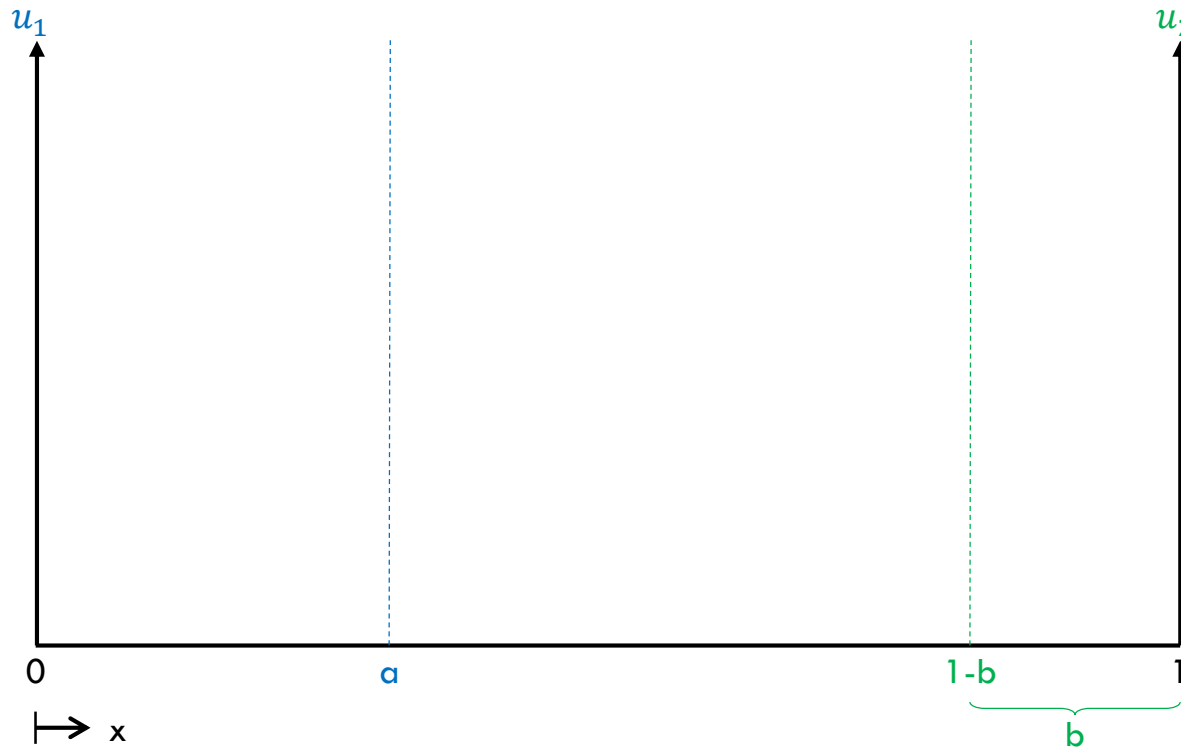


# The Linear city model

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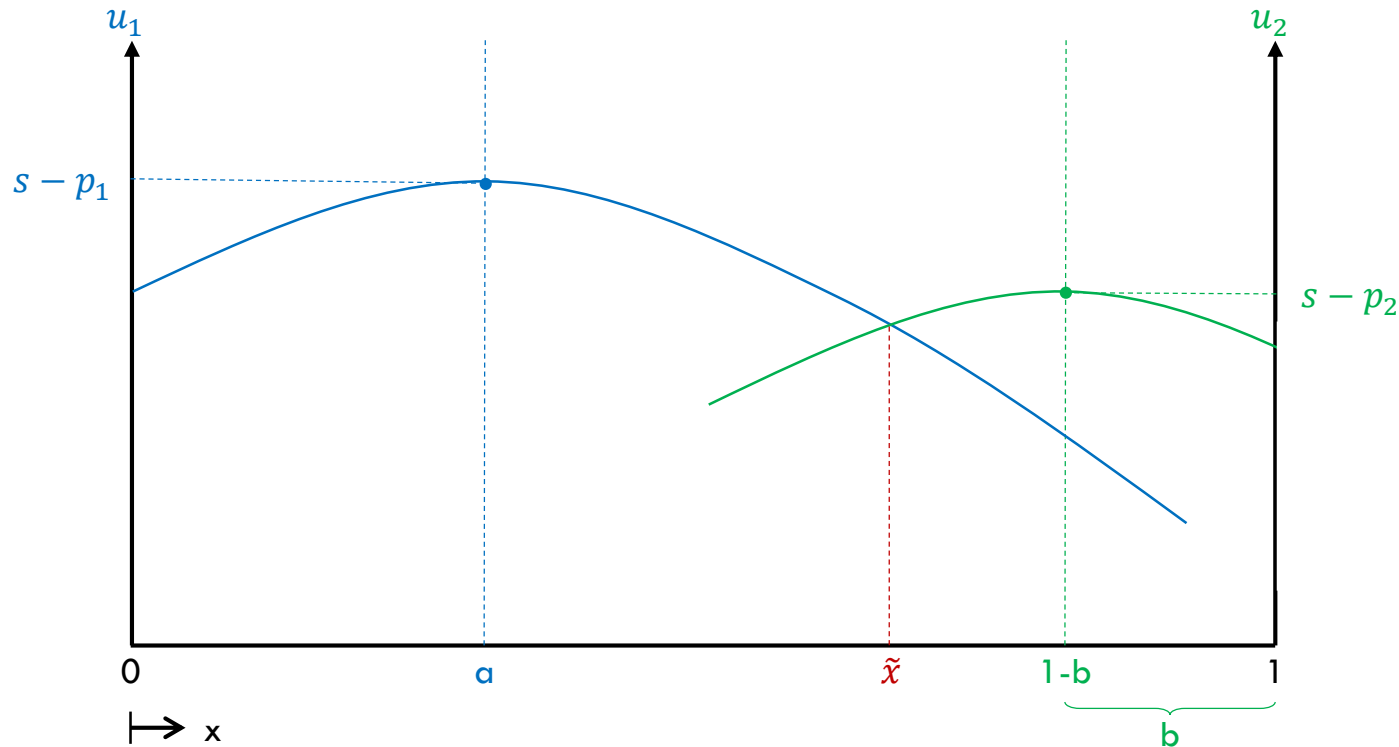
# The Linear city model

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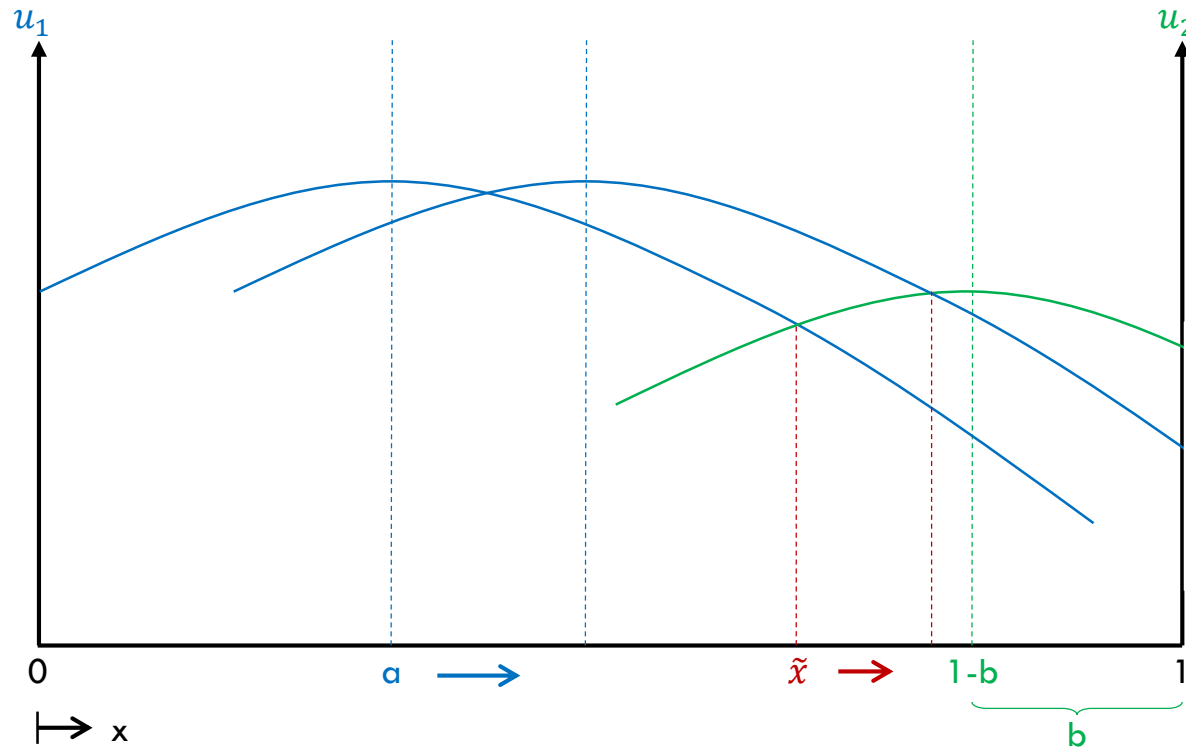
- X-axis: consumers are located uniformly from 0 to 1.
- Y-axis: consumer's utility from buying from firm 1 and firm 2 respectively
- Locations:
  - Firm 1 is located at  $a$
  - Firm 2 is located at  $1-b$

