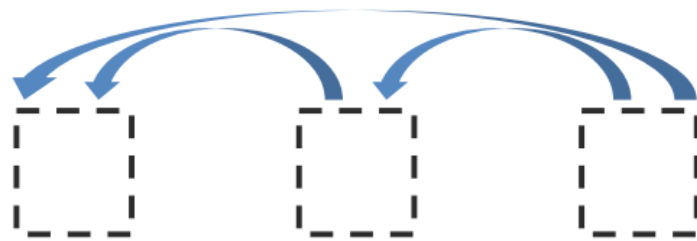
h_4

N=4, d-dimensional vectors



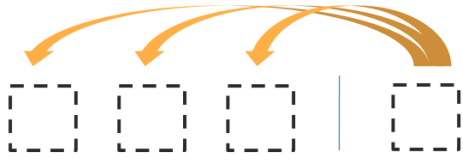
Decoder Self-attention

- Almost same as encoder self attention
- But only leftward positions are considered.



MaskedDecoder Self-Attention

Encoder-decoder attention



Encoder-Decoder Attention

Encoder states

$$[h_1 \quad h_2 \quad h_3]$$

Decoder states

$$[z_1 \quad z_2 \quad z_3 \quad z_4]$$

$$\begin{bmatrix} \exp\left(\frac{1}{\sqrt{d}} z_1 \cdot h_1\right) & \exp\left(\frac{1}{\sqrt{d}} z_1 \cdot h_2\right) & \exp\left(\frac{1}{\sqrt{d}} z_1 \cdot h_3\right) \\ \exp\left(\frac{1}{\sqrt{d}} z_2 \cdot h_1\right) & \exp\left(\frac{1}{\sqrt{d}} z_2 \cdot h_2\right) & \exp\left(\frac{1}{\sqrt{d}} z_2 \cdot h_3\right) \\ \exp\left(\frac{1}{\sqrt{d}} z_3 \cdot h_1\right) & \exp\left(\frac{1}{\sqrt{d}} z_3 \cdot h_2\right) & \exp\left(\frac{1}{\sqrt{d}} z_3 \cdot h_3\right) \\ \exp\left(\frac{1}{\sqrt{d}} z_4 \cdot h_1\right) & \exp\left(\frac{1}{\sqrt{d}} z_4 \cdot h_2\right) & \exp\left(\frac{1}{\sqrt{d}} z_4 \cdot h_3\right) \end{bmatrix}$$

$$\begin{aligned} S_1 &= \sum_j \exp\left(\frac{1}{\sqrt{d}} z_1 \cdot h_j\right) \\ S_2 &= \sum_j \exp\left(\frac{1}{\sqrt{d}} z_2 \cdot h_j\right) \\ S_3 &= \sum_j \exp\left(\frac{1}{\sqrt{d}} z_3 \cdot h_j\right) \\ S_4 &= \sum_j \exp\left(\frac{1}{\sqrt{d}} z_4 \cdot h_j\right) \end{aligned}$$

$$\begin{bmatrix} a_{1,1} = \frac{1}{S_1} \exp\left(\frac{1}{\sqrt{d}} z_1 \cdot h_1\right) & a_{1,2} = \frac{1}{S_1} \exp\left(\frac{1}{\sqrt{d}} z_1 \cdot h_2\right) & a_{1,3} = \frac{1}{S_1} \exp\left(\frac{1}{\sqrt{d}} z_1 \cdot h_3\right) \\ a_{2,1} = \frac{1}{S_2} \exp\left(\frac{1}{\sqrt{d}} z_2 \cdot h_1\right) & a_{2,2} = \frac{1}{S_2} \exp\left(\frac{1}{\sqrt{d}} z_2 \cdot h_2\right) & a_{2,3} = \frac{1}{S_2} \exp\left(\frac{1}{\sqrt{d}} z_2 \cdot h_3\right) \\ a_{3,1} = \frac{1}{S_3} \exp\left(\frac{1}{\sqrt{d}} z_3 \cdot h_1\right) & a_{3,2} = \frac{1}{S_3} \exp\left(\frac{1}{\sqrt{d}} z_3 \cdot h_2\right) & a_{3,3} = \frac{1}{S_3} \exp\left(\frac{1}{\sqrt{d}} z_3 \cdot h_3\right) \\ a_{4,1} = \frac{1}{S_4} \exp\left(\frac{1}{\sqrt{d}} z_4 \cdot h_1\right) & a_{4,2} = \frac{1}{S_4} \exp\left(\frac{1}{\sqrt{d}} z_4 \cdot h_2\right) & a_{4,3} = \frac{1}{S_4} \exp\left(\frac{1}{\sqrt{d}} z_4 \cdot h_3\right) \end{bmatrix}$$

