

## Exercises for Seminar 5 Fall 2011

### 1) *The putting out system*

Use the model presented on the lectures as a starting point, but assume:

$$U(w, e) = w - \frac{1}{2}e^2$$
$$f(e) = e$$

output price  $p = 1$  and  $w = q \times e$

1. Show that in equilibrium:  $e = q = \frac{1}{2}$
2. Draw iso-surplus and iso-utility curves, illustrate the equilibrium.
3. Explain the intuition behind U-shaped iso-utility curves.
4. For which values of  $q$  is a pareto-improvement possible, if  $e$  is set to 1?
5. Why isnt such  $(e, q)$ -combinations incentive compatible?

### 2) *Contingent renewal*

Use the model presented on the lectures as a starting point, but assume:

$$U(w, e) = w - \frac{1}{2}e^2$$

Probability of contract renewal,  $p = A + a \times e$ , for a suitable choice of  $a$  and  $A$ .

1. Derive the optimal effort of the worker as a function of  $w$ .
2. Show that  $e = \frac{aR}{1+r-p}$ , where  $R = r \frac{u(w,e)}{r-Vu}$  is the employment rent.
3. Show that  $\frac{de}{dw} = \frac{a}{1+r-p}$
4. Compare the equilibrium with the equilibrium in the putting-out system