### Environmental Economics 4910

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### **Outline** - Economics

#### micro

- game theory
- public economics
- political economics
- development economics
- behavioral economics
- international trade
- macro

### **Environmental Problems**

- Overusing/exploiting renewable and exhaustible resources
  - Atlantic northwest cod fishery has collapsed before... (1992).
- Land use changes (e.g. tropical deforestation)
  - football pitch cleared from the Amazon rainforest every minute.
- Waste (e.g. hazardous, or plastic)
  - 40 percent of plastic is used only once. An estimated five trillion pieces of plastic floating on and in the world's oceans.
- Water (over-usage, or contamination)
  - 9 percent of the world's population don't have access to safe drinking water. 40 percent of the world's population don't have proper sanitation (WHO).
- Air (particles, NO<sub>x</sub>, acid rain; ozone layer)
  - Reduce life expectancy by 1y (LA), 4y (China), 9y (India).
- Greenhouse gases (e.g., CO<sub>2</sub>)
  - UN goal: 2 (1,5)°C, but "93 percent chance that global warming will exceed 4C by the end of this century".

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Environmental Economics

- National vs. international
- Political vs. marked-based
- Number of sources and number of affected parties
- Affecting producers vs consumers
- Tangible vs. nonverifiable pollutants
- Flow pollutants vs. accumulating stocks
- Contemporary vs. long-term effects

### Outline

- Welfare theorems and market failures (micro)
- Policy instruments (Pigou, Coase, Weitzman) (public ec.)
- Trade and the environment (int. trade)
- Self-enforcing vs. binding agreements (game theory)
- S Architectures for agreements (economic systems)
- Free-riding and participation (contract theory)
- Supply-side environmental policy (resource ec.)
- Oeforestation and REDD contracts (development ec.)
- Interpretation of the Future: Discounting (behavioral ec.)
- Integrated Assessment Models (Traeger) (macro)

#### Consumption and Production: "ECON 101"

• Consumers *i*'s utility and good *j*'s production function:

$$u^i\left(x_1^i,...,x_J^i
ight)$$
 and  $\sum\limits_i x_j^i \leq f^j\left(y_j^1,...,y_j^K
ight)$  ,

- ...where i ∈ {1, ..., I} consumes x<sub>j</sub><sup>i</sup> of good j ∈ {1, ..., J}, and y<sub>j</sub><sup>k</sup> is the quantity of input k ∈ {1, ..., K} used in the production of good j.
- Pareto optimality (PO) requires that

$$\max_{\{x_j^i\}, \{y_j^k\}} u^1 \left(x_1^1, ..., x_J^1\right) \text{ s.t.}$$

$$u^i \left(x_1^i, ..., x_J^i\right) \geq \overline{u}^i, \forall i \qquad (\text{shadow value: } \lambda_i),$$

$$\sum_i x_j^i \leq f^j \left(y_j^1, ..., y_j^K\right) \quad \forall j \quad (\text{shadow value: } \mu_j),$$

$$\sum_j y_j^k \leq \overline{y}^k \quad \forall k \qquad (\text{shadow value: } \eta_k).$$

for some default levels (ū<sup>i</sup>'s) and input quantities (y<sup>k</sup>'s).
Do we need to include labor/leisure in the model?

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#### Environmental Economics

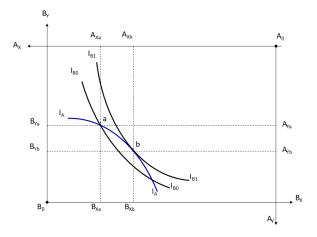
• Lagrange (/Kuhn-Tucker) problem with foc for  $x_i^i$  and  $y_i^k$  (if  $\lambda_1 \equiv 1$ ):

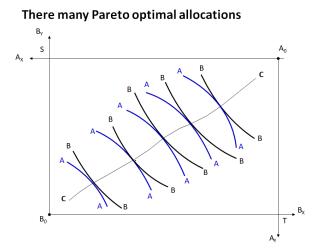
$$\begin{aligned} \lambda_i u_j^i &= \mu_j, \\ \mu_j f_k^j &= \eta_k. \end{aligned}$$

