Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Convolutional Neural Networks and how to fit them

Eilif Solberg

TEK5040/TEK9040

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Outline

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

Neural Networks Neuron Network of neurons

CNN Architectures Convolutional neural networks

Fitness

Optimization

Regularization

Hyperparameters

Getting started

Supervised Deep Learning Cheat Sheet

- 1. Generate training and validation data on the form x, y, where y is the supervision, e.g. class label, only available during training. Later, add data augmentation to training data to improve generalization.
- 2. Create a suitable model (use pretrained model if appropriate). Add model regularization to improve generalization.
- 3. Define a metric (what you care about) and loss function (something differentiable).
- 4. Choose an optimizer (SGD-like) and learning rate (schedule).
- 5. Define training step where we on a minibatch x, y:
 - Calculate model predictions \hat{y} and loss wrt y.
 - Find gradient of loss with respect to variables
 - Update model paramaters either by passing gradients to optimizer, or by using custom update rule.
 - Update loss and metric summaries.
- 6. Define validation step where we on each iteration update metric (and optionally loss) summaries.
- 7. Regularly plot loss and metric as well as other potential summaries.

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 •0000000000
 00000000000
 00000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Neural Networks

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで



Biological model



イロト 不得 トイヨト イヨト

-

Figure: Biological model of neuron. Illustration from http://cs231n.github.io/neural-networks-1/

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 00000000000
 00000000000
 00000

Mathematical model



Figure: Biological model of neuron. Illustration from http://cs231n.github.io/neural-networks-1/



イロト 不得下 イヨト イヨト

ъ

Figure: Mathematical model of Neuron. Illustration from http://cs231n.github.io/neural-networks-1/

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 0000000000
 0000000000
 00000
 0000000000
 0000
 0000
 0000

Neuron in TensorFlow

```
import numpy as np
1
    import tensorflow as tf
2
3
    class Neuron(object):
4
      def __init__(self, num_inputs):
5
        self.weights = tf.Variable(np.random.uniform(-0.1, 0.1,
6
        → size=num_inputs)) # random uniform initialzation
        self.bias = tf.Variable(0) # zero initialization
7
8
9
      def call (self. x):
10
        """Calculate activation for the neuron."""
        cell_body_sum = tf.reduce_sum(x*self.weights) + self.bias
11
12
        # apply sigmoid activation function
        firing_rate = 1.0 / (1.0 + tf.exp(-cell_body_sum))
13
        return firing rate
14
15
16
     neuron = Neuron(num_inputs=5)
     output = neuron([0.1, 0.4, -0.3, 0.7, -1.3])
17
```

• Why do we define the weights and bias with tf.Variable?

▲ロト ▲冊ト ▲ヨト ▲ヨト ヨー のくで



Detector / activation function

Non-saturating activation functions as ReLU, leaky ReLU dominating





Figure: Sigmoid function

Figure: Tanh function

Figure: ReLU function

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

Activation functions in TensorFlow

Some commonly used activations functions are already implemented and can be found at tf.keras.activations, e.g.

1 # Note that activation functions work elementwise on the input → tensor/array
2 tf.keras.activations.relu # f(x) = tf.maximum(x, 0)
3 tf.keras.activations.tanh # f(x) = → (tf.exp(2*x)-1)/(tf.exp(2*x)+1)
4 tf.keras.activations.sigmoid # f(x) = 1 / (1+tf.exp(-x))

Note: activation functions with *trainable parameters* are found under tf.keras.layers and start with *uppercase* letters.

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 000000
 0000000000
 00000000000
 00000000000
 00000000000
 00000

Network with several fully connected layers



Figure: Illustration from http://cs231n.github.io/neural-networks-1/

▲ロト ▲園 ト ▲ ヨ ト ▲ ヨ ト ● ④ ● ●

- What is the number of parameters?
- Mathematican: One hidden layer is enough

Layer of neurons in TensorFlow

```
class FullyConnected_v1(object):
1
2
      def __init__(self, num_inputs, num_outputs):
        self.weights = tf.Variable(np.random.uniform(-0.1, 0.1,
3
            size=[num_inputs, num_outputs]))
        \hookrightarrow
        self.bias = tf.Variable(np.zeros(num_outputs))
4
5
      def __call__(self, x):
6
        # Why do we right-multiply with matrix rather than
7
        \hookrightarrow left-multiply?
        return tf.matmul(x, self.weights) + self.bias
8
9
    # array of shape [batch_size, 3] ==> [batch_size, 5]
10
    fc = FullyConnected_v1(nun_inputs=3, num_outputs=5)
11
    # array of shape [2, 3] ==> [2, 5]
12
    fc(np.array([[1.0, 0.4, 0.2], [-0.4, 0.3, 0.2]]))
13
```