## The Linear city model



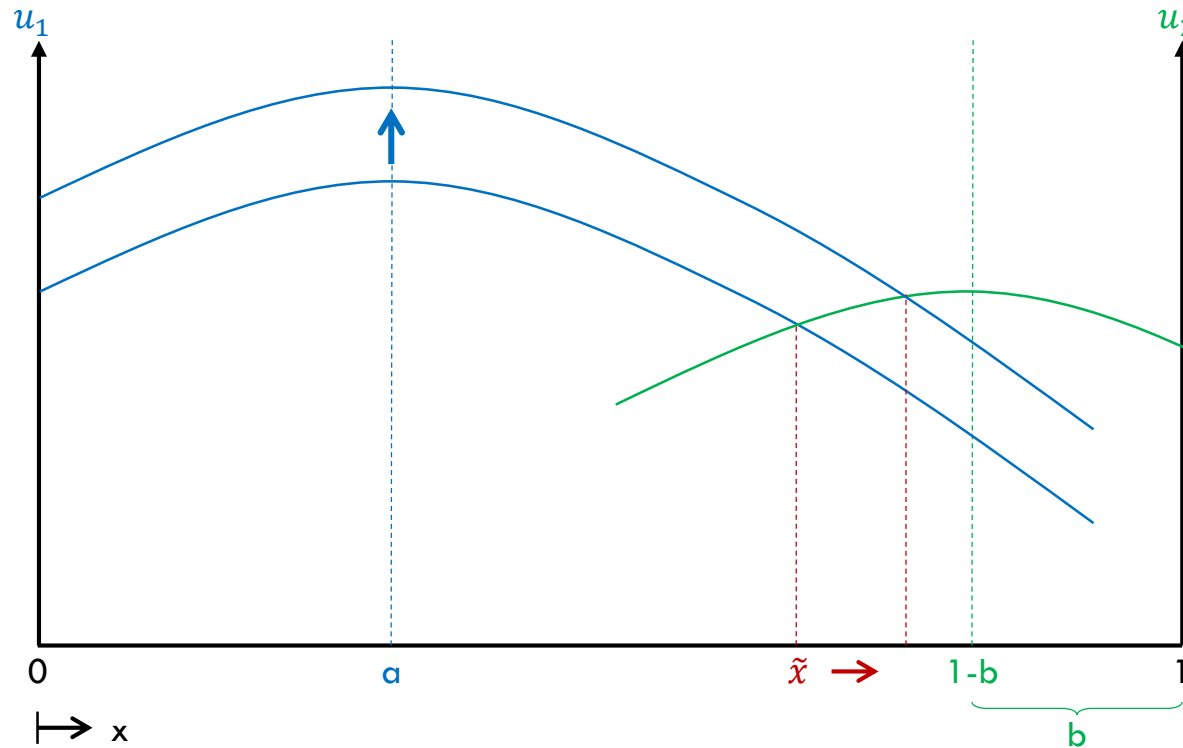
- Consumers have a reservation utility  $s$
- Utility decreases quadratically in the distance to the firm:
  - $u_1 = s - p_1 - t(x - a)^2$
  - $u_2 = s - p_2 - t(1 - b - x)^2$
- Consumers who are located at the same place as a store, utility is  $s - p$
- From there, utility decreases in distance.
- Demand is determined by the indifferent consumer  $\tilde{x}$ :
  - Firm 1:  $D_1(p_1, p_2, a, b) = \tilde{x}$
  - Firm 2:  $D_2(p_1, p_2, a, b) = 1 - \tilde{x}$