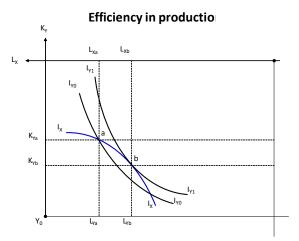
- The shadow values depend on the default levels; the  $\overline{u}_i$ 's.
- For PO, it is sufficient that the foc's hold for *some* shadow values.
- When the foc's are combined:

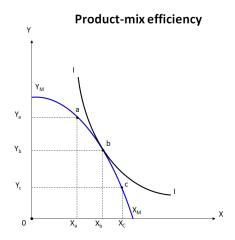
$$\begin{array}{ll} \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{\mu_{j}}{\mu_{j'}} = \frac{u_{k}^{i'}}{u_{l}^{i'}} \,\,\forall \left(i,i'\right), \left(j,j'\right) \quad (\text{efficiency in consumption}), \\ \frac{f_{k}^{j}}{f_{k'}^{j}} & = & \frac{\eta_{k}}{\eta_{k'}} = \frac{f_{k}^{j'}}{f_{k'}^{j'}} \,\,\forall \left(k,k'\right), \left(j,j'\right) \quad (\text{efficiency in production}), \\ \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{f_{k}^{j'}}{f_{k}^{j}} \,\,\forall \left(j,j'\right), i,k \qquad (\text{efficiency in exchange}). \end{array}$$

#### Edgeworth box: 2 Individuals (A and B), 2 goods (X and Y)







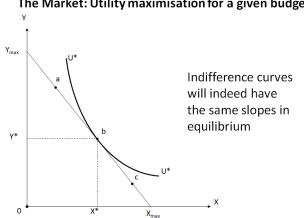


- Consumers' choice, given endowment  $E^i$  (with shadow value  $v_i$ ):  $\max_{\{x_j^i\}_j} u^i \left(x_1^i, ..., x_j^i\right) \text{ s.t. } \sum_j p_j x_j^i \leq E^i \quad (v_i) \Rightarrow u_j^i = v_i p_j.$
- Producers:

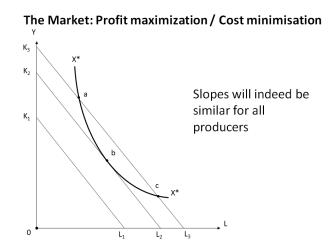
$$\max p_j f^j \left( y_j^1, ..., y_j^K \right) - \sum_k w^k y_j^k \Rightarrow p_j f_k^j = w^k.$$

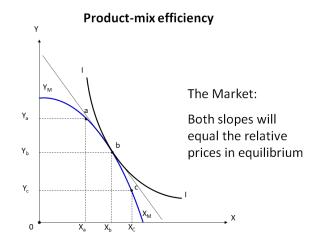
Combined:

$$\begin{array}{lll} \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{\mu_{j}}{\mu_{j'}} = \frac{u_{j}^{i'}}{u_{j'}^{i'}} \text{ if just } \mu_{j} = p_{j}, \\ \frac{f_{k}^{j}}{f_{k'}^{j}} & = & \frac{\eta_{k}}{\eta_{k'}} = \frac{f_{k}^{j'}}{f_{k'}^{j'}} \text{ if just } \eta_{k} = w^{k}, \\ \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{f_{k}^{j'}}{f_{k}^{j}} = \frac{p_{j}}{p_{j'}} \ \forall (j,j'), i, k. \end{array}$$



#### The Market: Utility maximisation for a given budget



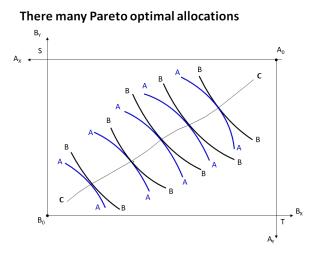


### Consumption and Production: Welfare Theorems

#### Theorem

- Every market equilibrium  $\Rightarrow$  Pareto optimal.
- ② Every Pareto optimal outcome ⇒ market equilibrium given some allocation of endowments.
  - Where is the environment?

#### The final allocation depends on the endowments



### Consumption and Production: With Externalities

• Externalities from inputs/productions to consumers:

$$u^i\left(x_1^i,...,x_J^i,\sum_j g_j
ight)$$
 and  $\sum_i x_j^i \leq f^j\left(y_j^1,...,y_j^K,g_j
ight)$ .

