

# Seminar 4. Question B. Sketch of answer

①

1) Exogenous:  $S_x, Y_x, P_x, M, F_S, G, T, p_e, \bar{E}$

Predetermined:  $M_0, B_0, F_{no}, F_x, P$

Endogenous:  $E, F_r, Y, i, e_e, S, Y_p, W_r, r, R$

2) Keywords are expected returns, risk and risk aversion, expectations that differ between investors. Expand on these.

3) With appropriate substitutions from the other equations, the equilibrium condition for the FX-market can be written

$$(i) \quad F_S = -\frac{P}{E} \left[ (i - i_x + \varepsilon \frac{E - \bar{E}}{\bar{E}}) \frac{M_0 + B_0 + EF_{no}}{P} \right] - F_x^*$$

Differentiating (i) with respect to  $i$  and  $E$ :

$$0 = \left[ -\frac{P}{E} \phi_r' \right] di + \left[ \frac{P}{E^2} \phi(r, W_r) - \frac{P}{E} \phi_r' \varepsilon \frac{1}{E} - \frac{P}{E} \phi_r' \frac{F_{no}}{P} \right] dE$$

Calculate the derivatives for  $\phi(r, W_r) = \frac{EF_{no}}{P}$  and  $E = \bar{E}$  and multiply with  $E/P$  on both sides

$$0 = -\phi_r' di + \left[ \frac{EF_{no}}{P} \cdot \frac{1}{E} - \phi_r' \varepsilon \frac{1}{E} - \phi_r' \frac{EF_{no}}{P} \frac{1}{E} \right] dE$$

Solve

$$(ii) \quad \frac{dE/E}{di} = \frac{\phi_r'}{\underbrace{(1-\varepsilon)EF_{no}/P}_+ - \underbrace{\phi_r' E}_+} < 0$$

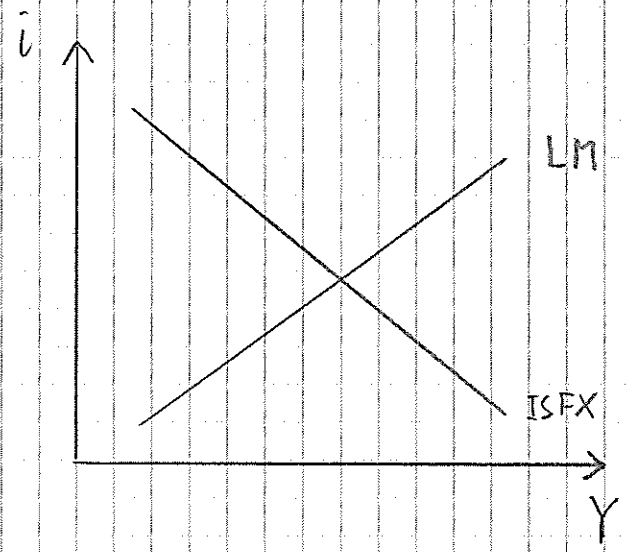
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Discuss signs, related to answer to q. 2.

Degree of capital mobility is measured by  $|f'|$ .

$$|f'| \uparrow \rightarrow \left| \frac{dE/E}{di} \right| \uparrow$$

4)



ISFX represents the combinations of  $i$  and  $Y$  that are compatible with joint (short-run) equilibrium in the goods market and the foreign exchange market. Defined by:

$$(0) \quad Y = \left( Y - S^* \frac{EF^*}{P} - T, \frac{M_0 + B_0 + EF_{f0}}{P}, i - r_e, S^* \right) + G + X \left( \frac{EP^*}{P}, Y, Y^* \right)$$

$$(00) \quad F_S = - \frac{P}{E} \left( i - i^* + \left( \frac{E - \bar{E}}{\bar{E}}, \frac{M_0 + B_0 + EF_{f0}}{P} \right) - F^* \right)$$

LM combinations of  $i$  and  $Y$  compatible with equilibrium in the money market.

Slopes:

IS:  $i \uparrow$  reduces demand directly in (0) and indirectly because  $E \downarrow$  as follows from (00). (Some ambiguity in the latter effect if  $F^* > 0$ ).

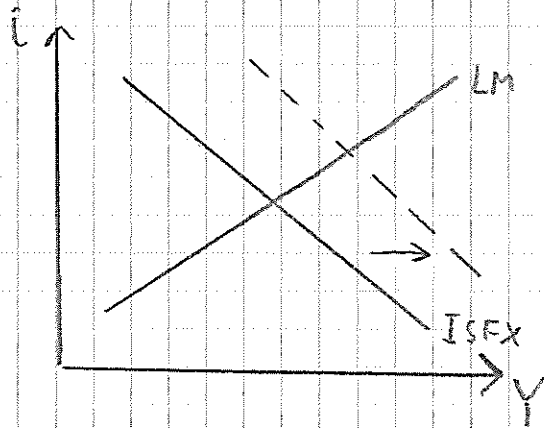
LM:  $Y \uparrow$  leads to increased money demand which raises the interest rate when  $M$  is given. (eq. (3))

5)  $i_x \uparrow$

The LM-curve is unaffected.

Does  $S_x$  increase too, or is it constant, which requires that  $p_{xe}$  goes up together with  $i_x$ ?

If  $S_x$  constant,  $i_x$  affects only FX-equation (00), where  $i_x \uparrow \rightarrow E \uparrow$ , and ISFX shifts to the right.



$i_x \Rightarrow i \uparrow, Y \uparrow$

Increase in  $S_x$  shifts ISFX in opposite direction.

Net effect ambiguous then.

Increase in  $i$  is less than increase in  $i_x$ .

Suppose  $S_x$  is constant. If  $\Delta i = \Delta i_x$ , then  $E$  is constant. But then aggregate demand must be lower than before. But if  $Y$  were lower there would be no reason for  $i$  to increase.

If  $S_x$  increases too, that means an even lower increase in  $i$  (or possibly a decline).

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Comparison to question A.

In A the short run effect is also that  $i$  increases, but less than the increase in  $i_x$ .

That it increases we can infer from that  $Y$  goes up. This raises money demand and hence  $i \uparrow$ .

That  $\Delta i < \Delta i_x$  follows from that  $\dot{E}/E < 0$  along the saddle-path to the new equilibrium and

$$\text{VIP: } \dot{i} = i_x + \dot{E}/E.$$

Hence, qualitatively we get the same result, unless  $\beta_x$  increases and has a sufficiently strong effect to make  $i$  and  $Y$  decline.

(Mechanisms and quantitative effects are/can be different).

b) For simplicity focus on case where  $\beta_x$  is constant.

Three possible policies:

a) Sterilized intervention: Sell foreign currency, buy domestic bonds.  $F_{\$} \downarrow$ .

b) Reduce  $M$  by selling domestic bonds

c) Unsterilized intervention: Sell foreign currency.  $F_{\$} \downarrow, M \downarrow$

a) Shifts the ISFX curve back to where it was before.  
 Effect of  $i^*$  is isolated to foreign exchange market.

Problem: Intervention may have to be large if capital mobility is strong.

b) Shifts LM-curve upwards until  $\Delta i = \Delta i^*$ .

Side effect: Output is reduced relative to what it was before the shift.

c) This is the same as combining a) and b) in equal amounts. The ISFX-curve shifts back, but not all the way. The LM-curve shifts upward but less than needed to make  $\Delta i = \Delta i^*$ .

Side effects on other variables are smaller.