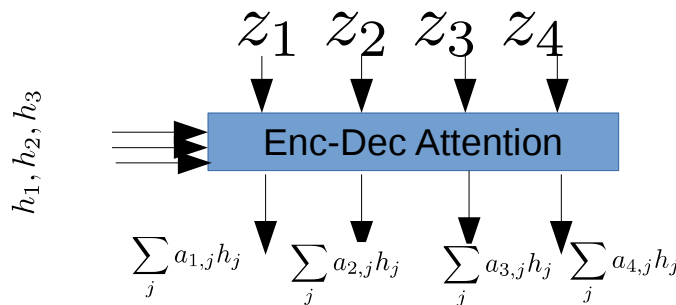
h_1

h_2

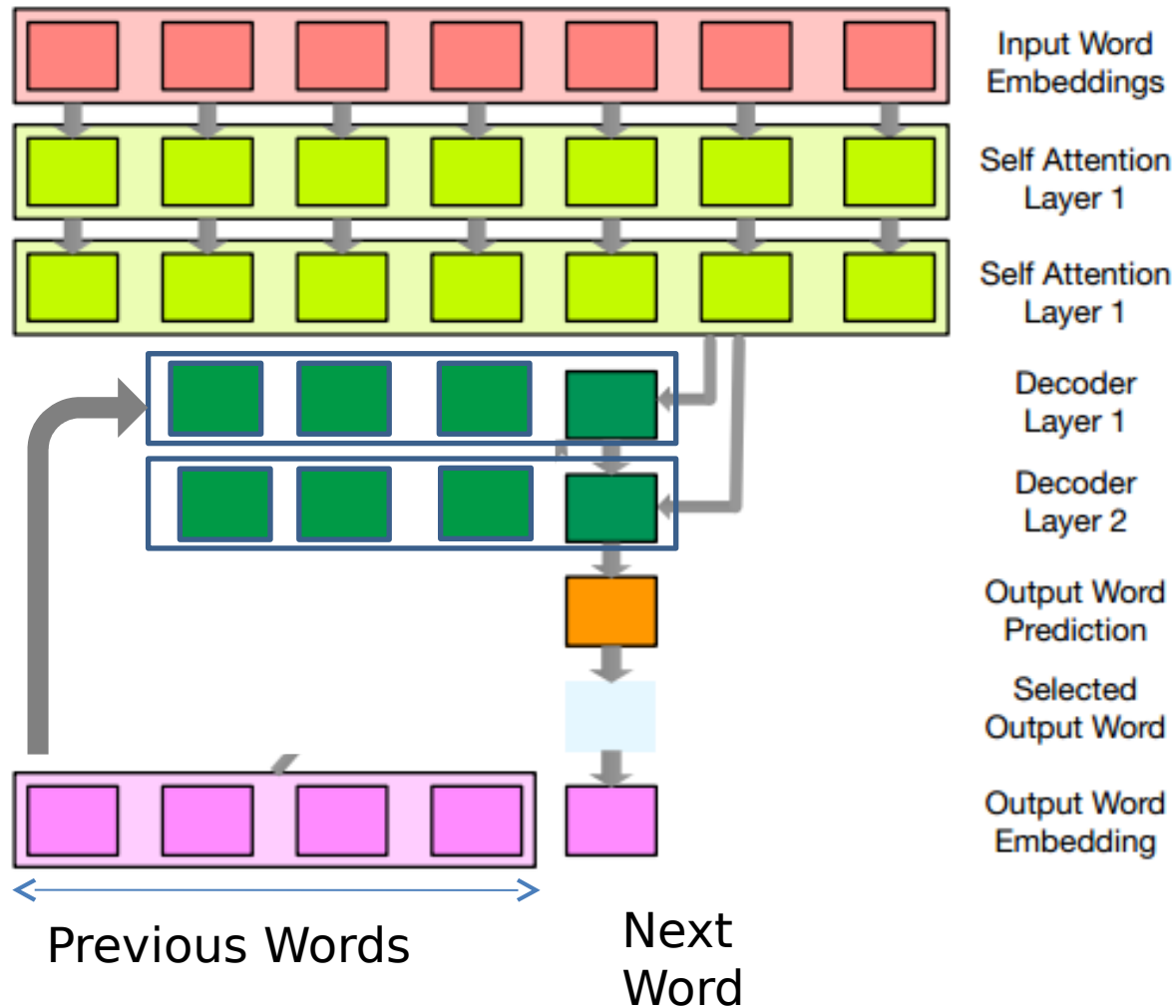
h_3

$$\begin{bmatrix} \sum_{j=1}^3 a_{1,j} h_j \\ \sum_{j=1}^3 a_{2,j} h_j \\ \sum_{j=1}^3 a_{3,j} h_j \\ \sum_{j=1}^3 a_{4,j} h_j \end{bmatrix}$$