• Pareto Optimality is given by the same conditions as above, plus:

$$\mu_j f_g^j = \sum_i \lambda_i \left( -u_g^i \right) = \sum_i \frac{\mu_j}{u_j^i} \left( -u_g^j \right) \Rightarrow f_g^j = \sum_i \frac{-u_g^i}{u_j^i}$$

- Market equilibrium with no regulation: j emits until f<sup>j</sup><sub>g</sub> = 0.
  With regulation or tax t<sup>j</sup><sub>g</sub> on j's emission: p<sub>j</sub>f<sup>j</sup><sub>g</sub> = t<sup>j</sup><sub>g</sub>
- This coincides with the PO outcome if

$$f_g^j = \frac{t_g^j}{p_j} = \sum_i \frac{-u_g^i}{u_j^i} = \sum_i \frac{-u_g^i}{p_j u_1^i / p_1} \Rightarrow t_g^j = \sum_i \frac{-u_g^i}{u_1^i} p_1.$$

• So, the emission **tax should be the same for all firms**, no matter how valuable/dirty they are.

# Consumption and Production: With Externalities (cont.)

- If there is a numeraire good (i.e.,  $u_1^i = 1 = p_1$ ), then  $t_g^j = -\sum_i u_g^i$ .
- Alternatively, the regulator may decide on the  $g_j$ 's directly.
- For each such policy, there will be equilibrium prices and quantities such that payoffs are functions  $u_i(\mathbf{g})$  and profits  $\pi_j(\mathbf{g})$ .
- Larger g<sub>j</sub>'s is likely to benefit producer j (B<sub>j</sub> (g<sub>j</sub>)) but be costly for consumers (C<sub>i</sub> (g<sub>j</sub>)).

#### Externalities and Public Goods

Let g<sub>i</sub> be emission by agent i ∈ N ≡ {1, ..., n}, and g = {g<sub>1</sub>, ..., g<sub>n</sub>}.
Externalities:

 $u_{i}\left(\mathbf{g}
ight)=B_{i}\left(g_{i}
ight)-C_{i}\left(\mathbf{g}
ight)$ , if  $\partial C_{i}/\partial g_{j}
eq0$  for some j
eq i.

• Uniformly mixing pollutant (and public good/bad):

$$u_{i}\left(\mathbf{g}
ight)=u_{i}\left(g_{i},\,G
ight)=B_{i}\left(g_{i}
ight)-\mathcal{C}_{i}\left(G
ight)$$
 , where  $G=\sum_{j\in\mathcal{N}}g_{j}$  .

- To get an interior solution, assume  $u_i$  is concave in  $g_i$ 
  - For example: Every  $B_i$  is concave while  $C_i$  is convex.
- Business as usual (interior) equilibrium:

$$B_{i}^{\prime}\left(g_{i}\right)=C_{i}^{\prime}\left(G
ight).$$

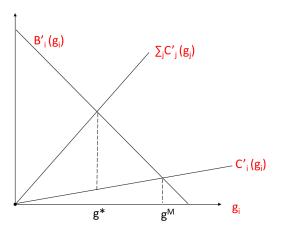
- Suppose transfers enter linearly and additively in u<sub>i</sub>.
- The first-best (FB; the unique PO outcome with transfers):

$$B_{i}^{\prime}\left(g_{i}^{*}
ight)=\sum_{j\in\mathcal{N}}C_{j}^{\prime}\left(G^{*}
ight).$$

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#### Externalities and Public Goods

#### Every polluter "i" emits too much



#### Pigou Taxes (The "Incorrect Prices" Approach)

- Suppose *i* pays  $t_i g_i$  and receives  $T_i(\mathbf{g})$ .
- Then, in equilibrium:

$$rac{\partial B_{i}\left(g_{i}
ight)}{\partial g_{i}}=C_{i}^{\prime}\left(G
ight)+t_{i}-rac{\partial T_{i}\left(\mathbf{g}
ight)}{\partial g_{i}}.$$

• Equivalent: A subsidy  $T_i(\mathbf{g}) - t_i g_i$ , f.ex.  $t_i \cdot (\overline{g}_i - g_i)$ .