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 0000000000
 00000
 00000000000
 0000
 00000
 00000

Layer of neurons in TensorFlow as Keras Layer

```
class FullyConnected_v2(tf.keras.layers.Layer):
 1
2
       def __init__(self, num_outputs):
         super(FullyConnected_v2, self).__init__()
3
         self.num_outputs = num_outputs
4
\mathbf{5}
6
       def build(self, input_shape):
         """Assume input_shape[0] is batch size and input_shape[1] is size
7
         \hookrightarrow of input samples."""
         self.W = tf.Variable(np.random.uniform(-0.1, 0.1,
8

    size=[input_shape[1], self.num_outputs]))

         self.b = tf.Variable(np.zeros(self.num_outputs))
9
10
       def call(self, x):
11
         return tf.matmul(x, self.W) + self.b
12
13
     # array of shape [batch_size, num_inputs] ==> [batch_size, 5]
14
    fc = FullyConnected_v2(num_outputs=5)
15
     # array of shape [2, 3] ==> [2, 5]
16
    fc(np.array([[1.0, 0.4, 0.2], [-0.4, 0.3, 0.2]]))
17
```

- Why don't we need to specify the number of input nodes?
- Can we later give an array of shape [2,4] as input?

Notes on extending Keras layer

- The build method is called the first time __call__ is called.
- We implement call rather than __call__. The __call__ metods is implemented in the parent class, and will call 'call'
- We may also use self.add_variable method to add variables to layer
- Remember to call super method in __init__ to initialize Layer class properly.
- This layer can already be found at tf.keras.layers.Dense (with more functionality)
- Optional: Implement get_config and compute_output_shape (for serialization and model summary purposes respectiverly).
- See custom layers and models guide and Layer documentation.

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 0000000000
 0000000000
 0000000000
 00000000000
 00000
 00000
 00000

Create model

```
class MyModel(tf.keras.Model):
1
      def __init__(self):
2
        super(MyModel, self).__init__()
3
        self.d1 = tf.keras.layers.Dense(4, activation='relu')
4
        self.d2 = tf.keras.layers.Dense(4, activation='relu')
5
        self.d3 = tf.keras.layers.Dense(1, activation='sigmoid')
6
7
      def call(self, x):
8
        x = self.d1(x)
9
        x = self.d2(x)
10
        return self.d3(x)
11
12
    model = MyModel()
13
    print(model(np.array([[1.0, 0.4, 0.2], [-0.4, 0.3, 0.2]])))
14
    print(model.summary())
15
```

Use kernel_initializer and bias_initializer arguments to specify initialization scheme different from default.

• Will later look at simpler ways as well to create a model.

CNN Architectures

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで

Template matching



Figure: Illustration from

http://pixuate.com/technology/template-matching/

1. Try to match template at each location by "sliding over window"

2. Threshold for detection

For 2D-objects, kind of possible but difficult

Neural Networks CNN Architectures Fitness 0000000000

Optimization Regularization

Hyperparameters Getting started

Convolution



Which filter has produces the activation map on the right?





Convolutional layer

-> Glorified template matching

- Many templates (aka output filters)
- We learn the templates, the weights are the templates
- Intermediate detection results only means to an end
 - treat them as *features*, which we again match new templates to

▲ロ ▶ ▲周 ▶ ▲ ヨ ▶ ▲ ヨ ▶ ● の < ○

• Starting from the second layer we have "nonlinear filters"

Hyperparameters of convolutional layer

- 1. Kernel height and width template sizes
- 2. Stride skips between template matches
- 3. Dilation rate
 - *Holes* in template where we "don't care".
 - Larger field-of-view without more weights...
- 4. Number of output filters number of templates
- 5. Padding expand image, typically with zeros

| input neurons | |
|-----------------------------------------|-----------------------------------------|
| 000000000000000000000000000000000000000 | first hidden layer |
| 00000 | |
| 00000 | 000000000000000000000000000000000000000 |
| 000000000000000000000000000000000000000 | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |

Figure: Image from http://neuralnetworksanddeeplearning.com/

▲ロ ▶ ▲周 ▶ ▲ ヨ ▶ ▲ ヨ ▶ ● の < ○

2D-Convolutional layers in TensorFlow

```
conv = tf.keras.layers.Conv2D(
1
      filters, # e.q. 64
2
      kernel_size, # e.g. (3, 3)
3
      strides=(1, 1).
4
      padding='valid', # other option is 'same'
5
      data_format=None,
6
      dilation_rate=(1, 1),
7
      activation=None,
8
      use bias=True.
9
      kernel_initializer='glorot_uniform',
10
      bias_initializer='zeros',
11
      kernel_regularizer=None,
12
      bias_regularizer=None,
13
      activity_regularizer=None,
14
15
      kernel_constraint=None,
16
      bias_constraint=None,
      **kwargs)
17
```

Note: some arguments can be both *strings* and *python objects*.



Pro tip

Many properties of convolutional layers can be most easily studied by considering 1D convolutions.

1. Shape of output (P=padding, W=kernel_width, S=stride)

$$(input_width + 2P - W)/S + 1$$

2. Field-Of-View as function of depth d (if stacked), assuming no stride, and W odd.

$$d(W-1)+1$$

▲ロ ▶ ▲周 ▶ ▲ ヨ ▶ ▲ ヨ ▶ ● の < ○

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 0000000000
 0000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 000000
 00000
 00000

Basic CNN architecture for image classification

Image \rightarrow [Conv \rightarrow ReLU]xN \rightarrow Fully Connected \rightarrow Softmax

• Increase filter depth when using stride

Improve with:

- Batch normalization
- Skip connections ala ResNet or DenseNet
- No fully connected, average pool predictions instead

▲ロ ▶ ▲周 ▶ ▲ ヨ ▶ ▲ ヨ ▶ ● の < ○

```
CNN TensorFlow
```

Can use tf.keras.models.Sequential to easily define a model from a sequence of layers

```
from tensorflow.keras.layers import Conv2D, Flatten, Dense
1
2
   model = tf.keras.models.Sequential([
3
     Conv2D(32, kernel_size=3, activation='relu'),
4
     Conv2D(64, kernel_size=3, strides=2, activation='relu'),
5
6
     Flatten().
     Dense(128, activation='relu'),
7
     Dense(10, activation='softmax')
8
   1)
9
```

```
        Neural Networks
        CNN Architectures
        Fitness
        Optimization
        Regularization
        Hyperparameters
        Getting started

        00000000000
        0000000000
        00000
        0000000000
        0000
        00000
        00000
```

CNN TensorFlow II

```
inputs = tf.keras.Input(shape=(32, 32, 3))
x = Conv2D(32, kernel_size=3, activation='relu')(inputs)
x = Conv2D(64, kernel_size=3, strides=2, activation='relu')(x)
x = Flatten()(x)
x = Dense(128, activation='relu')(x)
outputs = Dense(10, activation='softmax')(x)
model = tf.keras.Model(inputs=inputs, outputs=outputs)
```

• Allows for non-sequential structure, but structure of layers is still fixed in advance.

CNN TensorFlow III

```
class MyModel(tf.keras.Model):
1
      def init (self):
2
3
         super(MyModel, self).__init__()
        self.conv1 = Conv2D(32, kernel_size=3, activation='relu')
4
        self.conv2 = Conv2D(64, kernel size=3, strides=2, activation='relu')
5
        self.flatten = Flatten()
6
        self.d1 = Dense(128, activation='relu')
7
        self.d2 = Dense(10, activation='softmax')
8
9
      def call(self. x):
10
        x = self.conv1(x)
11
        x = self.conv2(x)
12
13
        x = self.flatten(x)
        x = self.d1(x)
14
        return self.d2(x)
15
16
    model = MyModel()
```

Most flexible, but more code (and thus room for mistakes).

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

• Need model code to restore model as python object.

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Fitness

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 0000000000
 0000000000
 0000000000
 0000
 00000
 00000

How do we fit model?