N=4, d-dimensional vectors



Overall Operation

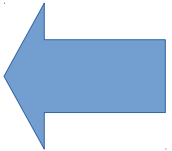


Reinforcement Learning

- Machine Translation/Summarization
- Dialog Systems
-
-

Reinforcement Learning

- Machine Translation/Summarization
- Dialog Systems
-
-



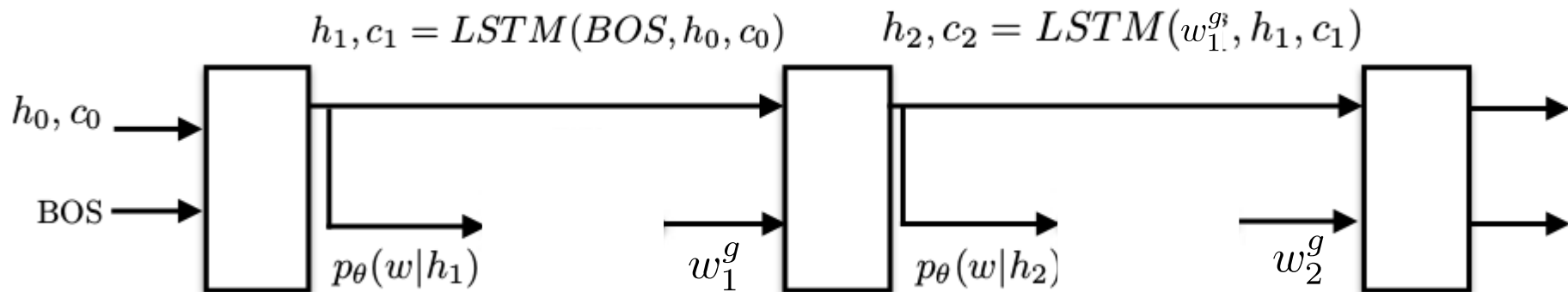
Why Reinforcement Learning

- Exposure bias
 - In training ground truths are used. In testing, generated word in the previous step is used to generate the next word.
 - Use generated words in training needs sampling : **Non differentiable**
- Maximum Likelihood criterion is not directly relevant to evaluation metrics
 - BLEU (Machine translation)
 - ROUGE (Summarization)
 - Use BLEU/ROUGE in training: **Non differentiable**

Sequence Generation as Reinforcement Learning

- **Agent:** The Recurrent Net
- **State:** Hidden layers, Attention weights etc.
- **Action:** Next Word
- **Policy:** Generate the next word (*action*) given the current hidden layers and attention weights (*state*)
- **Reward:** Score computed using the evaluation metric (eg: BLEU)

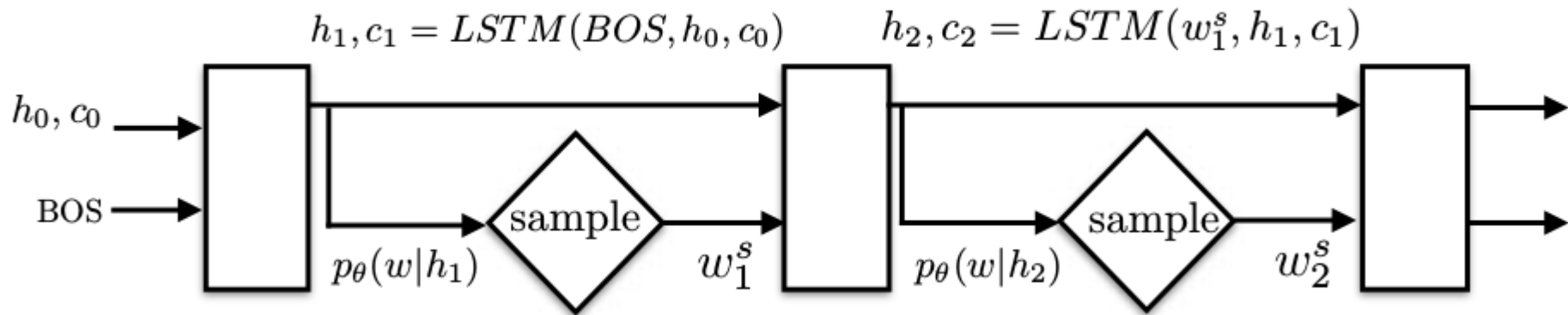
Maximum Likelihood Training (Revisit)



$$\text{Log Likelihood} = \sum_{t=1}^T \log p_\theta(w_t^g | h_t)$$

Minimize the negative log likelihood

Reinforcement Learning Formulation



$$\text{Reward} = r(w^s) = r(w_1^s, w_2^s, \dots, w_T^s)$$

Minimize the expected negative reward, $L(\theta) = -\mathbb{E}_{w^s \sim p_\theta} [r(w^s)]$
using REINFORCE algorithm

