

9.10 z_1, z_2, z_3 uafhængige, $U[0,1]$ -fordelt.

Småts implikering: X_1, X_2, X_3

$$X_3 = z_3 \quad E[X_3 | \mathcal{F}_2] = E[z_3 | \mathcal{F}_2] = E[z_3] = \frac{1}{2}$$

$$X_2 = \max\{z_2, E[X_3 | \mathcal{F}_2]\} = \max\{z_2, \frac{1}{2}\}, \quad E[X_2 | \mathcal{F}_1] = E[X_2]$$

$$X_1 = \max\{z_1, E[X_2 | \mathcal{F}_1]\} = \frac{1}{2} \cdot \frac{3}{4} + \frac{1}{2} \cdot \frac{1}{2} = \frac{3}{8} + \frac{1}{4} = \frac{3}{8} + \frac{2}{8} = \frac{5}{8}$$

$$= \max\{z_1, \frac{5}{8}\}$$

$$E[X_1] = \frac{3}{8} \cdot \frac{\frac{5}{8} + 1}{2} + \frac{5}{8} \cdot \frac{3}{8} = \frac{3}{8} \cdot \frac{13}{8} + \frac{25}{64}$$

$$= \frac{3}{8} \cdot \frac{13}{16} + \frac{50}{128} = \frac{39}{128} + \frac{50}{128} = \frac{89}{128}$$