▲□▶ ▲□▶ ▲□▶ ▲□▶ = 三 のへで

How do we find parameters θ for our network?

Supervised learning

- Training data comes as (X, Y) pairs, where Y is the target
- Want to learn f_θ(x) ~ p(y|x), conditional distribution of Y given X, where θ are our parameters.
- Define *differentiable* surrogate loss function, e.g. for a single sample with $Y \in \mathbb{R}^n$ and $Y \in \mathbb{N}$ respectively:

$$l(\theta) = l(f_{\theta}(X), Y) = \sum_{i=1}^{n} ((f_{\theta}(X))_{i} - Y_{i})^{2}$$
 squared error loss
$$l(\theta) = l(p_{\theta}(X), Y) = -log(p_{\theta}(X)_{Y})$$
 negative likelihood

The first loss is common in *regression*, while the second is common in *classification*.

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 000000
 000000
 0000000000
 000000
 00000
 00000

Losses in TensorFlow

```
def mean_squared_error(y_true, y_pred):
1
       """y_true: [batch_size, n], y_pred : [batch_size, n]"""
2
       # sum over axis, mean over batch dimension
3
      return tf.reduce_mean(tf.reduce_sum((y_true-y_pred)**2,
4
       \rightarrow axis=-1))
5
    def sparse_categorical_cross_entropy(y_true, y_pred):
6
       """y_true: [batch_size], y_pred : [batch_size, num_classes]"""
7
      y_true = tf.expand_dims(y_true, axis=-1) # [batch_size] ==>
8
       \hookrightarrow [batch size. 1]
       # tf.qather \rightarrow extracts probabilities from y_pred using
9
       \hookrightarrow indices in y_true
      log_likelihoods = tf.math.log(tf.gather(y_pred, y_true,
10
       \rightarrow batch dims=1))
      return -tf.reduce_mean(log_likelihoods)
11
12
    mean_squared_error(np.zeros((3, 5)), np.ones((3, 5))) # ==> 5
13
    sparse_categorical_cross_entropy([0, 1, 2], [[.9, .05, .05],
14
    \rightarrow [.5, .89, .6], [.05, .01, .94]])
```

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 0000000000
 0000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 000000
 00000
 00000

Losses in TensorFlow II

Many losses can already be found implemented at tf.keras.losses.

```
mse = tf.keras.losses.MeanSquaredError()
1
   loss = mse([0., 0., 1., 1.], [1., 1., 1., 0.])
2
   print('Loss: ', loss.numpy()) # Loss: 0.75
3
4
5
   cce = tf.keras.losses.SparseCategoricalCrossEntropy(from_logits
    \rightarrow =False) # set true if not softmax
    \hookrightarrow applied
   loss = cce([0, 1, 2], [[.9, .05, .05], [.5, .89, .6], [.05, .05])
6
    \rightarrow .01, .94]])
   print('Loss: ', loss.numpy()) # Loss: 0.3239
7
```

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 00000000000
 0000000000
 00000

Optimization

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 0000000000
 0000000000
 0000000000
 00000
 00000
 00000

Gradient

- For a function f: ℝⁿ → ℝ the gradient is the n-dimensional vector of all partial derivatives of the f with respect to the input variables.
- The gradient is the direction for which the function increases the most.



Figure: Gradient of the function $f(x^2, y^2) = x/e^{x^2+y^2}$ [By Vivekj78 [CC BY-SA 3.0 (https://creativecommons.org/licenses/by-sa/3.0)], from Wikimedia Commons]

イロト 不得 トイヨト イヨト

Neural Networks CNN Architectures Fitness Optimization Regularization Hyperparameters Getting started 00000000000 0000000000 00000 0000000000 00000 00000 00000

How do we find the gradient?

• Approximate by finite differences. Recall that for a function of one variable

$$\frac{d}{dx}f(x)\approx\frac{f(x+h)-f(x)}{h}$$

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● ○ ○ ○

for small enough h. How does this scale with number of variables?

- Analytically with backpropagation
 - Integration is an art derivation is craftmanship.
 - Gradients propagated from output towards input.