Reinforcement Learning Details

- Expected reward $L(\theta) = - \sum_w p_\theta(w) r(w)$
- We need the gradient $\nabla_\theta L(\theta) = - \sum_w r(w) \nabla_\theta p_\theta(w)$
- Need to write this as an expectation, so that we can evaluate it using samples. Use the log derivative trick:

$$\nabla_\theta L(\theta) = - \sum_w r(w) p_\theta(w) \nabla_\theta \log p_\theta(w)$$

- This is an expectation $\nabla_\theta L(\theta) = - \mathbb{E}_{w^s \sim p_\theta} [r(w^s) \nabla_\theta \log p_\theta(w^s)]$
- Approximate this with sample mean

$$\nabla_\theta L(\theta) \approx - \frac{1}{N} \sum_{s=1}^N r(w^s) \nabla_\theta \log p_\theta(w^s)$$

- In practice we use only one sample

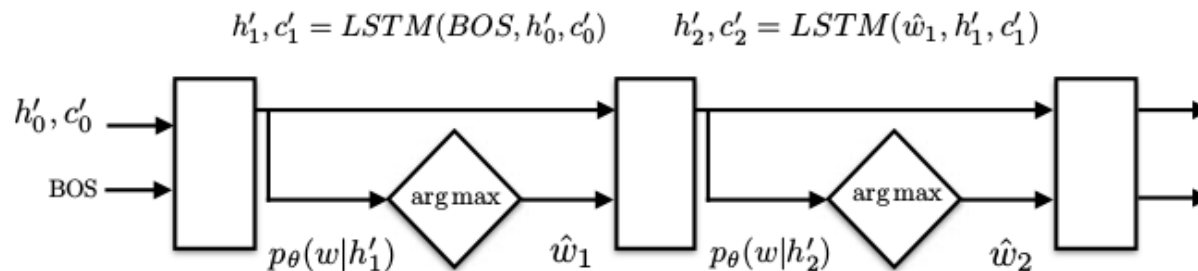
$$\nabla_\theta L(\theta) \approx -r(w^s) \nabla_\theta \log p_\theta(w^s)$$

Reinforcement Learning Details

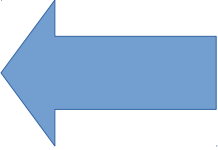
- Gradient $\nabla_{\theta} L(\theta) \approx -r(w^s) \nabla_{\theta} \log p_{\theta}(w^s)$
- This estimation has high variance. Use a baseline to combat this problem.

$$\nabla_{\theta} L(\theta) \approx -(r(w^s) - b) \nabla_{\theta} \log p_{\theta}(w^s)$$

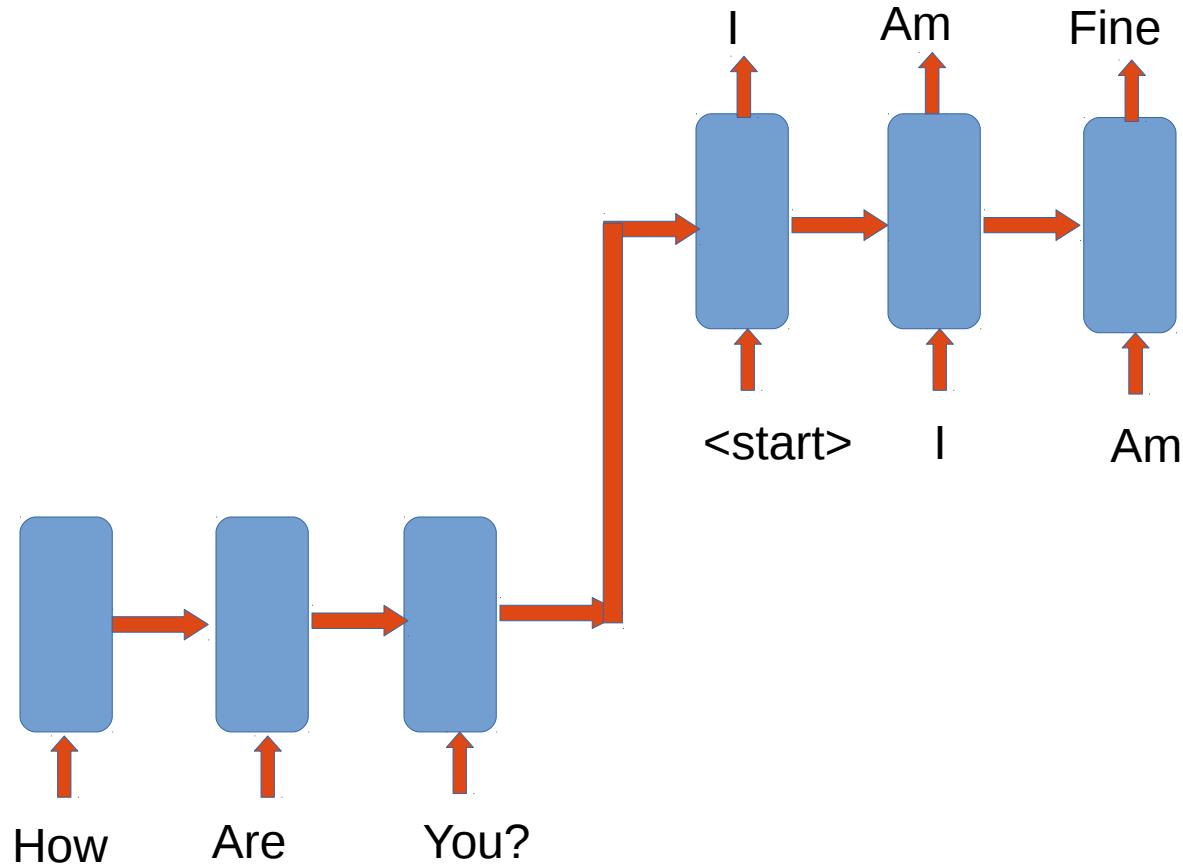
- Baseline can be anything independent of w^s
- It can for example be estimated as the reward for word sequence generated using argmax at each cell, $b = r(\hat{w}_1, \hat{w}_2, \hat{w}_3, \dots, \hat{w}_T)$



