

Seminar II

*Problem 1.*

Discuss reasons why a collateralized asset may be of higher value to the entrepreneur than to an outside investor.

*Problem 2. (Exam, spring 2009)*

Jenny has a business idea she wants to develop. Her project is risky: with probability  $p$ , it is successful while with probability  $(1 - p)$  it fails. Success means that investing an amount  $I$  returns  $RI$ , where  $R > 1$  is the return per unit of investment. Failure means a zero return on the project:  $R^F I = 0$ . The probability  $p$  of success depends on Jenny's own efforts: if she works hard, then  $p = p_H$ , while if she does not work hard, then  $p = p_L$ , where

$$0 < p_L < \frac{1}{R} < p_H < 1.$$

By not working hard, she will gain a benefit  $BI$ , where  $B$  is the benefit per unit of investment, satisfying

$$(p_H - p_L)\left(R - \frac{1}{p_H}\right) < B < 1 - p_L R.$$

Jenny has available own funds of size  $A \geq 0$ . If she wants to invest more than  $A$ , she will need funding from outside investors. Assume that the capital market is competitive, that Jenny is risk neutral, that limited liability prevails, and that efforts are not observable.

- a) How much will Jenny invest in the project?
- b) Find an expression for her borrowing capacity (or debt capacity), and discuss how this borrowing capacity is affected by the extent of the moral-hazard problem.

- c) Suppose now that even failure of the project has a positive return, but lower than the return following success:  $0 < R^F < R$ . Explain the difference between debt and equity as ways of funding a firm. Explain in particular why, in this situation, it is not optimal for Jenny to fund her investment by issuing equity only.

*Problem 3.*

Exercise 4.10 in Tirole, pp. 191-192.

*Problem 4.*

Review Problem 2, part (iii), in Tirole, p. 626.