• This coincides with the first-best if:

$$t_i = \sum_{j \in \mathcal{N} \setminus i} C_j'\left(G
ight) ext{ and } rac{\partial \mathcal{T}_i\left(\mathbf{g}
ight)}{\partial g_i} = 0.$$

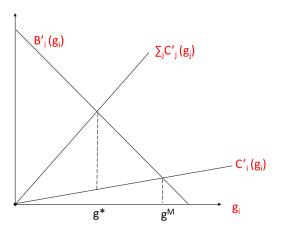
No earmarking: It is (almost) irrelevant how tax revenues are spent.
 For example: T<sub>i</sub> (g) = ∑<sub>i∈N\i</sub> t<sub>i</sub>g<sub>i</sub>/ (n − 1).

• If  $C'_i \approx 0$  for each emitter *i*, the linear tax is the same for all:

$$t = \sum_{j \in \mathcal{N}} C'_{j}(G^{*}) \Rightarrow B'_{i}(g_{i}) = \sum_{j \in \mathcal{N}} C'_{j}(G^{*}).$$

#### Pigou Taxes (The "Incorrect Prices" Approach)

#### Every polluter "i" emits too much



#### Pigou Taxes - Uncertainty

• Facing the same tax, we get:

$$B_{i}'(g_{i},\epsilon_{i})=t=B_{j}'(g_{j},\epsilon_{j})\,\forall\,(i,j)\in N^{2}$$

even if individual shocks  $(\epsilon_i)$  are private information.

• Then, define  $\boldsymbol{\epsilon}=(\epsilon_1,...,\epsilon_n)$  and

$$B(t,\epsilon) \equiv \sum_{i\in N} B_i \left( B_i^{\prime-1}(t,\epsilon_i),\epsilon_i \right).$$

The optimal tax is given by:

$$\max_{t} \mathsf{E}\left[B\left(t, \epsilon\right) - C\left(\sum_{i \in N} B_{i}^{\prime-1}\left(t, \epsilon_{i}\right)\right)\right]$$

#### Pigou Taxes - Uncertainty - Example Q

• Consider the quadratic approximation (Y=exp. "bliss" point):

$$B\left(G,\epsilon
ight)=-rac{b}{2}\left(Y-G-\epsilon
ight)^{2}$$
 and  $C\left(G
ight)=rac{c}{2}G^{2}$ 

where the aggregate shock is  $\epsilon \in \mathbb{R}$ ,  $E\epsilon = 0$ , and variance  $E\epsilon^2 = \sigma_{\epsilon}^2$ . • The equilibrium, given t:

$$\max_{G} -\frac{b}{2} \left(Y - G - \epsilon\right)^{2} - tG \Rightarrow b \left(Y - G - \epsilon\right) = t.$$

The tax pins down B' and B, leaving the uncertainty to G and C(G).
The optimal t:

$$\max_{t} - \frac{t^{2}}{2b} - \mathsf{E}\frac{c}{2}\left(Y - \epsilon - t/b\right)^{2} \Rightarrow t^{*} = c\left(Y - t^{*}/b\right) = \frac{cbY}{b+c}.$$

• The uncertainty does not influence the optimal level of t. (Why?)

• Welfare loss relative to no uncertainty increases in c:

$$L_t^{\epsilon} = \frac{c\sigma_{\epsilon}^2}{2}.$$

#### Pigou Taxes and Tax Revenues

• Tax revenues (at the above optimal  $t^*$ ):

$$\mathsf{E} t \mathsf{G} = \mathsf{E} \frac{c b \mathsf{Y}}{b + c} \left( \mathsf{Y} - \epsilon - \frac{c \mathsf{Y}}{b + c} \right) = \frac{c b^2 \mathsf{Y}^2}{b + c}.$$

• Tax revenues (at general t):

$$t(Y-\epsilon-t/b)$$

- Normally, revenues necessitate distortionary taxes.
- With the social value  $\lambda$ , the optimal t is thus:

$$\max_{t} - \frac{t^{2}}{2b} - \mathsf{E}\frac{c}{2} \left(Y - \epsilon - t/b\right)^{2} + \mathsf{E}\lambda t \left(Y - \epsilon - t/b\right) \Rightarrow$$
$$t = c \left(Y - t/b\right) + \lambda b \left(Y - 2t/b\right) = \frac{cb + \lambda b^{2}}{b + c + 2\lambda b} Y.$$

which can be increasing or decreasing in λ...
Q: (When) is there a "double dividend"?