Reinforcement Learning

- Machine Translation/Summarization
- Dialog Systems 
-
-

Maximum Likelihood Dialog Systems



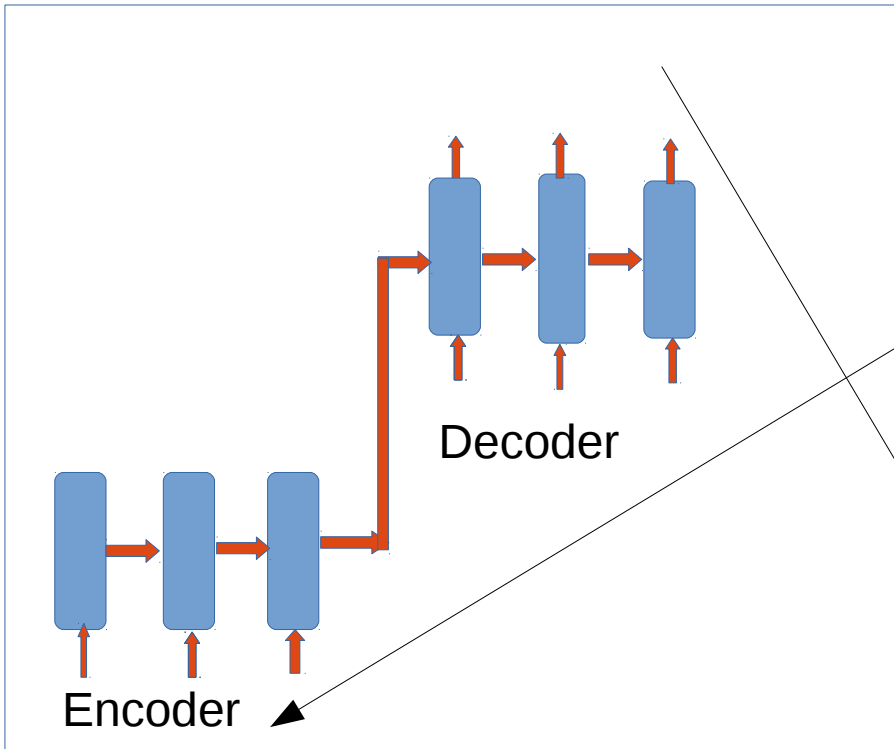
Why Reinforcement Learning

- Maximum Likelihood criterion is not directly relevant to successful dialogs
 - Dull responses (“I don’t know”)
 - Repetitive responses
- Need to integrate developer defined rewards relevant to longer term goals of the dialog

