

HG
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ECON 4130 14H

Exercises for seminar week 47

Rice chapter 9: No. 12, 33 (**Hint:** note that there are 0 parameters under H_0 here, so the DF for the Chi-square test must be equal to the number of free parameters in the full model.)
No. 40, 41

Extra exercise

An econometric model contains a response, Y , and 6 (exogenous) explanatory variables, $X, Z_1, Z_2, U_1, U_2, U_3$. The data are observations of $n = 22$ iid corresponding random vectors, $(Y_i, X_i, Z_{i1}, Z_{i2}, U_{i1}, U_{i2}, U_{i3})$, and the (full) regression model is (using observed values of the explanatory variables as fixed)

$$(1) \quad Y_i = \alpha + \beta x_i + \delta_1 z_{i1} + \delta_2 z_{i2} + \gamma_1 u_{i1} + \gamma_2 u_{i2} + \gamma_3 u_{i3} + e_i \quad \text{for } i = 1, 2, \dots, 22$$

Where, e_1, e_2, \dots, e_n are iid and normal, $e_i \sim N(0, \sigma^2)$.

A. Estimating (1) by OLS gives the following table of sums of squares (using Stata terminology)

Table 1 (for full model)

Source	SS	df
Model	7817	?
Residual	3743	?
Total	11560	?

Fill in the degrees of freedom (df's) in the table. Estimate the error term variance, σ^2 , using an unbiased estimator.

B. A submodel of interest is assuming both $\delta_1 = \delta_2$ and $\gamma_1 = \gamma_2 = \gamma_3$. We want to check if there is evidence in the data against this submodel using an appropriate F-test. We then need to re-estimate the model assuming the submodel (that we call the “reduced model”) to be true. Using OLS for the reduced model implies that we must regress the response Y on a modified set of explanatory variables.

Write up the corresponding (to (1)) regression model in the reduced case.

[Hint: Introduce two new parameters, δ for the common value of δ_1, δ_2 , and γ for the common value of $\gamma_1, \gamma_2, \gamma_3$, and substitute in (1). Define new regressor variables whenever necessary.]

- C. Estimating the reduced model by OLS gives the following table of sums of squares (using Stata terminology)

Table 2 (for the reduced model)

Source	SS	df
Model	5332	?
Residual	6228	?
Total	11560	?

Use this information to perform an F-test for testing the sub-model against the more general model in (1). Calculate the P-value, either approximately using the quantile table 5 in the back of Rice's book, or exactly using (e.g.) the "F.dist" function in Excel.