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#### Proposition

- Weak form: The regulation with Pigou tax revenues raises social efficiency relatively to regulation without tax revenues.
  - Holds trivially
- **2** Strong form: The optimal tax is larger than the Pigovian level.
  - The strong form may or may not hold.

# Coase (The "Property Rights" Approach)

- As long as the property rights are well defined, bargaining among the parties lead to an efficient outcome.
- The "Chicago school" argues that an externality does NOT imply that the government should act.
- Instead, the parties have an incentive to sort things out themselves.
- If an upstream polluter harms a downstream water consumer, the two will both benefit from coming to some kind of agreement.
- Coase (1960) uses the example of a cattle ranger and a farmer.
- With G cows, the benefit (profit) to the cattle ranger may be B(G) = (20 G) G.

$$B\left( G+1\right) -B\left( G\right) =19-2G.$$

- The cost (damage) to the farmer may be C(G) = 6G.
- The optimal number  $G^*$  is 7.

# Coase (The "Property Rights" Approach)

- If the "property right" belongs to the farmer,  $G_0 = 0$ .
  - The cattle ranger is willing to compensate the farmer for the damages as long as  $G \leq 7$ .
- If the "property right" belongs to the cattle ranger,  $G_0 = 10$ .
  - The farmer is willing to compensate the cattle ranger for reducing G as long as G > 7.
- Under "liability law", both can do as they want, but the cattle ranger must compensate the farmer for any damages.
  - Again, the equilibrium is 7.
  - This holds regardless of *how* the property rights are allocated.

### Coase (The "Property Rights" Approach)

- Suppose disagreement leads to the "default" payoffs  $u_i^D$ . For example,  $u_i^D$  may equal  $u_i$  ( $\mathbf{g}^{BAU}$ ).
- To negotiate a better outcome, a "proposer", *i*, would prefer to:

$$\max_{\mathbf{g},\mathbf{t}} u_{i} = B_{i}\left(g_{i}\right) - C_{i}\left(G\right) - t_{i} \text{ s.t.}$$
$$u_{j} = B_{j}\left(g_{j}\right) - C_{j}\left(G\right) - t_{j} \geq u_{j}^{D}\left(\mathsf{IR}_{j}\right).$$

- With budget balance,  $t_i = -\sum_{j \in N \setminus i} t_j$ , so *i* prefers the largest  $t_j$ 's satisfying IR<sub>j</sub>.
- $IR_i$  can be substituted into  $u_i$ , so that *i* maximizes:

$$\begin{aligned} \max_{\mathbf{g},\mathbf{t}} u_i &= B_i\left(g_i\right) - C_i\left(G\right) + \sum_{j \in N \setminus i} \left[B_j\left(g_j\right) - C_j\left(G\right) - u_j^D\right] \\ &= \sum_{j \in N} \left[B_j\left(g_j\right) - C_j\left(G\right)\right] - \sum_{j \in N \setminus i} u_j^D = \sum_{j \in N} u_j\left(\mathbf{g}^*\right) - \sum_{j \in N \setminus i} u_j^D. \end{aligned}$$

In other words: *i* maximizes the sum of payoffs (minus a constant).
Consequently, the proposed g<sub>j</sub>'s coincides with the first best.

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#### Theorem

- The parties negotiate the efficient outcome, regardless of the initial allocation of property rights (i.e., the default outcome,  $u_j^D$ ) as long as there are no 'transaction costs.'
- For example,  $u_j^D$  may reflect BAU (i.e., everyone has the "right" to emit as much as they want), or  $u_j^D$  could be  $u_j$  (**0**), i.e., no-one has the right to emit anything.
- "Transaction costs" (*tc<sub>i</sub>*) must be sufficiently small:

$$tc_i \leq \sum_{j \in \mathcal{N}} \left[ u_j \left( \mathbf{g}^* \right) - u_j^D 
ight].$$

- Q: What is this "transaction cost"?
- Q: Who should have the bargaining power? What should the property rights be, if there are substantial transaction costs?

