## Problem set 2 ECON 4330

## Part 1: An infinite horizon model

In this problem we consider an infinite horizon model with a representative agent and perfect foresight who faces a fixed world market interest rate. Each period, the agent must obey the following budget constraint:

$$C_s + B_{s+1} = Y_s + (1+r)B_s$$

1. Based on the fact that the budget constraint holds for every period from t to t+T, show that this implies

$$(1+r)B_t = \sum_{s=t}^{t+T} \left(\frac{1}{1+r}\right)^{s-t} (C_s - Y_s) + \frac{B_{t+T+1}}{(1+r)^T}$$

2. Explain the intuition behind

$$\lim_{T \to \infty} \frac{B_{t+T+1}}{(1+r)^T} = 0$$

- 3. Impose this restriction and assume that  $C_s = cY_s$  and  $Y_s = (1+g)^{s-t}Y_t$ .
  - (a) Find the intertemporal budget constraint for this case (when g < r).
  - (b) Imagine that keeping consumption at a fixed share c of output indeed is the optimal consumption-choice of a representative agent. Is c above or below one?
  - (c) Assume g = 0. What does the time-profile of  $B_t$  look like for the value of c you found in b)?
  - (d) Assume g > 0 (but also g < r). What does the time-profile look like now?

- 4. Now assume (as in question 6 of the first problem) that output is a function of the capital stock,  $Y_t = A_t F(K_t)$ . The utility function is specified as  $U_t = \sum_{s=t}^{\infty} \beta^{s-t} u(C_s)$ . Use the period s budget constraint to insert for  $C_s$  in the utility function.
  - (a) Find the first-order condition with respect to  $K_{t+1}$  and  $B_{t+1}$
  - (b) Suppose productivity is constant  $A_s = A_t$  for all  $s \ge t$  and that, by coincidence,  $\beta(1+r) = 1$ . Describe the time-profiles of consumption, investment and the current account (you can assume that initial net foreign assets,  $B_t$ , are zero).
  - (c) Sketch the effects on consumption, investment and the current account from
    - i. An unexpected temporary increase in productivity in period t+1 (that only lasts one period)
    - ii. A temporary increase in productivity in t+1 (that only lasts one period) that becomes known at the beginning of period t
    - iii. An unexpected permanent increase in productivity

## Part 2: Discussion

Discuss the article in the link below. Everyone should prepare at least:

- One question or comment relating the article to the curriculum so far.
- One question or comment to something in the article we cannot explain by the models presented so far.

http://www.economist.com/news/finance-and-economics/21690073-globalisation-can-make-everyone-better-does-not-mean-it-will-trade