# The Linear city model



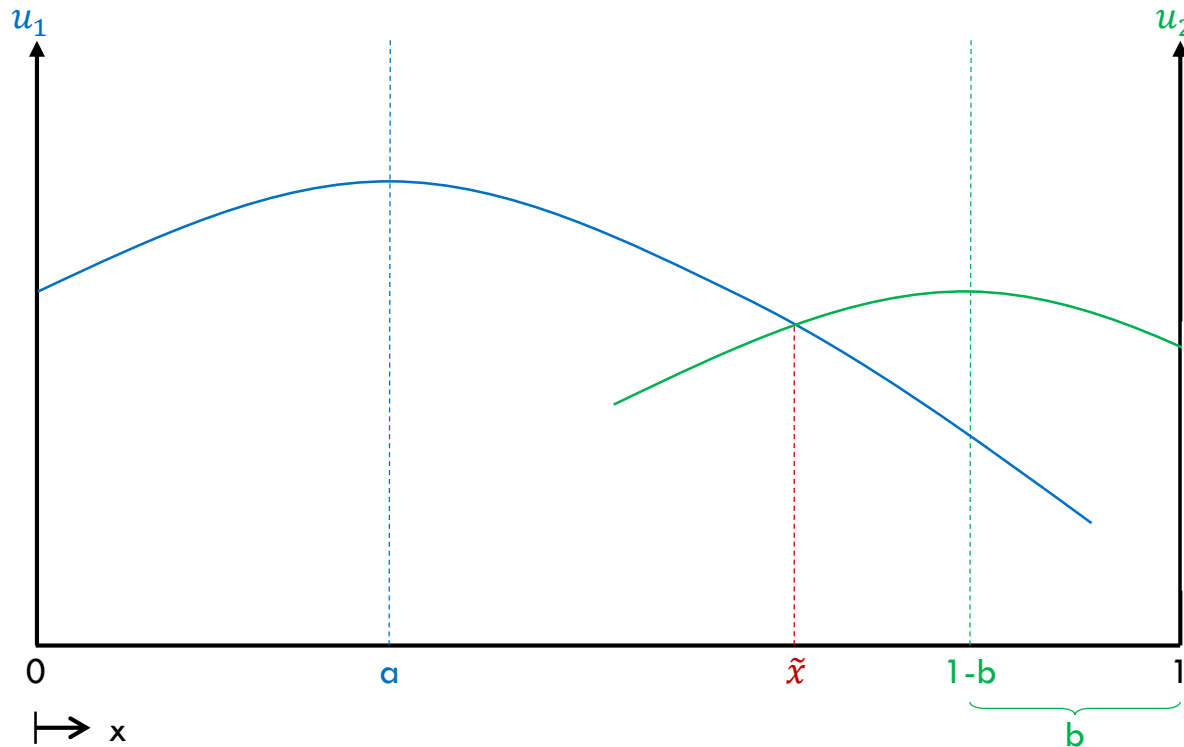
- Timing of the game:
  1. Firms choose location – this moves the «umbrellas» left/right

# The Linear city model



- Timing of the game:
  1. Firms choose location – this moves the «umbrellas» left/right
  2. Firms choose prices

# The Linear city model



- Timing of the game:
  1. Firms choose location – this moves the «umbrellas» left/right
  2. Firms choose prices
- What location is the optimal choice?
  - *Solution: Backward induction*
    - 1.Step: Solve the price game:
      - What are the optimal prices given  $a$  and  $b$ ?
      - Prices become functions of  $a$  and  $b$ :
 
$$p_1 = p_1(a, b)$$

$$p_2 = p_2(a, b)$$
    - 2.Step: Solve the location game.
      - What are the optimal locations  $a$  and  $b$ ?