# Emssion Trading Systems (ETS): A Brief History

- Theory by Coase '60, Crocker '66, Dales '68, Montgomery '72
- Computer simlulates late 60s by the EPA
- 1977 Clean Air Act: Permitted "offset-mechanism"
- 1990 Clean Air Act: Cap-and-trade in (SO2)
  - cost savings of \$700-\$800m/year compared to uniform emission rate standard (Carlson et al. '00 JPE)
  - SO2 emissions were reduced by 50% from 1980 levels by 2007
- 1997: Kyoto: CDM and JI
- 2005: EU ETS: First and largest CO2 ETS
- RGGI, WCI, China (2021?)
- Linkages considered, but no global system

#### Trading Pollution Permits ("Missing Market")

 If i has the right to emit Q<sub>i</sub><sup>0</sup>, while j has the right to emit Q<sub>j</sub><sup>0</sup>, the two might benefit from trading without increasing total emission:

$$g_i+g_j\leq Q_i^0+Q_j^0.$$

- That is, if *i* emits  $g_i$  and sell  $Q_i^0 g_i$ , *j* can emit  $g_j$  from buying  $g_j Q_j^0 = Q_i^0 g_i$  from *i*.
- This trade is beneficial as long as  $B'_i < B'_j$ .
- With efficient trade,  $B'_i = B'_i$ .

n

• More generally, a proposer *i* prefers to:

$$\begin{array}{lll} \max_{\mathbf{g},\mathbf{t}} u_i &=& B_i\left(g_i\right) - C_i\left(G\right) - t_i \text{ s.t.} \\ u_j &=& B_j\left(g_j\right) - C_j\left(G\right) - t_j \geq u_j^D\left(\mathsf{IR}_j\right) \text{ and} \\ G &=& \sum_{j \in N} g_j \leq \sum_{j \in N} Q_j^0 \text{ and } \sum_{j \in N} t_j \geq 0. \end{array}$$

- Consequently,  $B'_i = B'_j$  for all pairs (i, j)
- ... regardless of the endowments, i.e.,  $u_j^D$ .

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#### Perfect Pollution Markets ("Missing Market")

- If  $n \to \infty$ , every *i* is likely to take the permit price *p* as given.
- If *i* owns  $Q_i^0$  permits already, *i* solves

$$\max_{g_{i}}B_{i}\left(g_{i}\right)-C_{i}\left(G\right)-p\left(g_{i}-Q_{i}^{0}\right)\Rightarrow B_{i}'\left(g_{i}\right)=p,$$

since  $G = \sum_{j \in N} Q_j^0$  is independent of  $g_i$ .

• The outcome is FB if:

$$p = \sum_{j \in \mathcal{N}} C'_j (G^*)$$

 I.e., the outcome is FB if the quantity (and thus the price) is "right", i.e., if:

$$B_i'(g_i) = p = \sum_{j \in N} C_j'(G^*).$$

# Perfect Pollution Markets ("Missing Market")

#### Proposition

- When each emitter is a price-taker, the permit market equilibrium is efficient, regardless of the initial allocation of rights.
- So, permit trade => FB whether *n* is small or  $n = \infty$ .
  - Should we expect FB for any n? Why/why not?
- Q: Why is the initial allocation  $(Q_i^0)$  irrelevant?
- Q: Is that useful for the regulator? How will the regulator decide on the initial endowments? Must Q<sub>i</sub><sup>0</sup> be exogenous?
- What if  $Q_i^0$  depends on past production or past emissions?
- Montgomery '72: With  $G_j = \sum_{i \in N} h_{ij}g_i$ , the FB requires:

$$\mathcal{B}_{i}^{\prime}\left(g_{i}
ight)=\sum_{j\in N}h_{ij}\mathcal{C}_{j}^{\prime}\left(\mathcal{G}_{j}^{*}
ight)\Rightarrow ext{Pollution markets FB iff }p_{j}=\mathcal{C}_{j}^{\prime}.$$

### Prices vs. Quantities (Weitzman '74)

#### Proposition

• The efficiency loss under quotas is smaller than under prices/taxes ( $L_G^{\epsilon} < L_t^{\epsilon}$ ) IFF b < c.