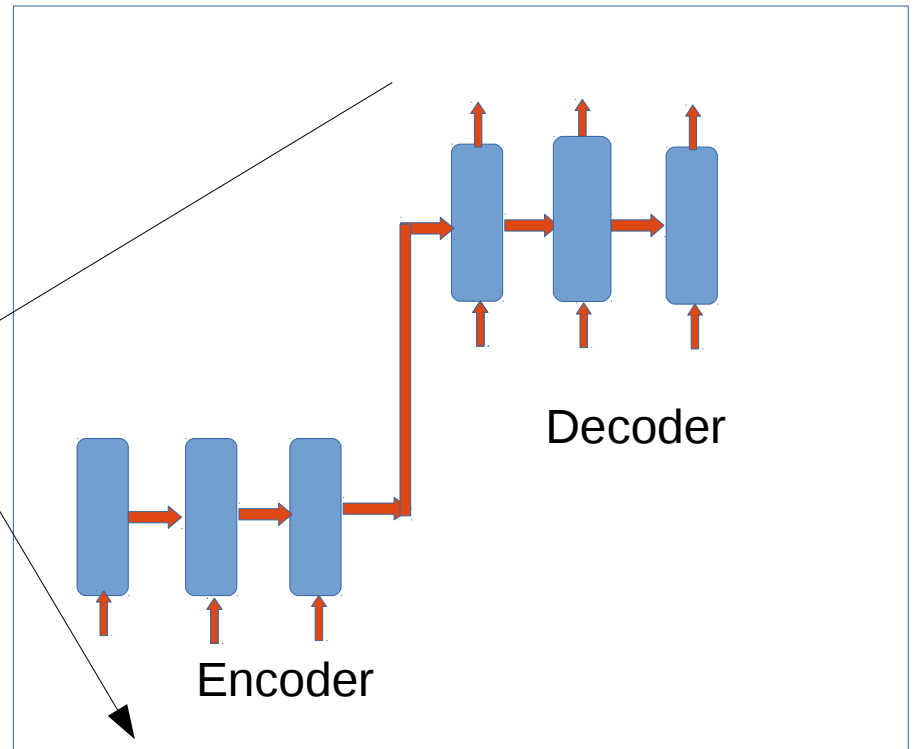
Dialog Generation as Reinforcement Learning

- **Agent:** The Recurrent Net
- **State:** Previous dialog turns
- **Action:** Next dialog utterance
- **Policy:** Generate the next dialog utterance (*action*) given the previous dialog turns (*state*)
- **Reward:** Score computed based on relevant factors such as ease of answering, information flow, semantic coherence etc.

