Some remarks on the mandatory assignment:

- Sets of the form  $U \times V$  are open in  $X \times Y$ , for  $U \subseteq X$ ,  $V \subseteq Y$  open subsets. However, not all open sets in  $X \times Y$  are on this form. Still it suffices to check continuity of functions  $Z \to X \times Y$  on sets of the form  $U \times V$ . You should know why.
- In exercise 1 you can save yourself (and me) a lot of time by using Theorem 19.6.
- In exercise 2d, f(nx) = nf(x) must be treated as a special case for an integer n < 0.
- In exercise 2d it would be nice if you specified that c = f(1). This was not so clear in all the solutions.

Curiously there were three different solutions. The most common approach was to prove that  $f|_{\mathbb{Q}} = f(1) \cdot \mathrm{id}_{\mathbb{Q}}$ , and use part c. Another approach was to use that  $\mathbb{Q}$  is dense in  $\mathbb{R}$  directly, and that limits commute with continuous functions. A third approach was to prove that f is differentiable and use the fundamental theorem of calculus.

• In exercise 3b the best model for the projective plane is likely  $\mathbb{P}^2 = S^2/(x \sim -x)$ , see page 372.