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 0000000000
 00000
 0000000000
 00000
 00000
 00000

Automatic differentiation - first order

Compute first order derivatives

```
1 x = tf.constant(3.0)
2 with tf.GradientTape() as g:
3 g.watch(x) # keep 'tape' of values that x affects
4 y = x * x
5 # Find derivative of y with respect to x
6 dy_dx = g.gradient(y, x) # Will compute to 6.0 (dy_dx x^2 = 2x)
```

Note that y should always be a scalar (typically our loss value), while x can in general be a vector (typically the parameters of our model).

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000
 00000000000
 0000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Automatic differentiation wrt. variables

No need to explicitly add 'watch' for trainable variables

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 0000000000
 00000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Automatic differentitation - second order

Compute first and second order derivatives

```
1 x = tf.Variable(3.0)

2 with tf.GradientTape() as g:

3 with tf.GradientTape() as gg:

4 y = x * x

5 dy_dx = gg.gradient(y, x) \# Will compute to 6.0 (dy_dx x^2 = 

<math>\Rightarrow 2x)

6 d2y_dx^2 = g.gradient(dy_dx, x) \# Will compute to 2.0 (dy_dx 2x)

\Rightarrow = 2)
```

For more information:

 https://www.tensorflow.org/api_docs/python/tf/ GradientTape

(Stochastic) gradient descent

Taking steps in the opposite direction of the gradient



Figure: [By Vivekj78 [CC BY-SA 3.0 (https://creativecommons.org/licenses/by-sa/3.0)], from Wikimedia Commons]

• Full gradient too expensive / not necessary

$$\sum_{i=1}^{N} \nabla_{\theta} l(f(X_i), Y_i) \approx \sum_{i=1}^{n} \nabla_{\theta} l(f(X_{P(i)}), Y_{P(i)})$$
(1)

イロト 不得 トイヨト イヨト

-

for a random permutation P.

Updating model with vanilla gradient descent

```
for x, y in train_data:
1
     with tf.GradientTape() as tape:
2
        y_pred = model(x, training=True) # training argument only
3
        \leftrightarrow needed when model has different behaviour under
        \leftrightarrow training and inference
        loss = loss_fn(y, y_pred)
4
5
     grads = tape.gradient(loss, model.trainable_variables)
6
     for grad, var in zip(grads, model.trainable_variables):
7
        var.assign_add(-lr*grad) # var = var - lr*grad
8
```

Can we do better than basic gradient descent with fixed step size?

Updating model with optimizer

'Optimizers' try to improve upon the simple update rule above by e.g. trying to incorporate some kind of curvature (without calculating second derivatives!)

```
optimizer = tf.keras.optimizers.SGD(0.0001, momentum=0.9)
1
   for x, y in train_data:
2
     with tf.GradientTape() as tape:
3
       y_pred = model(x, training=True)
4
       loss = loss_fn(y, y_pred)
5
6
     grads = tape.gradient(loss, model.trainable_variables)
7
     optimizer.apply_gradients(zip(grads,
8
         model.trainable variables))
```

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Optimizer

1 print(tf.keras.optimizers.Adam.__doc__)

Optimizer that implements the Adam algorithm. Adam optimization is a stochastic gradient descent method that is based on adaptive estimation of first-order and second-order moments. According to the paper [Adam: A Method for Stochastic Optimization. Kingma et al., 2014](http://arxiv.org/abs/1412.6980), the method is "*computationally efficient, has little memory requirement, invariant to diagonal rescaling of gradients, and is well suited for problems that are large in terms of data/parameters*".

For AMSGrad see [On The Convergence Of Adam And Beyond. Reddi et al., 5-8](https://openreview.net/pdf?id=ryQu7f-RZ).

- SGD with momentum, RMSprop, Adam are popular choices
- For more see https://www.tensorflow.org/api_docs/ python/tf/keras/optimizers.



Learning rate schedule

Normally you want to reduce your learning rate as training progresses (typically when loss stops decreasing).

```
class MySchedule(tf.keras.optimizers.
   schedules.LearningRateSchedule):
 def __call__(self, step):
    if step < 100000:
      1r = 0.1
    elif 100000 <= step < 200000:
      lr = 0.01
    else:
      lr = 0.001
   return lr
optimizer = tf.keras.optimizers.SGD(M
   ySchedule())
```



Figure: Example train run following learning rate schedule shown left.

See e.g. tf.keras.optimizers.schedules for common learning rate schedules.