#### Perfect Pollution Markets - Uncertainty

• Consider the quadratic approximation (Y=exp. "bliss" point):

$$B\left(G,\epsilon
ight)=-rac{b}{2}\left(Y-G-\epsilon
ight)^{2}$$
 and  $C\left(G
ight)=rac{c}{2}G^{2}$ ,

where the aggregate shock is  $\epsilon \in \mathbb{R}$ ,  $E\epsilon = 0$ , and variance  $E\epsilon^2 = \sigma_{\epsilon}^2$ . • With uncertainty, the optimal cap is

$$\max_{G} \mathsf{E}B(G,\epsilon) - C(G) = \max_{G} \mathsf{E} - \frac{b}{2} (Y - G - \epsilon)^{2} - \frac{c}{2} G^{2}$$
$$= \max_{G} \mathsf{E} - \frac{b}{2} \left[ (Y - G)^{2} - 2\epsilon (Y - G) + \epsilon^{2} \right] - \frac{c}{2} G^{2}$$
$$= \max_{G} - \frac{b}{2} \left[ (Y - G)^{2} + \sigma_{\epsilon}^{2} \right] - \frac{c}{2} G^{2} \Rightarrow G^{*} = \frac{b}{c + b} Y.$$

• The shock does not affect G, but only B'.

• Relative to no uncertainty, the welfare loss is:

$$L_G^{\epsilon} = \frac{b\sigma_{\epsilon}^2}{2}$$

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#### Pigou Taxes - Uncertainty - Example Q

• The equilibrium, given emission tax t:

$$\max_{G} -\frac{b}{2} (Y - G - \epsilon)^{2} - tG \implies b (Y - G - \epsilon) = t$$
$$\implies G = Y - \epsilon - t/b.$$

• So, G becomes stochastic. The optimal t:

$$\begin{aligned} \max_{t} &-\frac{t^{2}}{2b} - \mathsf{E}\frac{c}{2}\left(Y - \epsilon - \frac{t}{b}\right)^{2} \\ &= \max_{t} - \frac{t^{2}}{2b} - \mathsf{E}\frac{c}{2}\left[\left(Y - \frac{t}{b}\right)^{2} - 2\epsilon\left(Y - \frac{t}{b}\right) + \epsilon^{2}\right] \\ &= \max_{t} - \frac{t^{2}}{2b} - \frac{c}{2}\left[\left(Y - \frac{t}{b}\right)^{2} + \sigma_{\epsilon}^{2}\right] \Rightarrow t^{*} = \frac{cbY}{b + c}.\end{aligned}$$

• The uncertainty does not influence  $t^*$ , but Welfare loss is:

$$L_t^{\epsilon} = \frac{c\sigma_{\epsilon}^2}{2}.$$

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#### Proposition

- The efficiency loss under quotas is smaller than under prices/taxes,  $L_G^{\epsilon} < L_t^{\epsilon}$ , IFF b < c.
- This holds generally when *B* and *C* are approximated by quadratic functions, no matter the distribution of errors, and even if there are (additive) shocks in the *C* function.
- Q: How can the losses be reduced further?
- By hybrid schemes?
- Floor/ceiling for price?

#### Prices vs. Quantities: Revenues

• Pigou taxes raises revenues, which has an additional benefit:

$$tG = \frac{cbY}{b+c} \left(Y - \epsilon - \frac{cY}{b+c}\right)$$

• The willingness to pay for a quota is B', so the revenues when auctioning the initial quota endowments are:

$$\frac{b}{c+b}Yb\left(Y-\frac{b}{c+b}Y-\epsilon\right)=\frac{b^2Y}{c+b}\left(\frac{c}{c+b}Y-\epsilon\right)$$

- This has the same mean as the expected Pigou tax revenues.
- The variance of the auction revenues is smaller IFF b < c.
- This adds to the benefits of quotas, rather than taxes, IFF b < c.

- What other things determine the choice of policy instrument?
- Why are quotas more often seen in practice, than Pigou taxes?
- Why do firms prefer (tradable permits)?
- If firms like to be compensated, why can't tax revenues return to firms, instead of free tradable permits?
- What do you thing left-wing and right-wing policy makers prefer?
- If the two wings must negotiate, what do you think they will agree on?