Training Setup



Agent 1



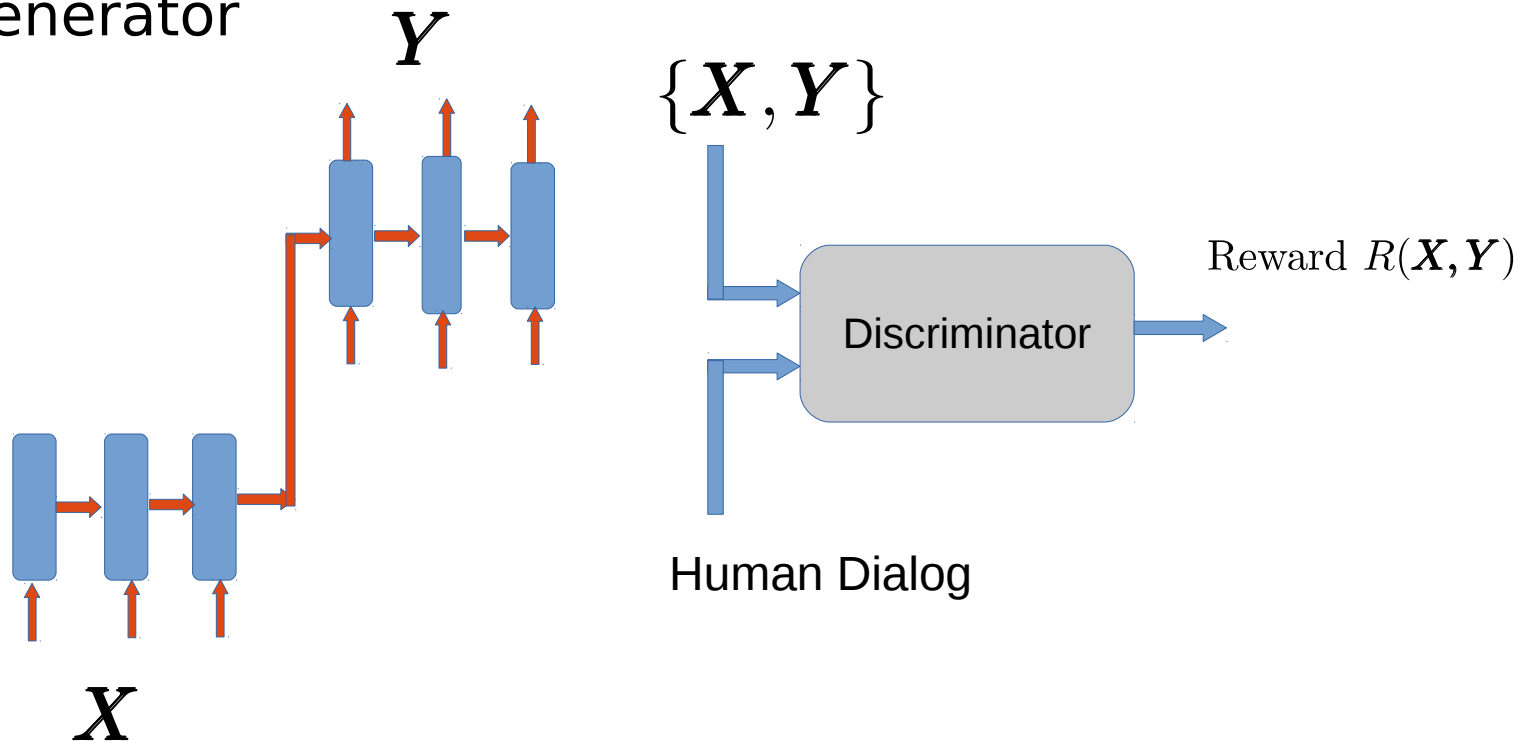
Agent 2

Training Procedure

- From the viewpoint of a given agent, the procedure is similar to that of sequence generation
 - REINFORCE algorithm
- Appropriate rewards must be calculated based on current and previous dialog turns.
- Can be initialized with maximum likelihood trained models.

