

## Problem set 2 – ECON 4921, September 19, 2007

### 1) The putting out system

Use the model presented on the lectures as a starting point, but assume:

$$U(w,e) = w - \frac{1}{2}e^2$$
$$f(e) = e$$

output price,  $p = 1$   
 $w = q \cdot e$

- Show that in equilibrium:  $e = q = \frac{1}{2}$
- Draw iso-profit and iso-utility curves, illustrate the equilibrium.
- Explain the intuition behind U-shaped iso-utility curves.
- For which values of  $q$  is a pareto-improvement possible, if  $e$  is set to 1?
- Why isn't such  $(e,q)$ -combinations incentive compatible?

### 2) Contingent renewal

Use the model presented on the lectures as a starting point, but assume:

$$U(w,e) = w - \frac{1}{2}e^2$$

Probability of contract renewal,  $p = A + a \cdot e$ , for a suitable choice of  $a$  and  $A$ .

- Derive the optimal effort of the worker as a function of  $w$ .
- Show that:  $e = aR / (1+r-p)$ , where  $R = r(u(w,e) / r - Vu)$  is the unemployment rent.
- Show that  $de / dw = a / (1+r-p)$
- Compare the equilibrium with the equilibrium in the putting-out system.