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 0000
 00000
 00000
 00000

Regularization

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで



Overfitting



Figure: Model complexity. {Image from scikit-learn}

Figure: Train vs test error

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

- Early stopping is an option, but can we do better?
- Also see tutorial https://www.tensorflow.org/ tutorials/keras/overfit_and_underfit

Neural NetworksCNN ArchitecturesFitnessOptimizationRegularizationHyperparametersGetting started0000000000000000000000000000000000000000000000000000000000000000000000000000000

Regularization vs optimization

- Optimization: try to reduce training loss
 - often leads to reduction of validation/test loss as a side-effect

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

- Regularization: try to reduce test loss
 - may lead to increase in train loss

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 0000
 00000
 0000
 00000

Weight regularization

- Penalize non-smooth functions by penalizing large values for the model weights.
- Weight penalty added to loss term, usually squared L2 normalization uniformly for all parameters

 $J(\theta) = I(\theta) + \lambda \|\theta\|_2^2$

where $\lambda \geq 0$. In TensorFlow this might look like

```
        Neural Networks
        CNN Architectures
        Fitness
        Optimization
        Regularization
        Hyperparameters
        Getting started

        00000000000
        00000000000
        00000
        00000000000
        0000
        00000
        00000
```

Weight regularization in TensorFlow - layer

```
dense = tf.keras.layers.Dense(10,
1
      kernel_regularizer=tf.keras.regularizers.12(0.0001))
   \hookrightarrow
   # each time dense is run for input x, a loss is added to
2
       dense.losses
   \rightarrow
   for x, y in train_data:
3
     with tf.GradientTape() as tape:
4
       v_pred = dense(x)
5
6
       loss = loss_fn(y, y_pred) # primary loss
       loss += sum(dense.losses) # add regularization loss
7
       assert dense.losses[0].numpy() ==
8
       # ... compute gradient, update model
9
```

Weight regularization in TensorFlow - use in model

If you have a tf.keras.Model object, *model*, the losses for all layers will be collected into the list *model.losses*.

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● ○ ○ ○

Dropout



Figure: Left: Inference execution of model. Right: sample of train execution.

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで

```
TensorFlow dropout
```

- 1 dropout = tf.keras.layers.Dropout(0.5)
- 2 tf.random.set_seed(123)
- x = [[1.0, 1.0, 1.0], [1.0, 1.0]]
- 4 dropout(x, training=True) # [[0., 2., 0.], [2., 2., 2.]]
- 5 dropout(x, training=True) # [[2., 0., 2.], [2., 2., 0.]]
- 6 dropout(x, training=False) # [[1., 1., 1.], [1., 1., 1.]]
 - Different behaviours during training and inference (randomness only during training)

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

• Expected value remains the same



Batch normalization

- Unit normalize the input of a neuron, or set of (related) neurons, over the batch.
- Idea: keep mean and standard deviation of input fairly constant to improve optimization.

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

- Many theories why it works.
- Turns out randomness also act as regularization.
- Your best friend and your worst enemy

TensorFlow batch normalization

```
batch_norm = tf.keras.layers.BatchNormalization(axis=-1,
1
    \hookrightarrow center=False. scale=False)
   x = np.array([[-1.0, 4.0, 1.0], [1.0, -4.0, 3.0]])
2
   # [batch_size, num_features] == [2, 3]
3
   # feature 1: mean = 0, std ~= 1
4
   # feature 2: mean = 0, std ~= 4
\mathbf{5}
   # feature 3: mean = 2, std ~= 1
6
   batch_norm(x, training=True) # ~= [[-1.0, 1.0, -1.0], [1.0,
7
    \hookrightarrow -1.0. 1.077
   batch_norm(x, training=False) # ~= ?
8
```

 Different behaviours during training and inference (randomness only during training)

• Expected value about the same

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 0000000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 000000
 00000
 00000</t

Batch normalization for image data

For a tensor [batch_size \times height \times width \times depth], normalize "template matching scores" for each template *d* by

$$\mu_{d} \leftarrow \frac{1}{N * H * W} \sum_{i=1}^{N} \sum_{h=1}^{H} \sum_{w=1}^{W} x_{i,h,w,d}$$
(2)

$$\sigma_d^2 \leftarrow \frac{1}{N * H * W} \sum_{i=1}^{1} \sum_{h=1}^{1} \sum_{w=1}^{1} (x_{i,h,w,d} - \mu_d)^2$$
(3)

$$\hat{x}_{i,h,w,d} \leftarrow \frac{x_{i,h,w,d} - \mu_d}{\sqrt{(\sigma_d^2 + \epsilon)}} \tag{4}$$

$$y_{i,h,w,d} \leftarrow \gamma \hat{x}_{i,h,w,d} + \beta \tag{5}$$

where N, H and W represents batch size, height and width.