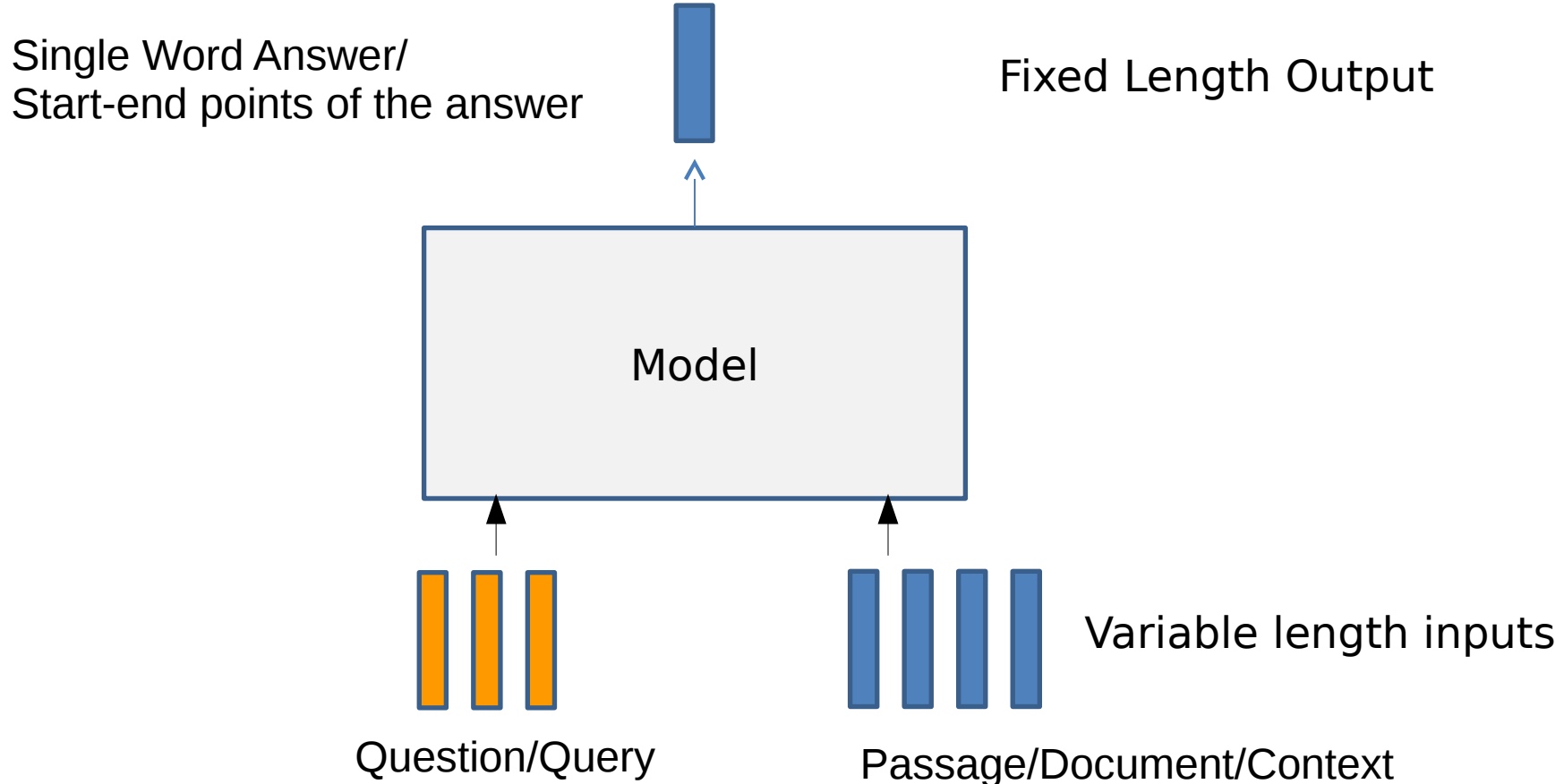
Adversarial Learning

- Use a discriminator as in GANs to calculate the reward
- Same training procedure based on REINFORCE for generator



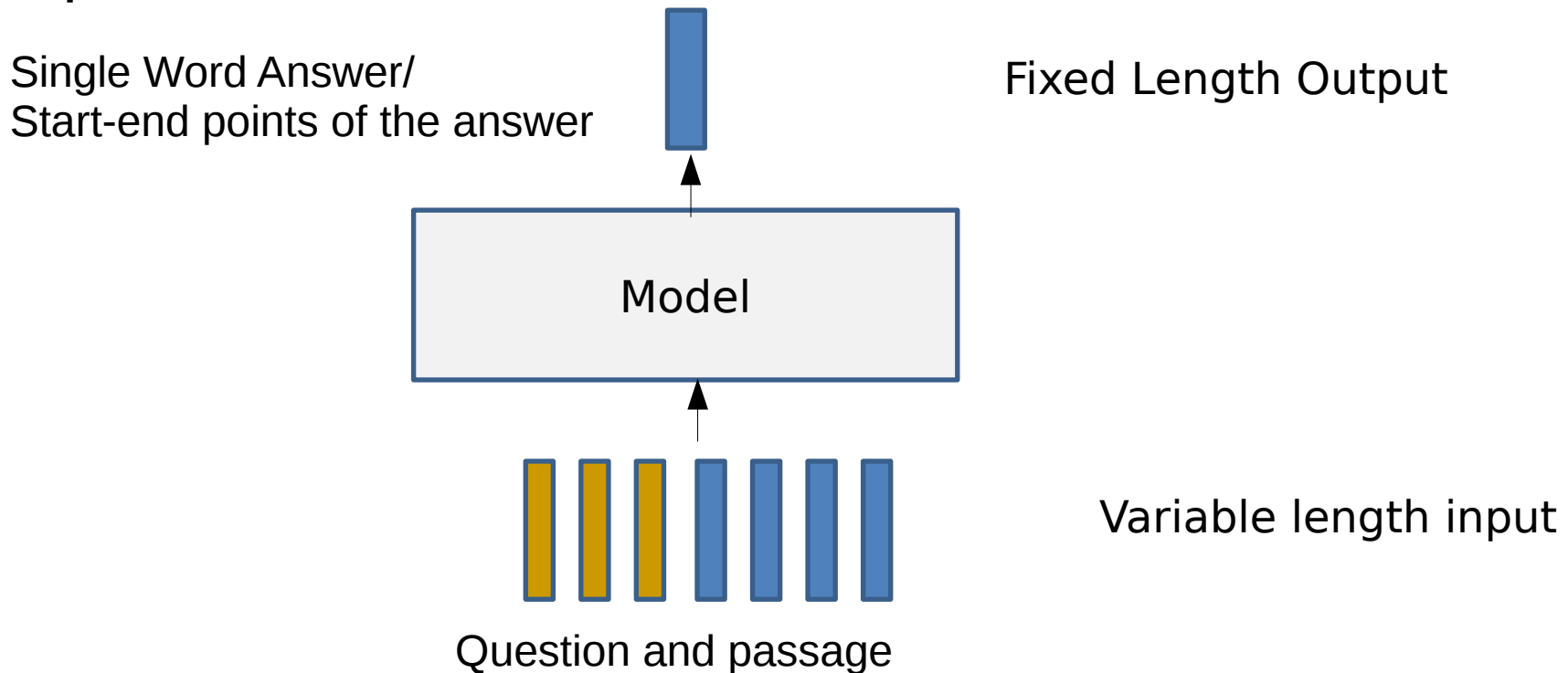
Question Answering

- Slightly different from sequence-to-sequence model.



QA- Naive Approach

- Combine question and passage and use an RNN to classify it.
- Will not work because relationship between the passage and question is not adequately captured.



QA- More Successful Approach

- Use attention between the question and passage
 - Bi-directional attention, co-attention
- Temporal relationship modeling
- Classification or predict start and end-point of the answer within passage.

QA Example with Bi-directional Attention