- "Template/Feature more present than usual or not"
- During inference we use stored values for μ_d and σ_d .
- scale and center params in BatchNormalization layer
 corresponds to α and β respectively

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 000000000000
 000000000000
 00000
 00000

Data augmentation

Idea: apply random transformation to X that does not alter Y.

- Normally you would like result X' to be *plausible*, i.e. *could* have been a sample from the distribution of interest
- Which transformation you may use is application-dependent.
- May also have transformations that change Y as long as we know the effect. E.g. flipping image and label image for semantic segmentation.

Image data

- Horizontal mirroring (issue for objects not left/right symmetric)
- Random crop
- Scale
- Aspect ratio
- Lightning etc.

Text data

- Synonym insertion
- Back-translation: translate and translate back with e.g. Google Translate!!!

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 000000000000
 0000
 00000000000
 0000
 00000

Reguluarization summary

- Data augmentation randomness in *input* ==> "increases" training data set
- Dropout randomness in *activations*
- Batch normalization randomness in activations
- Usually either dropout or batch normalization enough
- Weight regularization penalizes large weights ("non-smooth function")

Hyperparameters

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで

Hyperparameters to search

From Wikipedia:

In machine learning, a hyperparameter is a parameter whose value is used to control the learning process. By contrast, the values of other parameters (typically node weights) are derived via training.

Important examples are:

- Learning rate (and learning rate schedule)
- Regularization params: L2, (dropout)
- Model architecture
 - What is the search space?



Search strategies

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

- Random search rather than grid search
- Logscale when appropriate
- Careful with best values on border
- May refine search

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000000000
 00000000000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000
 00000

Getting started

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで



Install TensorFlow

Need Python 3.5-3.8. In case of GPU, install prerequisites first. On Linux/Ubuntu (without virtual environment)

- 1 pip3 install --upgrade pip
- 2 pip3 install --user tensorflow>=2
 - See https://www.tensorflow.org/install for more.
 - API: https://www.tensorflow.org/api_docs/python/
 - Tutorials: https://www.tensorflow.org/tutorials

Why TensorFlow / machine learning framework

- Automatic differentiation
- High-level APIs for deep learning (Keras), yet flexible
- Predefined/pretrained models
- Speed optimized implementation accross devices
 - C++ on CPU
 - CUDA on Nvidia GPUs
 - TPU
 - Embedded devices



Predifined/pretrained models

```
from matplotlib import pyplot as plt
1
2
   model = tf.keras.applications.NASNetMobile(weights="imagenet")
3
   image_file = tf.keras.utils.get_file("dog.jpg",
4
    → "https://encrypted-tbn0.gstatic.com/images?q=tbn:ANd9GcRDg8
    image = plt.imread(image_file)
5
   plt.imshow(image); plt.show()
6
7
   # resize and preprocess to what model expects
8
   image = tf.expand_dims(tf.image.resize(image, [224, 224]), 0)
9
   image = tf.keras.applications.nasnet.preprocess_input(image)
10
   p = model(image)[0] # 1000-dimensional vector with probabilities
11
```

 Neural Networks
 CNN Architectures
 Fitness
 Optimization
 Regularization
 Hyperparameters
 Getting started

 00000000000
 00000000000
 00000
 00000000000
 00000
 00000
 00000

- 12 # Show labels and probabilty for top5 predictions
- 13 sorted_indices = tf.argsort(p, direction="DESCENDING")
- 14 labels_path = tf.keras.utils.get_file('ImageNetLabels.txt','htt |
 - → ps://storage.googleapis.com/download.tensorflow.org/data/Im → ageNetLabels.txt')

- 16 for idx in sorted_indices[:5]:
- 17 print("%25s: %g" % (imagenet_labels[idx], p[idx]))
 - Also unofficial/random models from community
 - Use as part of larger system and/or finetuning.